

# Heating old neutron stars

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# Heating neutron star matter by weak interactions

- Chemical (“beta”) equilibrium sets relative number densities of particles ( $n, p, e, \dots$ ) at different pressures 
$$n \leftrightarrow p + (e, \mu) \Rightarrow \mu_n = \mu_p + \mu_e$$
- Compressing or expanding a fluid element perturbs equilibrium 
$$\text{e.g., } \mu_n > \mu_p + \mu_e$$
- Non-equilibrium reactions tend to restore equilibrium 
$$n \rightarrow p + e + \bar{\nu}_e$$
- “Chemical” energy released as neutrinos & “heat”

# Possible forcing mechanisms

- Neutron star oscillations (bulk viscosity):  
SGR flare oscillations, r-modes – Not promising
- Accretion: effect overwhelmed by external  
& crustal heat release – No.
- $d\Omega/dt$ : “**Rotochemical heating**” – Yes
- $dG/dt$ : “**Gravitochemical heating**” - !!!???

# “Rotochemical heating”

NS spin-down (decreasing centrifugal support)

→ progressive density increase

→ chemical imbalance       $\eta \equiv \mu_n - \mu_p - \mu_{e,\mu} > 0$

→ non-equilibrium reactions       $n \rightarrow p + (e, \mu) + \bar{\nu}_{e,\mu}$

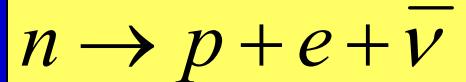
→ internal heating

→ possibly detectable thermal emission

Reisenegger 1995, 1997; Fernández & Reisenegger 2005;  
Reisenegger et al. 2006, submitted (all ApJ)

# Fast vs. slow processes

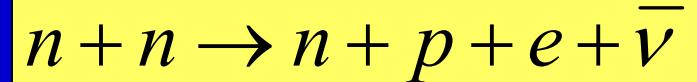
“Direct Urca”



Fast

But not allowed if proton density too low.

“Modified Urca”

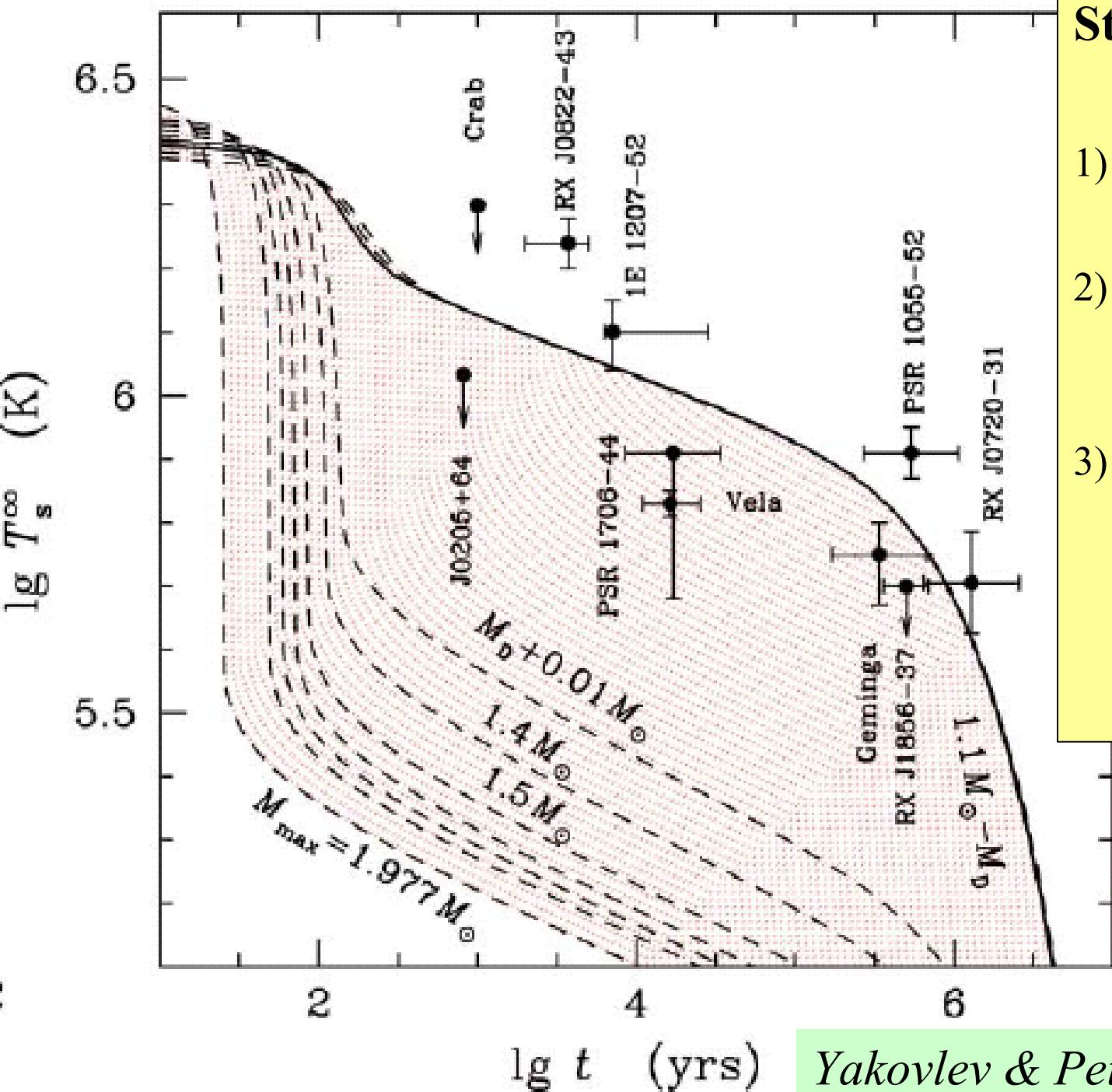


Dominant process if direct Urca not allowed, but:

Much slower

## Standard neutron star cooling:

- 1) No thermal emission after 10 Myr.
- 2) Finite diffusion time matters only during first few 100 yr.
- 3) Cooling of young neutron stars in rough agreement with slow cooling models (see D. Page's talk)



# Thermo-chemical evolution

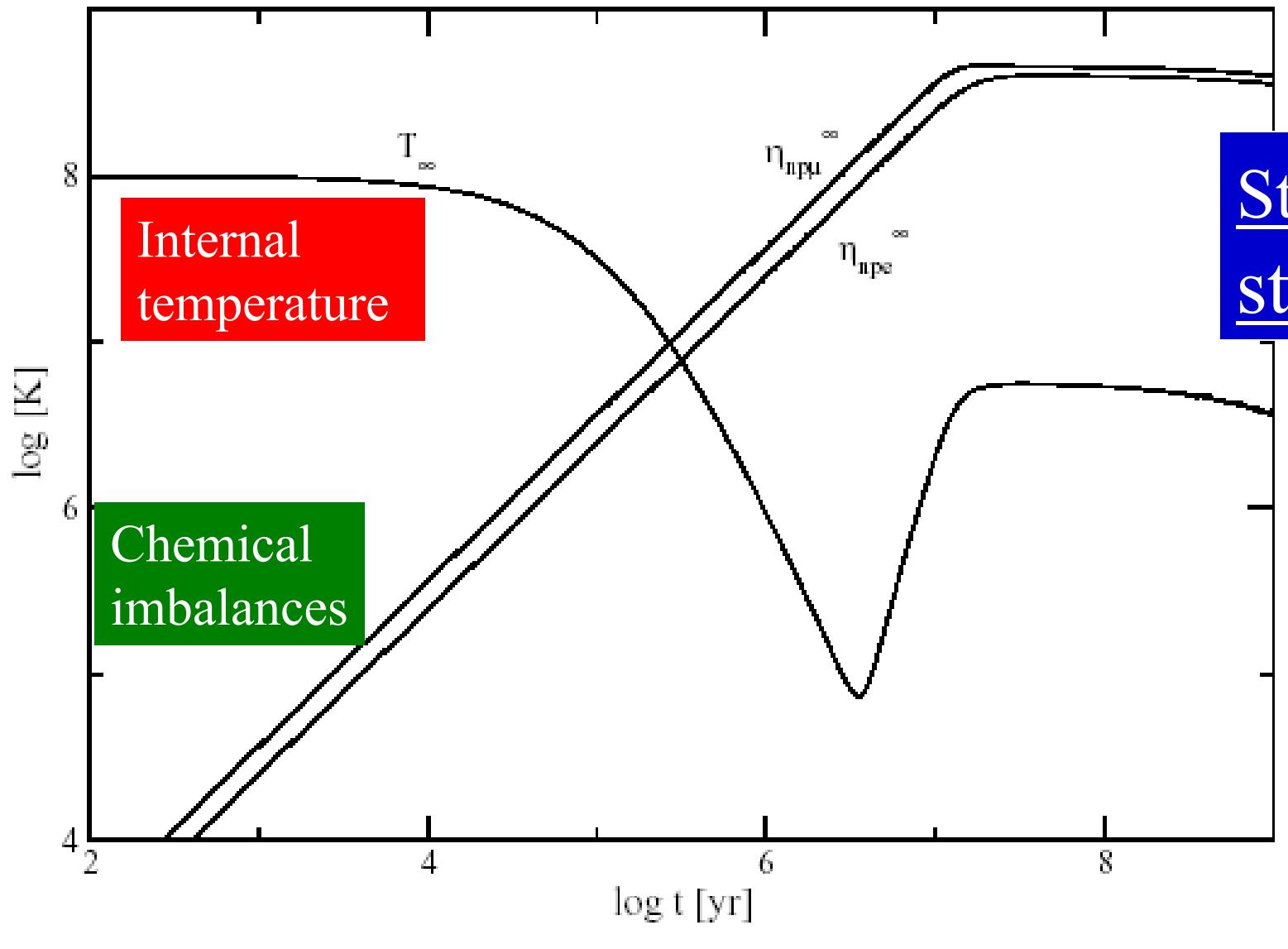
Variables:

- Chemical imbalances  $\eta_{e,\mu} \equiv \mu_n - \mu_p - \mu_{e,\mu}$
- Internal temperature  $T$

*Both are uniform in diffusive equilibrium.*

$$\frac{d\eta}{dt} = \left( \begin{array}{c} \text{increase through} \\ \text{compression} \end{array} \right) - \left( \begin{array}{c} \text{decrease through} \\ n \leftrightarrow p + e \end{array} \right)$$

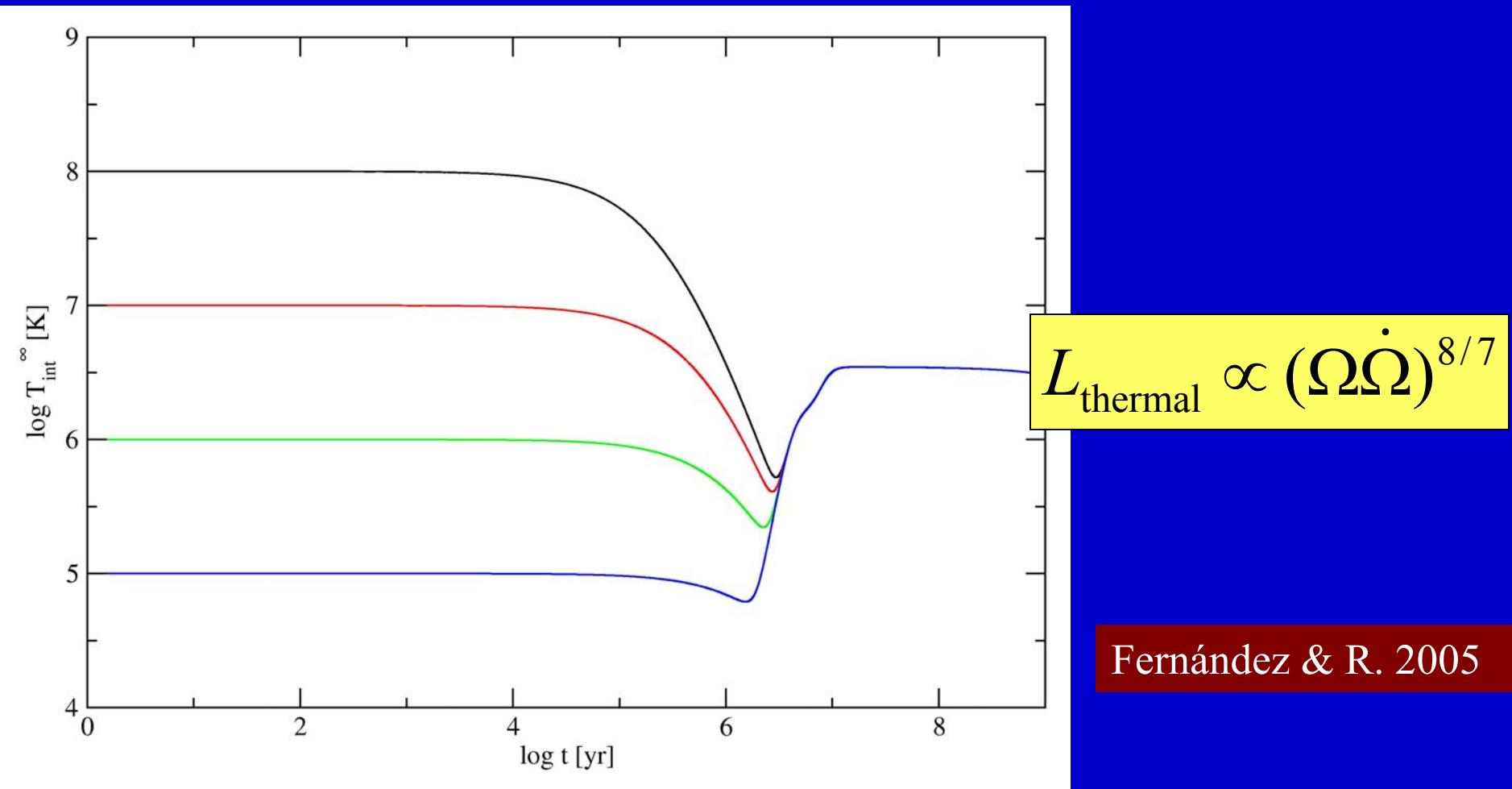
$$\frac{dT}{dt} = \left( \begin{array}{c} \text{increase through} \\ n \leftrightarrow p + e \end{array} \right) - \left( \begin{array}{c} \text{decrease through} \\ \text{radiation : } \gamma, \nu \end{array} \right)$$



MSP evolution

*Magnetic dipole spin-down ( $n=3$ )  
with  $P_0 = 1 \text{ ms}$ ;  $B = 10^8 \text{ G}$ ;  
modified Urca*

# Insensitivity to initial temperature



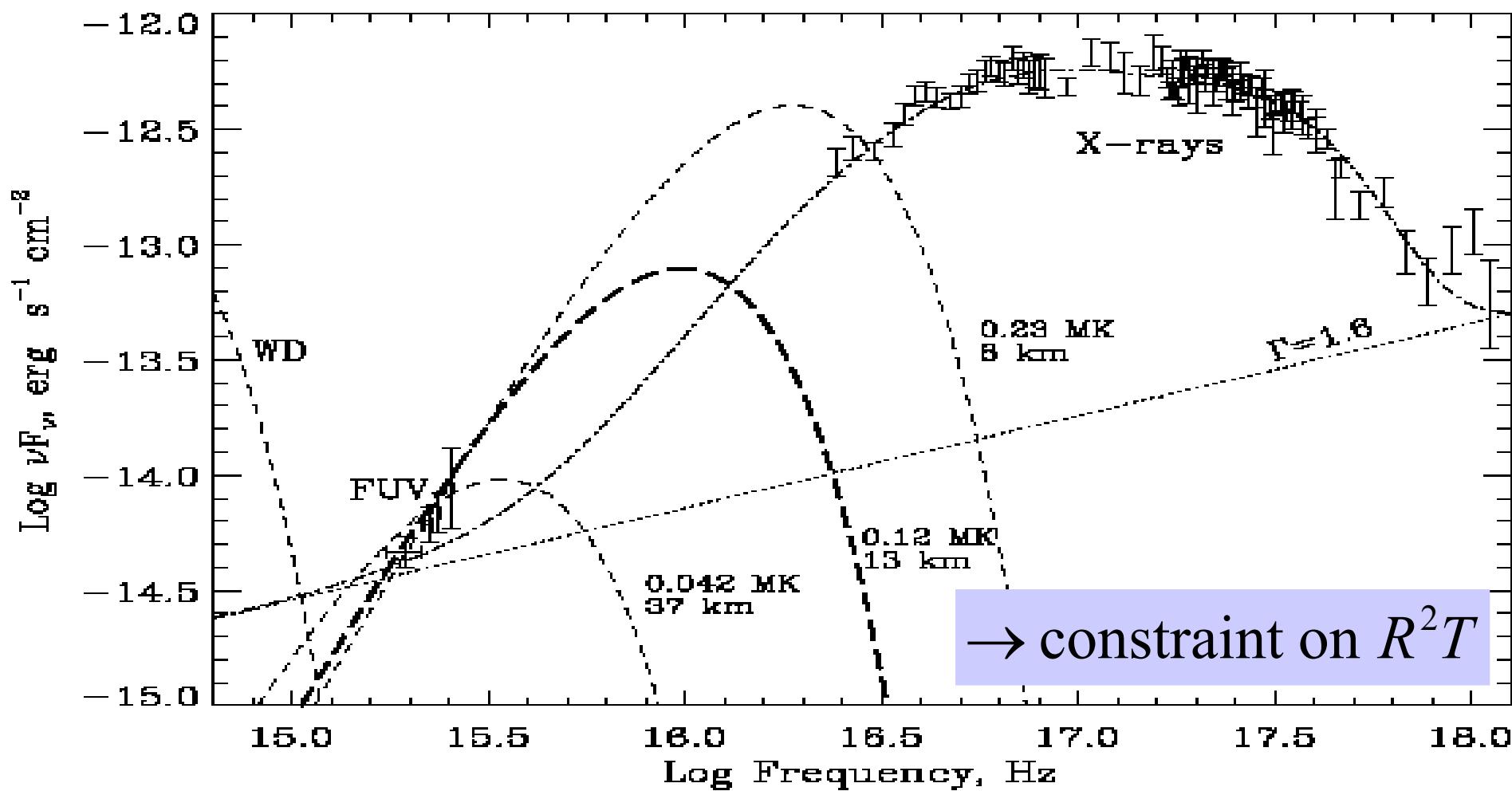
Fernández & R. 2005

For a given NS model, MSP temperatures can be predicted uniquely from the measured spin-down rate.

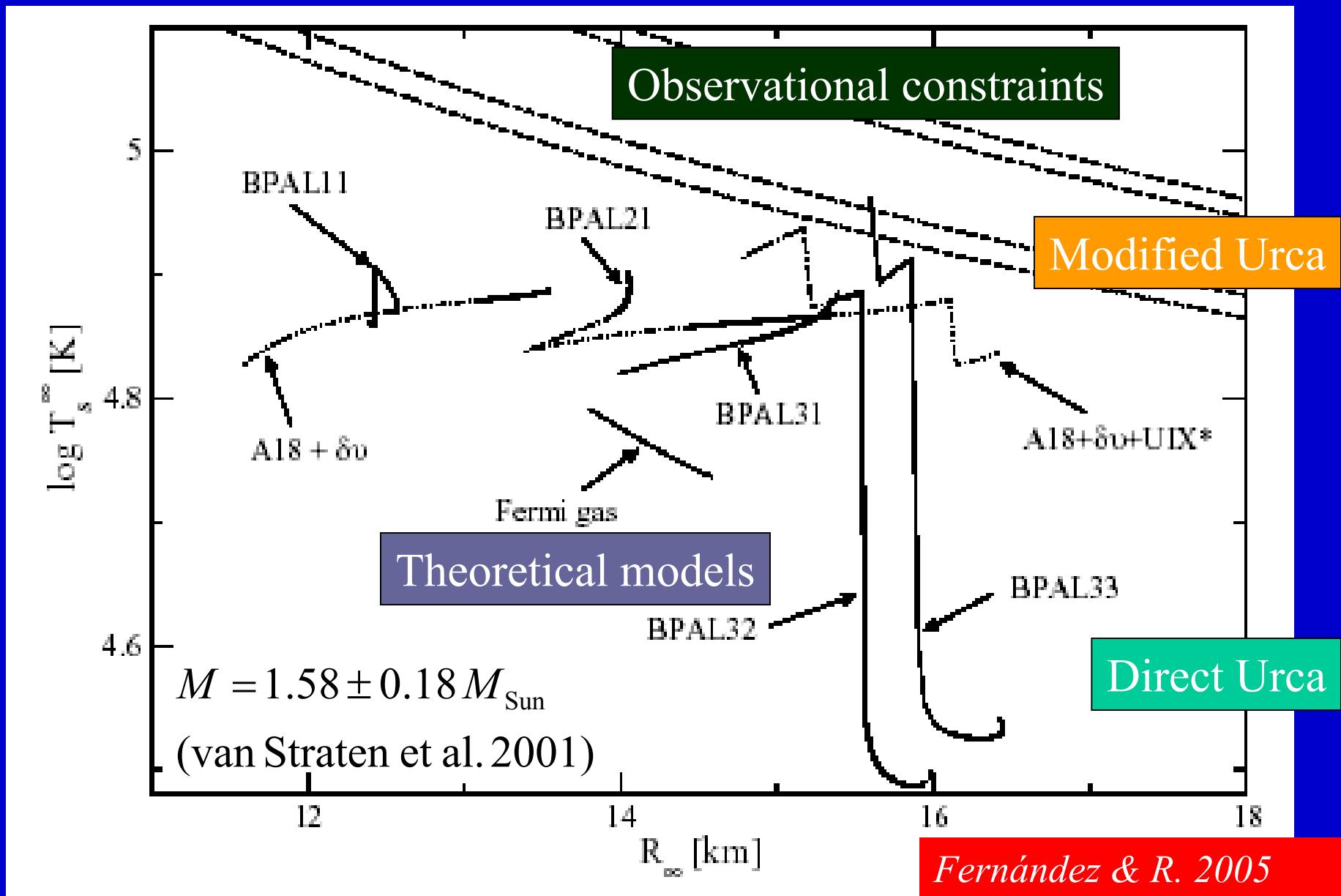
# The nearest MSP: PSR J0437-4715

HST-STIS far-UV observation (1150-1700 Å)

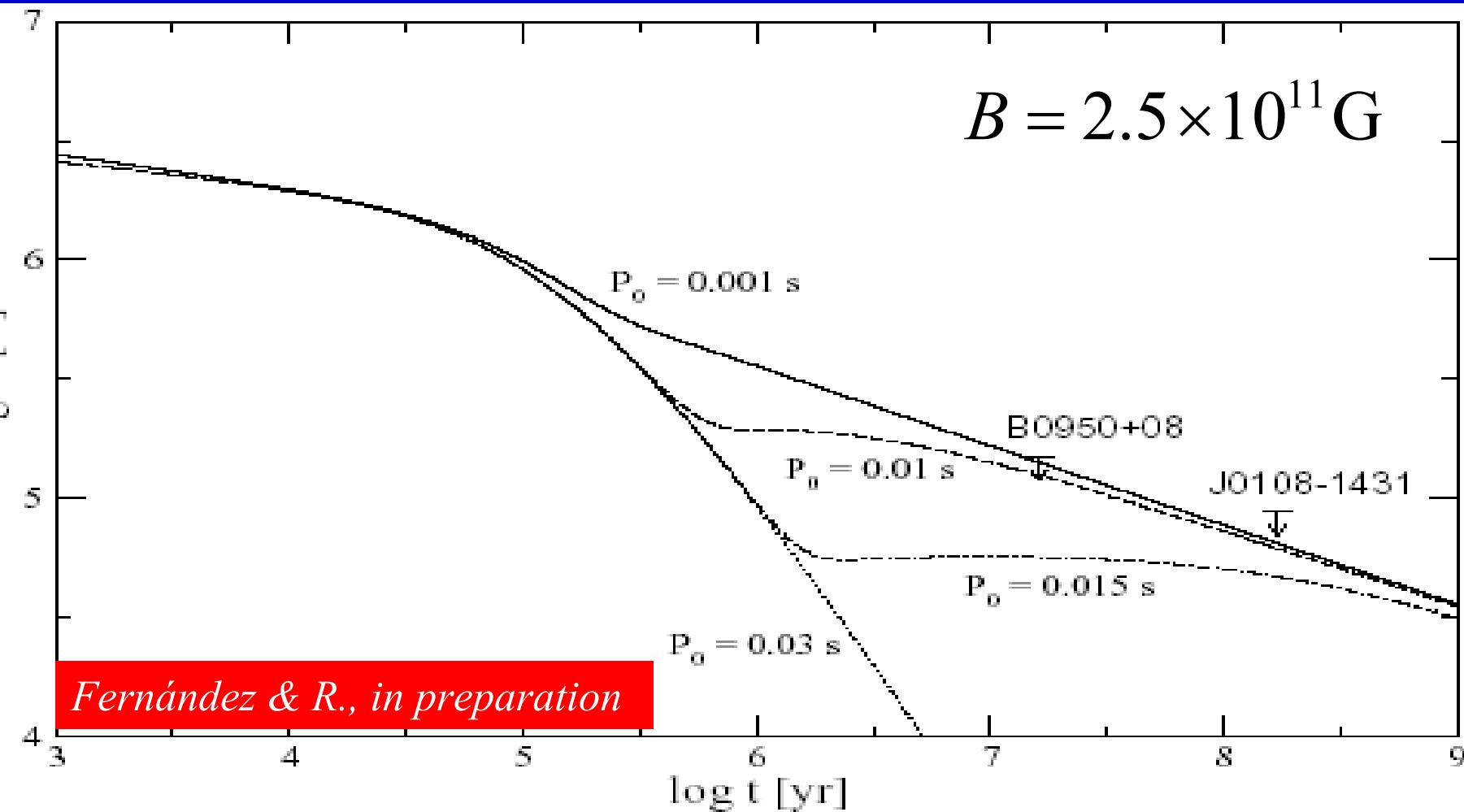
*Kargaltsev, Pavlov, & Romani 2004*



# PSR J0437-4715: Predictions vs. observation



# Old, classical pulsars: sensitivity to initial rotation rate



# $dG/dt$ ?

- Dirac (1937): constants of nature may depend on cosmological time.
  - Extensions to GR (Brans & Dicke 1961) supported by string theory
  - Present cosmology: excellent fits, dark mysteries, speculations: “Brane worlds”, curled-up extra dimensions, effective gravitational constant
  - Observational claims for variations of
    - $a_{\text{EM}} \equiv e^2/\hbar c$  (Webb et al. 2001; disputed)
    - $m_p/m_e$  (Reinhold et al. 2006)
- See how NSs constrain  $d/dt$  of  $\alpha_G \equiv Gm_n^2/\hbar c$

# Previous constraints on $dG/dt$

| <b>Method</b>   | <b>G' / G [yr<sup>-1</sup>] </b> | <b>Timespan [yr]</b> | <b>Reference</b>              |
|---|----------------------------------|----------------------|-------------------------------|
| Solar System planet and satellite orbits                          | 1E-12                            | 24                   | Williams et al (1996)         |
| Binary pulsar orbit   | 5E-12                            | 10                   | Kaspi et al (1994)            |
| Rotation of isolated PSRs (var. moment of inertia)                | 6E-11                            | 10                   | Goldman (1990)                |
| White dwarf oscillations  | 3E-10                            | 20                   | Benvenuto et al. (2004)       |
| Paleontology:<br>Earth's surface temp.<br>vs. prehistoric fauna   | 2E-11                            | 4E+09                | Eichendorf & Reinhardt (1977) |
| Binary pulsar masses<br>(Chandrasekhar mass at time of formation) | 2E-12                            | 2E+09                | Thorsett (1996)               |
| Helioseismology<br>(Solar evolution models)                       | 2E-12                            | 5E+09                | Guenther et al. (1998)        |
| Globular clusters<br>(isochrones vs. age of the Universe)         | 7E-12                            | 1E+10                | Degl'Innocenti et al. (1996)  |
| CMB temperature fluctuations (WMAP vs. specific models)           | 1E-13                            | 1E+10                | Nagata et al. (2004)          |
| Big Bang Nucleosynthesis<br>(abundances of D, He, Li)             | 2E-13                            | 1E+10                | Copi et al. (2004)            |

# *Gravitochemical heating*

$dG/dt$  (increasing/decreasing gravity)

⇒ density increase/decrease

⇒ chemical imbalance     $\eta \equiv \mu_n - \mu_p - \mu_{e,\mu} \neq 0$

⇒ non-equilibrium reactions     $n \leftrightarrow p + (e, \mu)$

⇒ internal heating

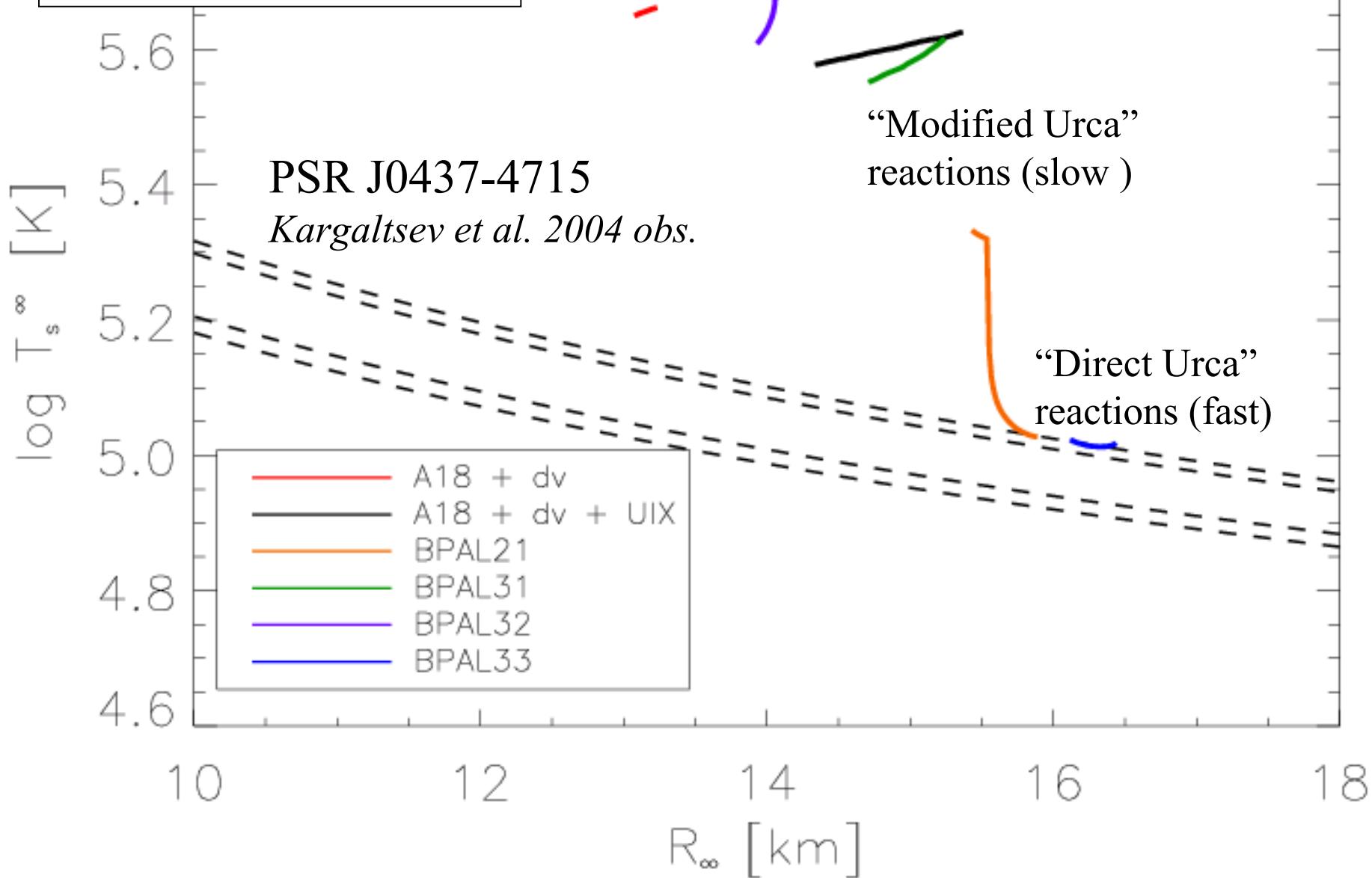
⇒ possibly detectable thermal emission

Paula Jofré, undergraduate thesis

Jofré, Reisenegger, & Fernández, paper in preparation

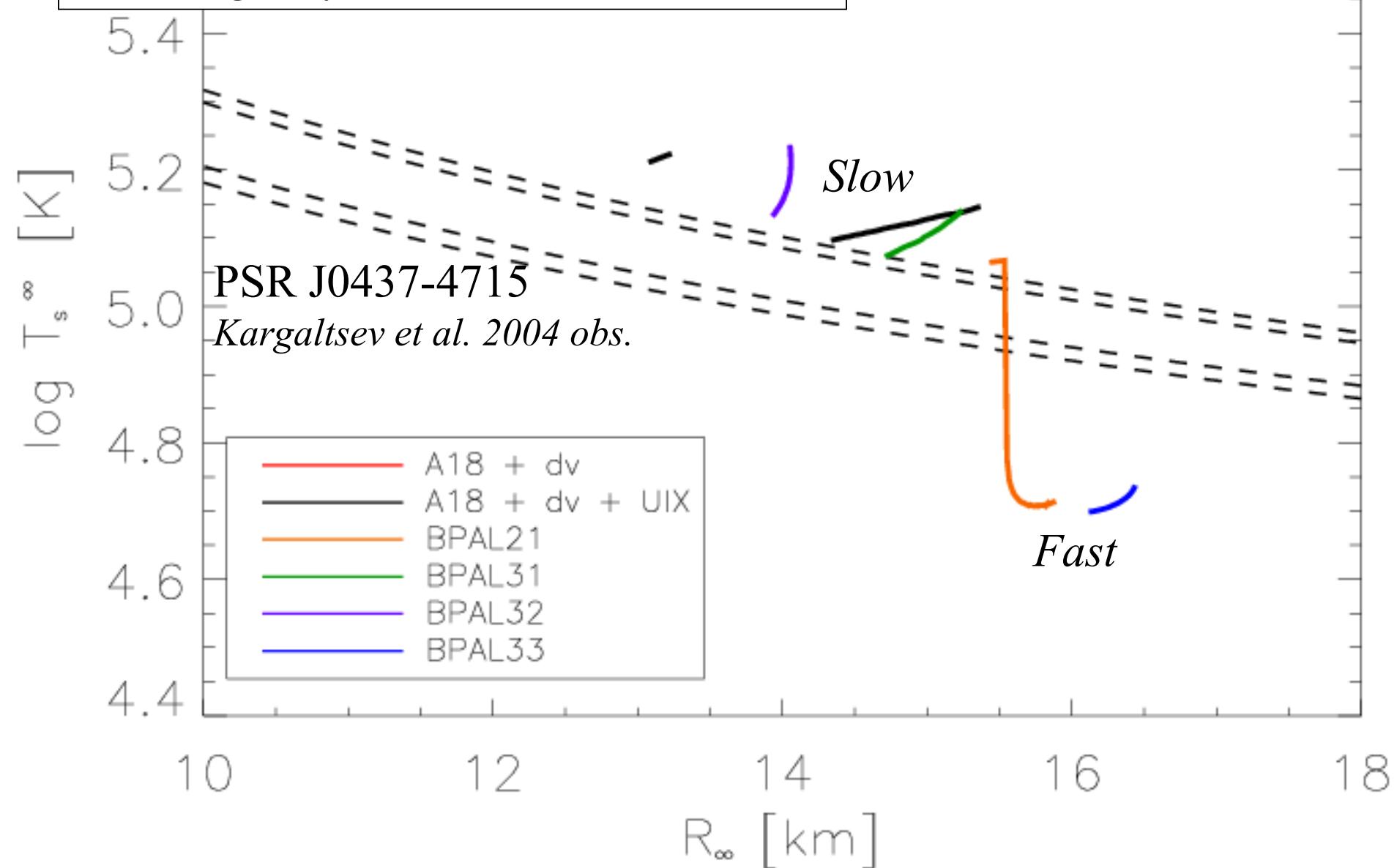
$$|\dot{G}| / G = 2 \times 10^{-10} \text{ yr}^{-1}$$

Most general constraint  
from PSR J0437-4715



Constraint from PSR J0437-4715  
assuming only modified Urca is allowed

$$|\dot{G}| / G = 4 \times 10^{-12} \text{ yr}^{-1}$$



# Constraint from PSR J0437-4715:

$$|\dot{G}|/G < 4 \cdot 10^{-12} \text{ yr}^{-1}$$

...if only modified Urca processes are allowed,  
and the star has reached its stationary state.

Required time:  $t_{eq} \approx 90 \text{ Myr}$

Compare to age estimates:  $t_{\text{spin-down}} = 4.9 \text{ Gyr}$

$t_{\text{WD cooling}} \approx 2.5 - 5.3 \text{ Gyr}$

(Hansen & Phinney 1998)

# Now:

| Method  | G' / G [yr <sup>-1</sup> ] | Time [yr]    | Reference                                 |
|---|----------------------------|--------------|---|
| Solar System planet and satellite orbits                          | 1E-12                      | 24           | Williams et al (1996)                     |
| Binary pulsar orbit   | 5E-12                      | 10           | Kaspi et al (1994)                        |
| Rotation of isolated PSRs<br>(var. moment of inertia)             | 6E-11                      | 10           | Goldman (1990)                            |
| White dwarf oscillations  | 3E-10                      | 20           | Benvenuto et al. (2004)                   |
| <b>Gravitochemical heating of NSs (PSR J0437-4715)</b>            | <b>2E-10</b>               | <b>1E+05</b> | <b>Jofré et al.<br/>(to be published)</b> |
| <b>MOST GENERAL</b>   |                            |              |   |
| <b>Gravitochemical heating of NSs (PSR J0437-4715)</b>            | <b>4E-12</b>               | <b>9E+07</b> | <b>Jofré et al.<br/>(to be published)</b> |
| <b>ONLY MODIFIED URCA</b>   |                            |              |   |
| Paleontology:<br>Earth's surface temp.<br>vs. prehistoric fauna   | 2E-11                      | 4E+09        | Eichendorf & Reinhardt (1977)             |
| Binary pulsar masses<br>(Chandrasekhar mass at time of formation) | 2E-12                      | 2E+09        | Thorsett (1996)                           |
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# Main uncertainties

- Atmospheric model:
  - Deviations from blackbody
    - H atmosphere underpredicts Rayleigh-Jeans tail
- Neutrino emission mechanism/rate:
  - Slow (mod. Urca) vs. fast (direct Urca, others)
  - Cooper pairing (superfluidity): R. 1997; Villain & Haensel 2005; Flores & R., in prep.

Not important (because stationary state):

- Heat capacity: steady state
- Heat transport through crust

# Conclusions

- *Rotochemical heating* must occur in all neutron stars with decreasing rotation rates
- *Gravitochemical heating* happens if  $dG/dt \neq 0$
- Both lead to a stationary state of nearly constant temperature that can be probed with old enough pulsars (e.g., MSPs)
- Observed UV emission of PSR J0437-4715 may be due to rotochemical heating
- The same emission can be used to constrain  $|dG/dt|$ :
  - competitive with best existing constraints if fast cooling processes could be ruled out
- Sensitive UV observations of other nearby, old neutron stars of different rotation rates are useful to constrain both mechanisms
- Superfluid effects being calculated