

School of Physics and Astronomy

FACULTY OF MATHEMATICS AND PHYSICAL SCIENCES



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# Particle Acceleration (and colliding stellar winds)

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An Inter-disciplinary Workshop/Forum on  
Magnetospheric Activities in Moons, Planets, Stars  
and Black Holes

MSSL, 19<sup>th</sup> Sept 2007



- I. Basic Review of Particle Acceleration
  - concentrating on non-relativistic DSA
  
- II. Particle Acceleration at Colliding Stellar Winds

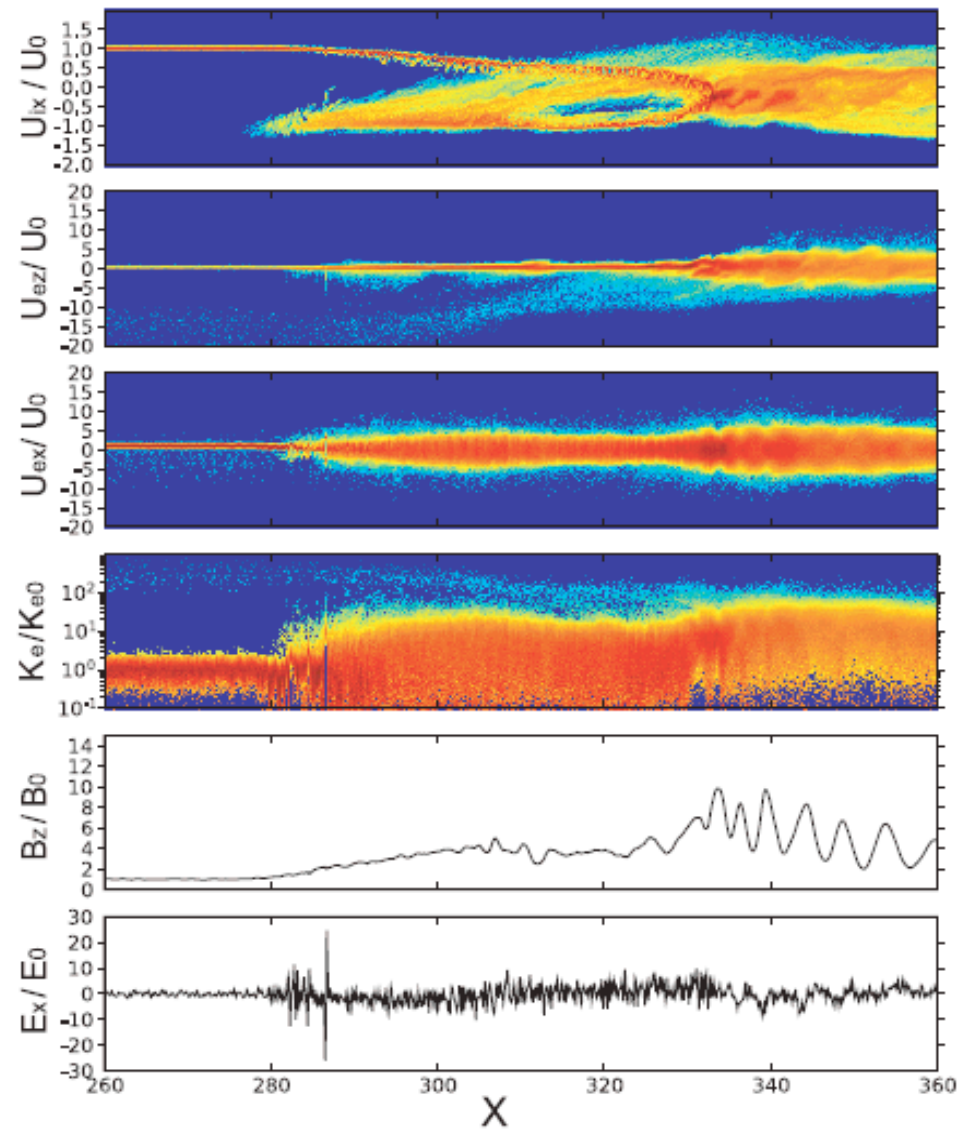
# Techniques



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- Semi-analytical
- Monte-Carlo
- Particle-in-cell (PIC)

Complemented by lab experiments



Amano & Hoshino (2007)



# Reconnection and stochastic acceleration

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## Reconnection

- Usually thought to produce steep spectra
- Complex and intricate magnetic environment
- Particles can be accelerated:
  - Directly (through strong electric fields)
  - Stochastically (2<sup>nd</sup> order Fermi process due to high turbulence)
  - At MHD shock waves (i.e. through DSA)

## 2<sup>nd</sup> order Fermi

- Can give a hard spectrum at low energies (falls off at high E)
- Spectral index depends on additional unknown factors such as the residence time of the particles in the accn. region.
- Mean change in mtm:

$$\frac{\Delta p}{p} \approx \frac{V^2}{v^2}$$



# Diffusive Shock Acceleration (DSA)

Scattering by (self-excited) turbulence around shock front

Converging plasma

Isotropy implies

$$\frac{\langle \Delta p \rangle}{p} = \frac{4 \Delta u}{3v}$$

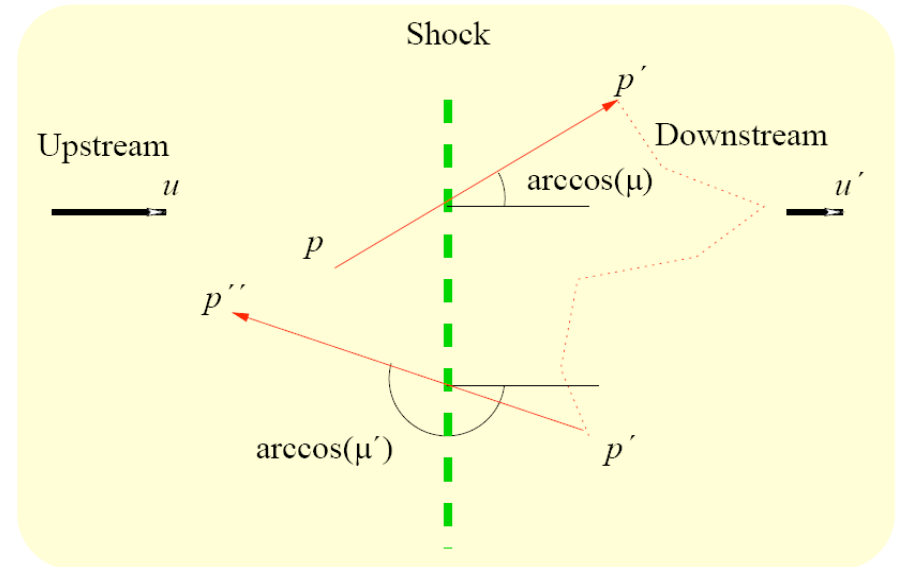
Escape probability downstream =  $4u_2/v$

Test particle predictions of DSA:  $N(\Delta) \propto \Delta^{-p}$

where 
$$p = \frac{r_{tot} + 2}{r_{tot} - 1}$$

and  $r_{tot}$  is the overall compression ratio

For strong, unmodified shocks,  $r_{tot} = 4$ , and  $p=2$





# Nonrelativistic (DSA) vs. Relativistic

pitch-angle diffusion  $\mu$  near-isotropy  $\mu$  spatial diffusion

solution of PDE in  $x, p$  required

small escape probability, small  $\langle \Delta p \rangle / p$  per cycle

spectral index of power-law of particle distribution is independent of scattering law

pitch-angle diffusion, particles in narrow, forward directed cone

solution of PDE in  $\mu, x, p$  required

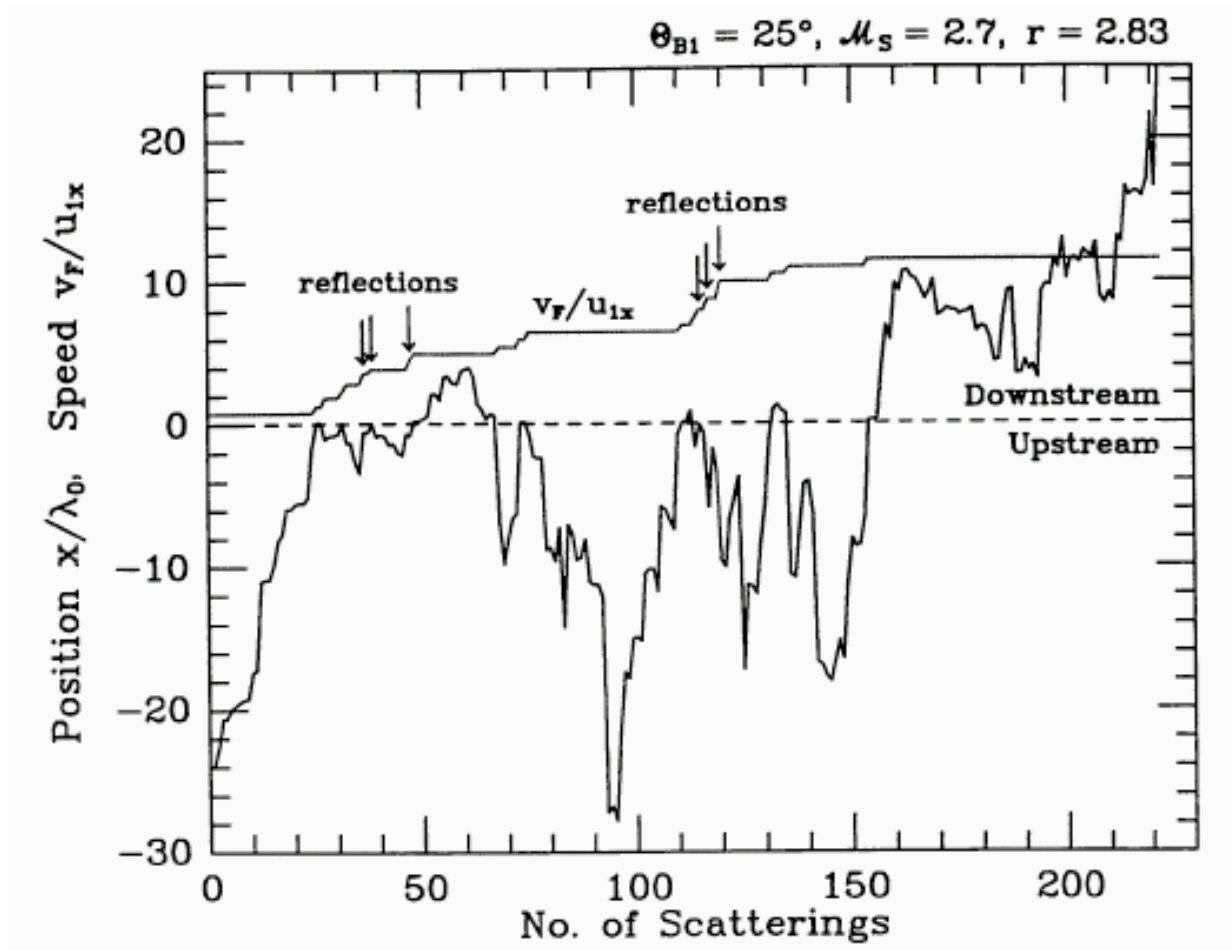
escape probability  $\sim 0.5$ ,  $\langle \Delta p \rangle / p \sim \mu^2$  for first cycle, then  $\sim 2$

Spectral index asymptotes as  $\mu \rightarrow \infty$ , weakly dependent on scattering law



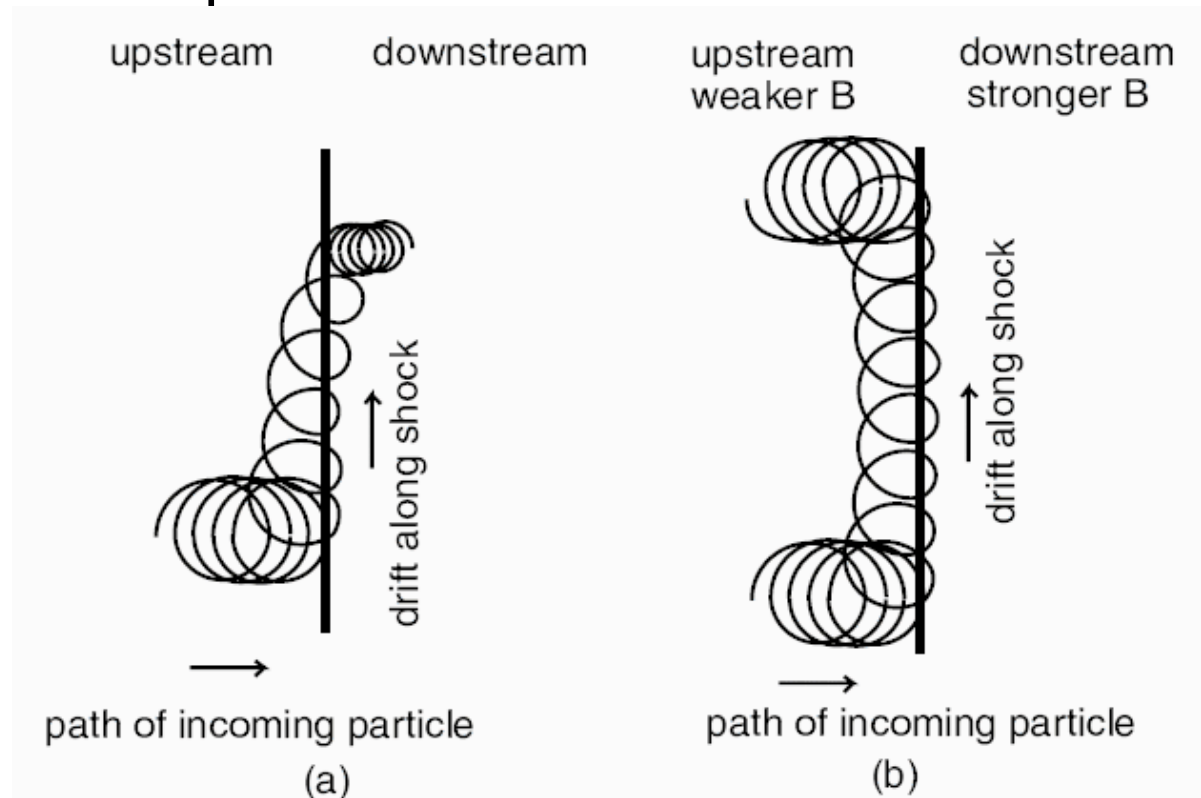
# Shock crossings/reflections

Monte Carlo model – particles pitch-angle scatter elastically and isotropically



Any “thermal” particle which manages to diffuse back upstream across the shock gains energy and becomes superthermal. The viscous subshock is assumed to be transparent to all particles, even thermal ones, and any downstream particle with  $v \geq u_2$  has a chance to be injected.

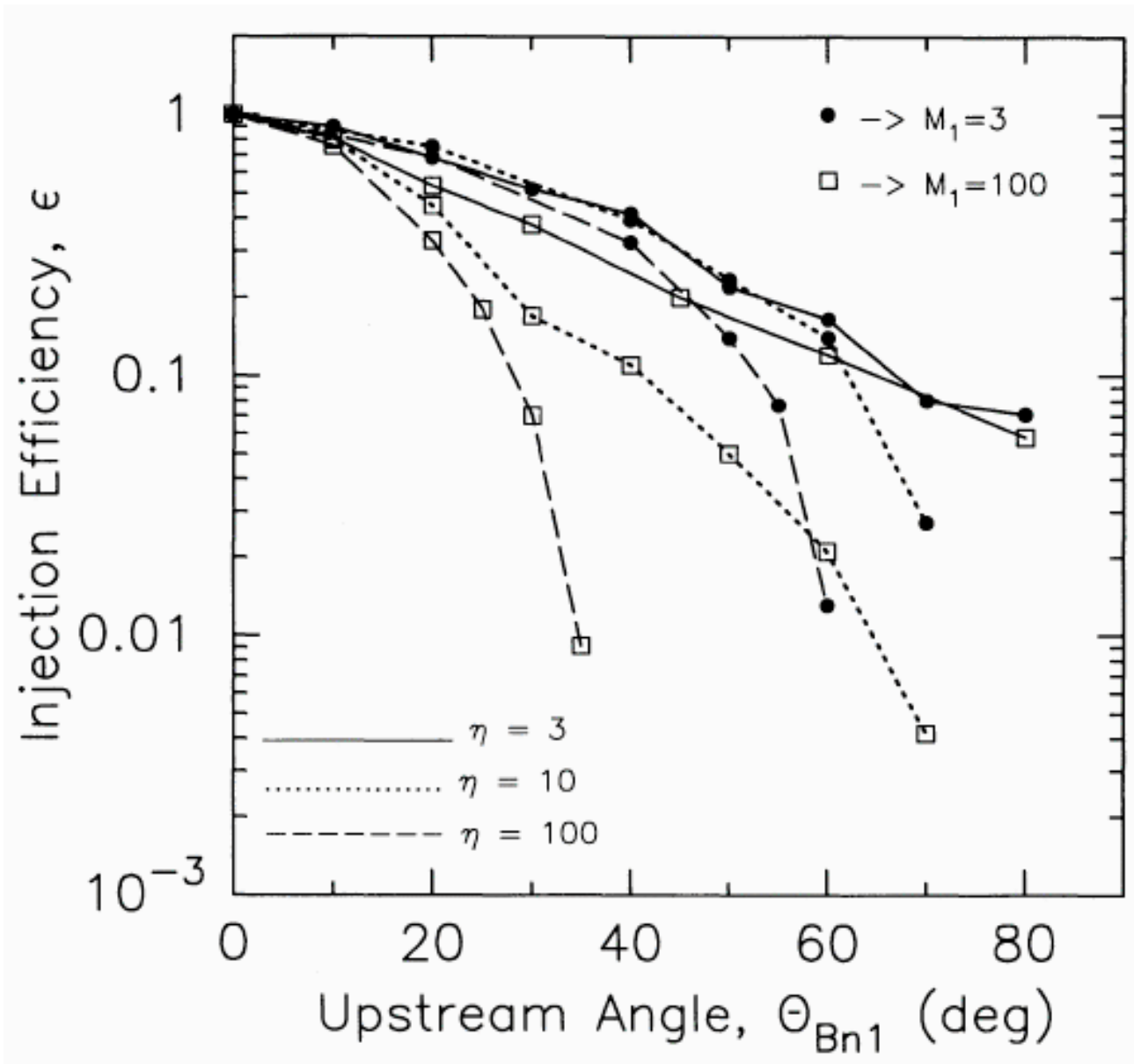
## Occurs for oblique shocks



- When B-field is compressed across shock, downstream gyroradius is smaller than upstream gyroradius – causes particle to “drift” along the shock front
- If particle moves at an angle to the B-field it sees an electric field which may either accelerate/decelerate the particle depending on the direction of motion
- Accn is more rapid in oblique shocks due to shock drift along the shock surface and slower diffusion in the shock normal direction.



# Injection efficiency





# DSA - spectral index

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Harder (flatter) CR spectra can be obtained by

- 1) Shock modification (at high energies)
- 2) Radiative losses (compression ratio increases)
- 3) Non-standard DSA (e.g. anisotropic scattering)
- 4) More complex flow (e.g. multiple shocks)
- 5) Various turbulence mechanisms
- 6) If plasma  $\beta$  is low, scattering center compression ratio  $\neq$  gas compression ratio

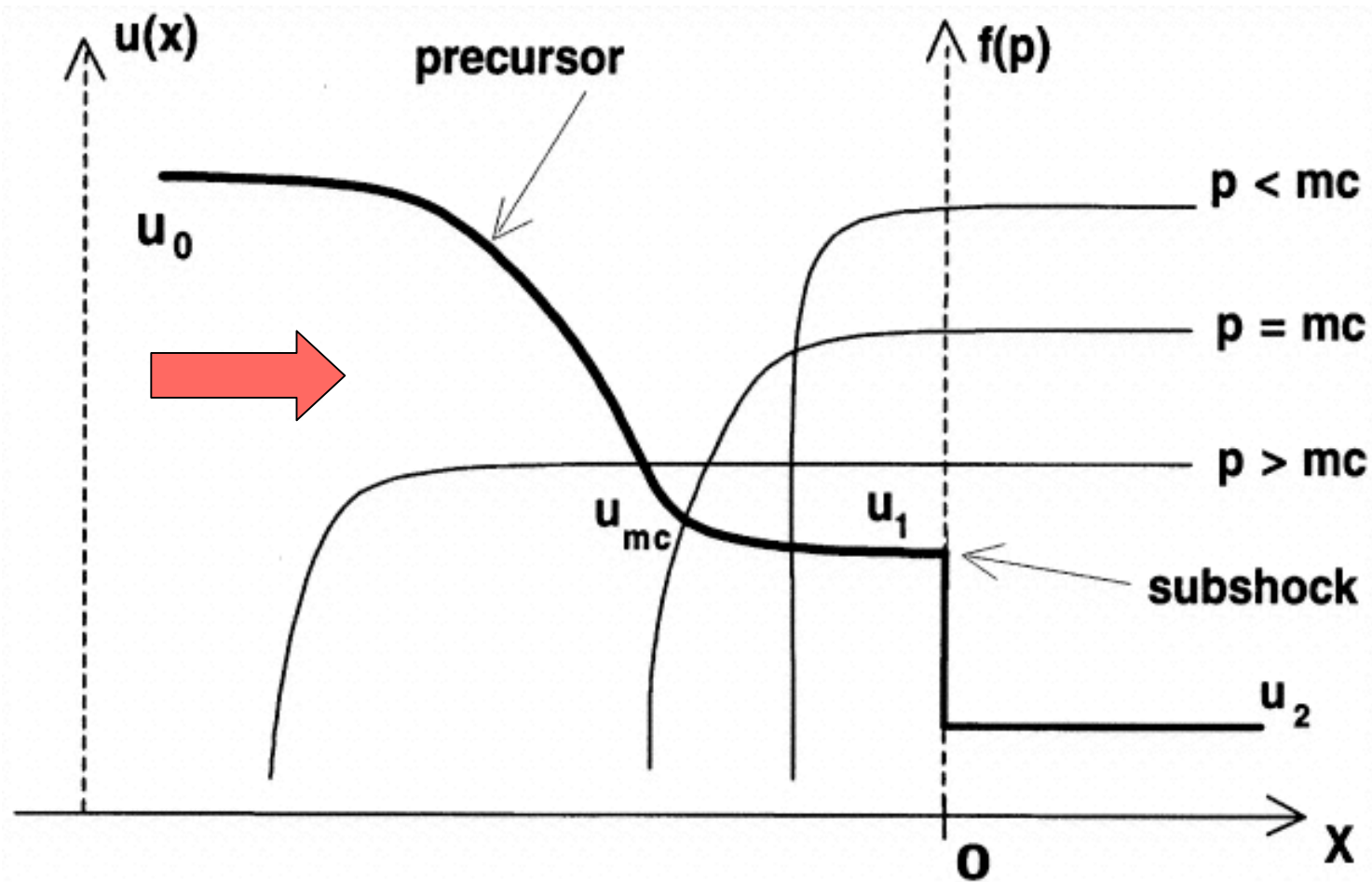
Softer (steeper) spectra can be obtained by

- 1) Shock modification (at low energies)
- 2) Shock curvature (high energy particles escape more readily)
- 3) Non-standard DSA (e.g. subdiffusive regimes)

# Shock modification



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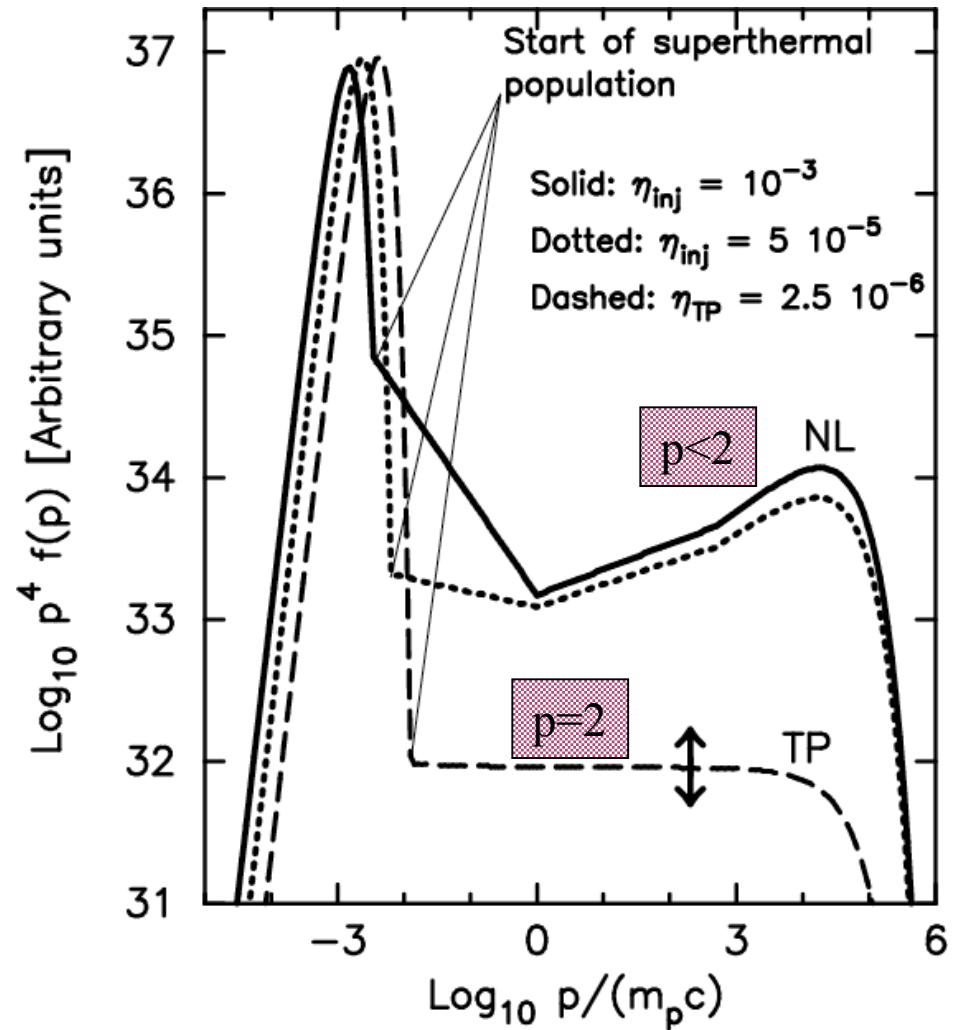
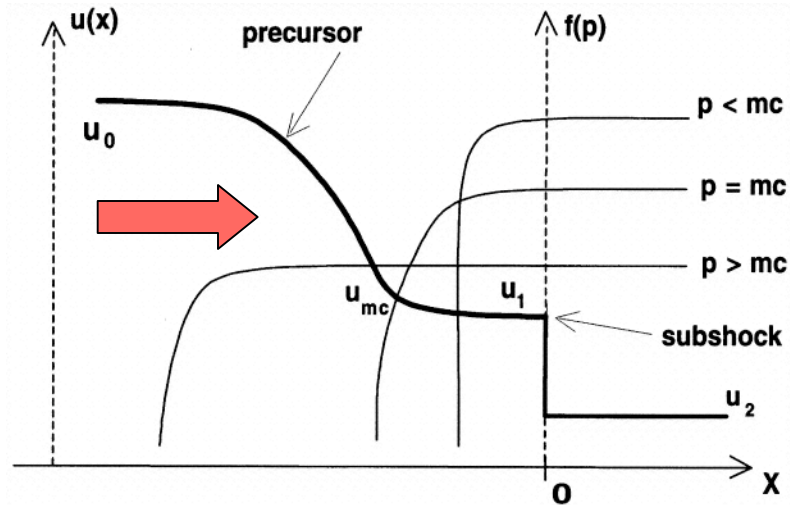


Berezhko & Ellison (1999)

# Concave NT particle spectra



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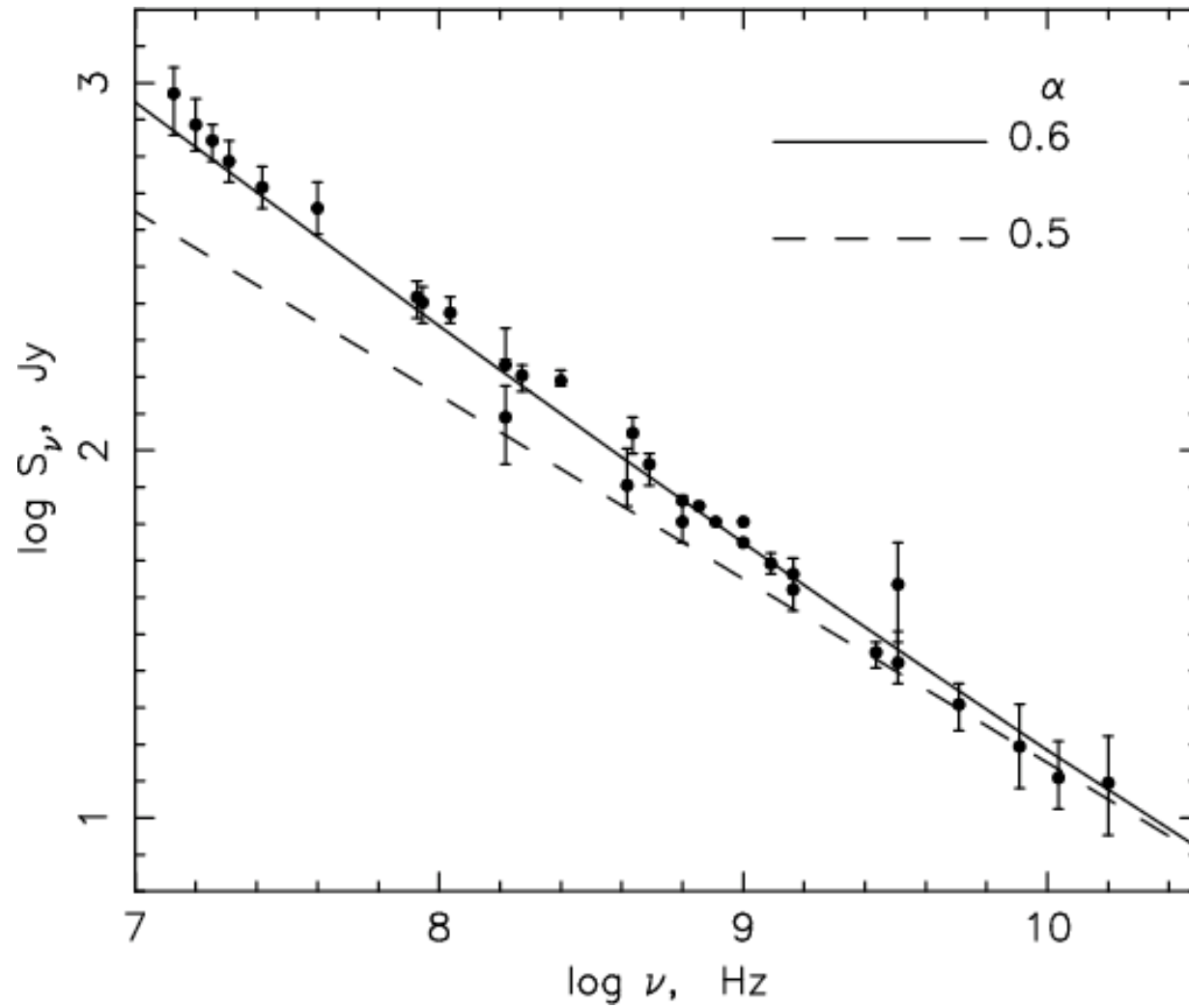


Ellison et al. (2004)

# Shock modification evidence



## Tycho SNR

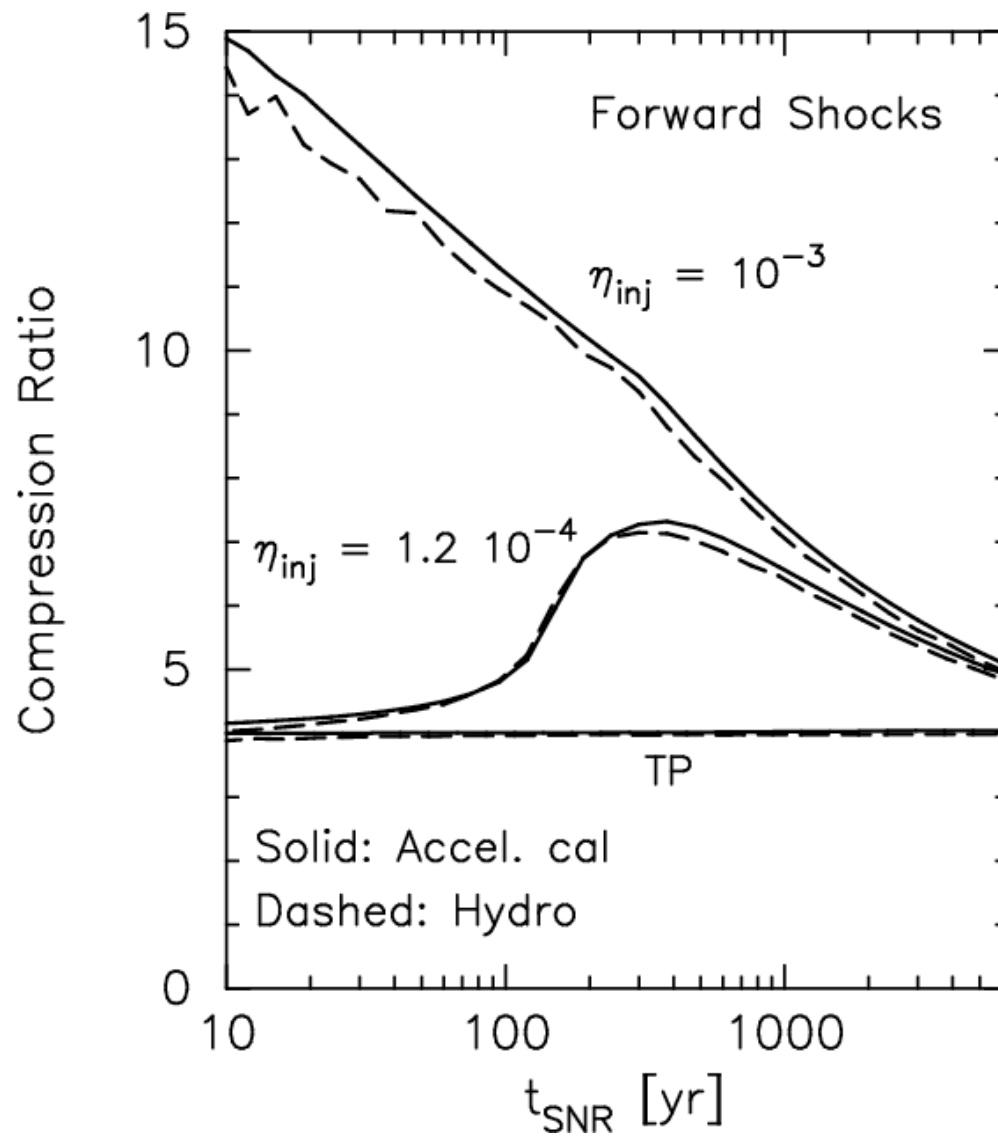


Volk et al (2002)

# Shock Modification



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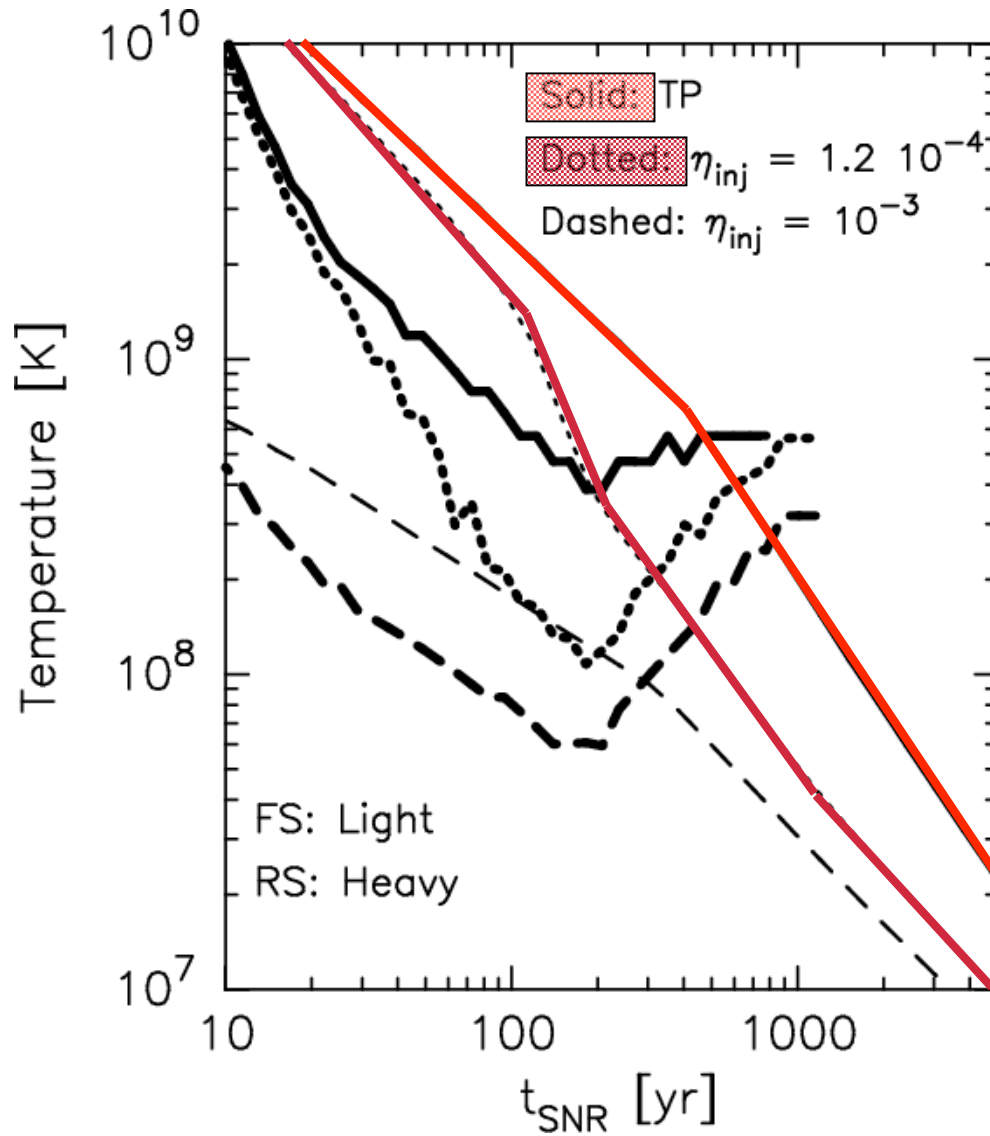
Higher overall  
compression  
ratios

Ellison et al. (2004)

# Shock modification



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Lower post-shock  
ion temperatures

Ellison et al. (2004)

# B-field amplification – evidence (I)

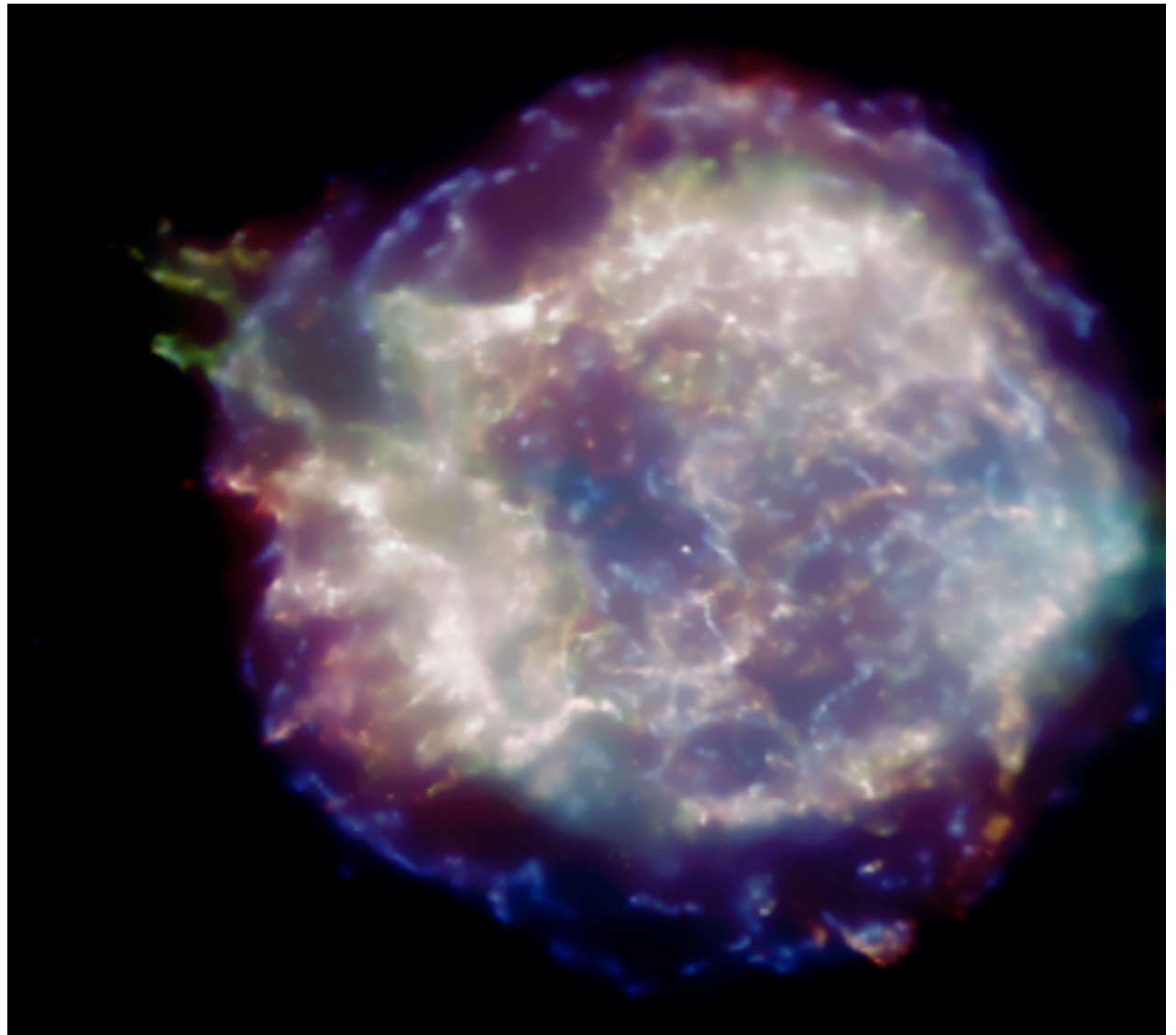


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Several young objects well studied in X-ray synchrotron radiation

Thin filaments suggest rapid cooling of electrons:  
 $B_{\text{shock}} \gg B_{\text{ISM}}$

Also brightness contrast of sync X-rays upstream and downstream of the shock is  $\sim 50$ , whereas it is expected to be  $< 16$  with simple MHD compression at the shock.

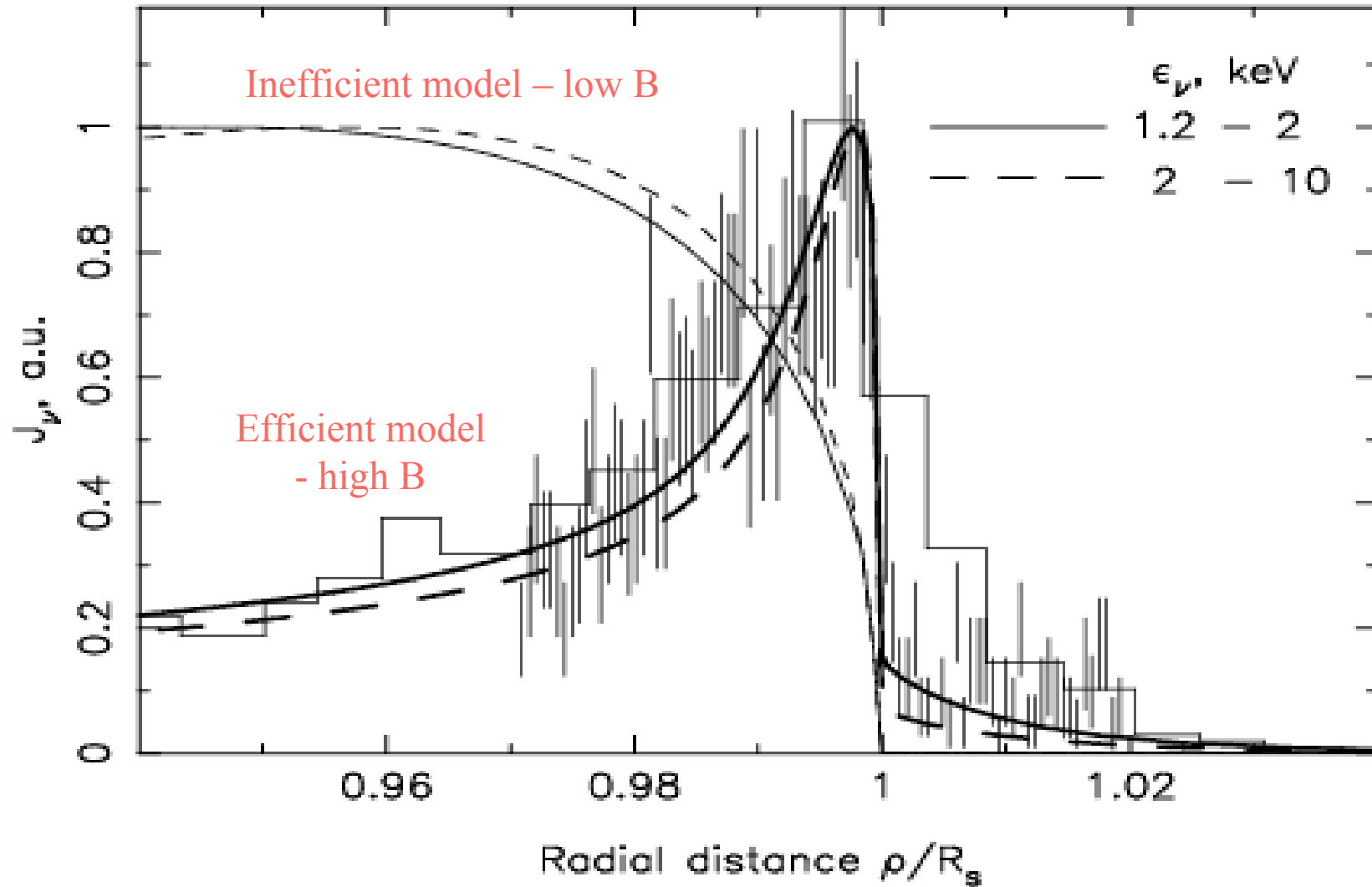




# B-field amplification – evidence (II)



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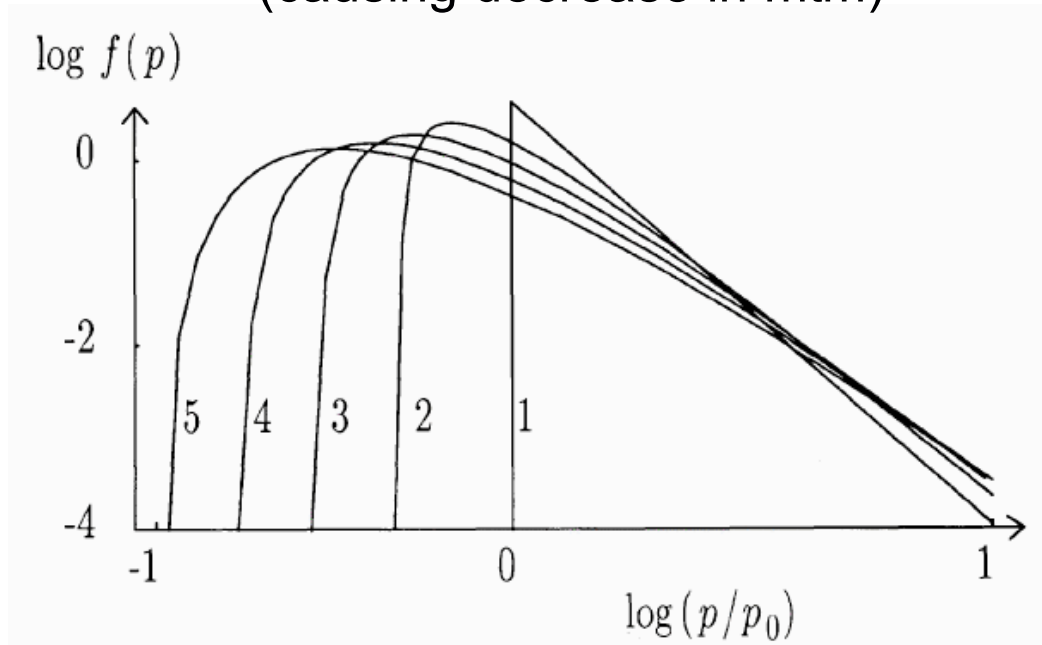


Berezhko et al. (2003)

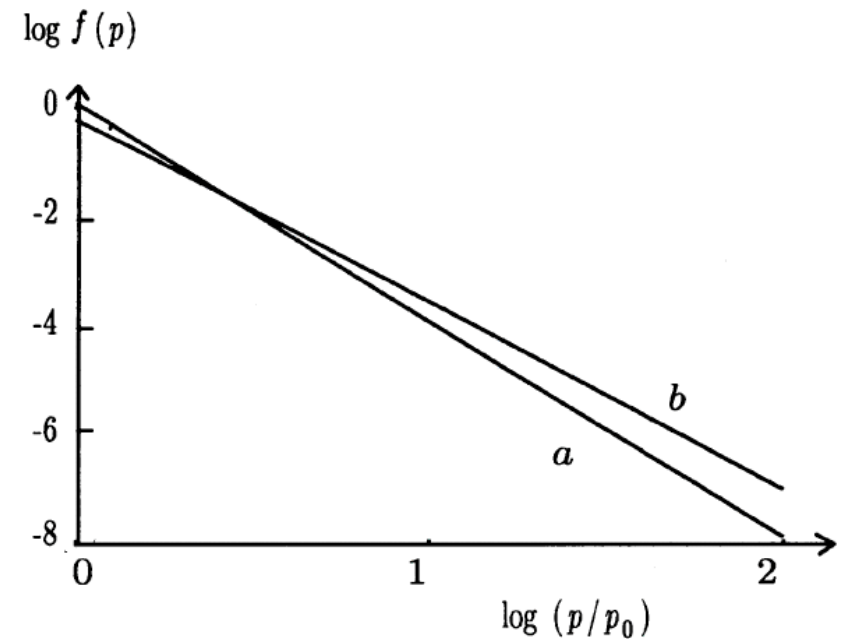


# Re-acceleration

- Acceleration at a sequence of shocks can flatten the spectral index
- $p_{-1}$  after an arbitrary number of shocks (independent of shock strength)
- Adiabatic decompression between each shock is a central assumption (causing decrease in  $m_{\text{th}}$ )



Spectrum of particles injected at 1<sup>st</sup> shock, after subsequent shocks



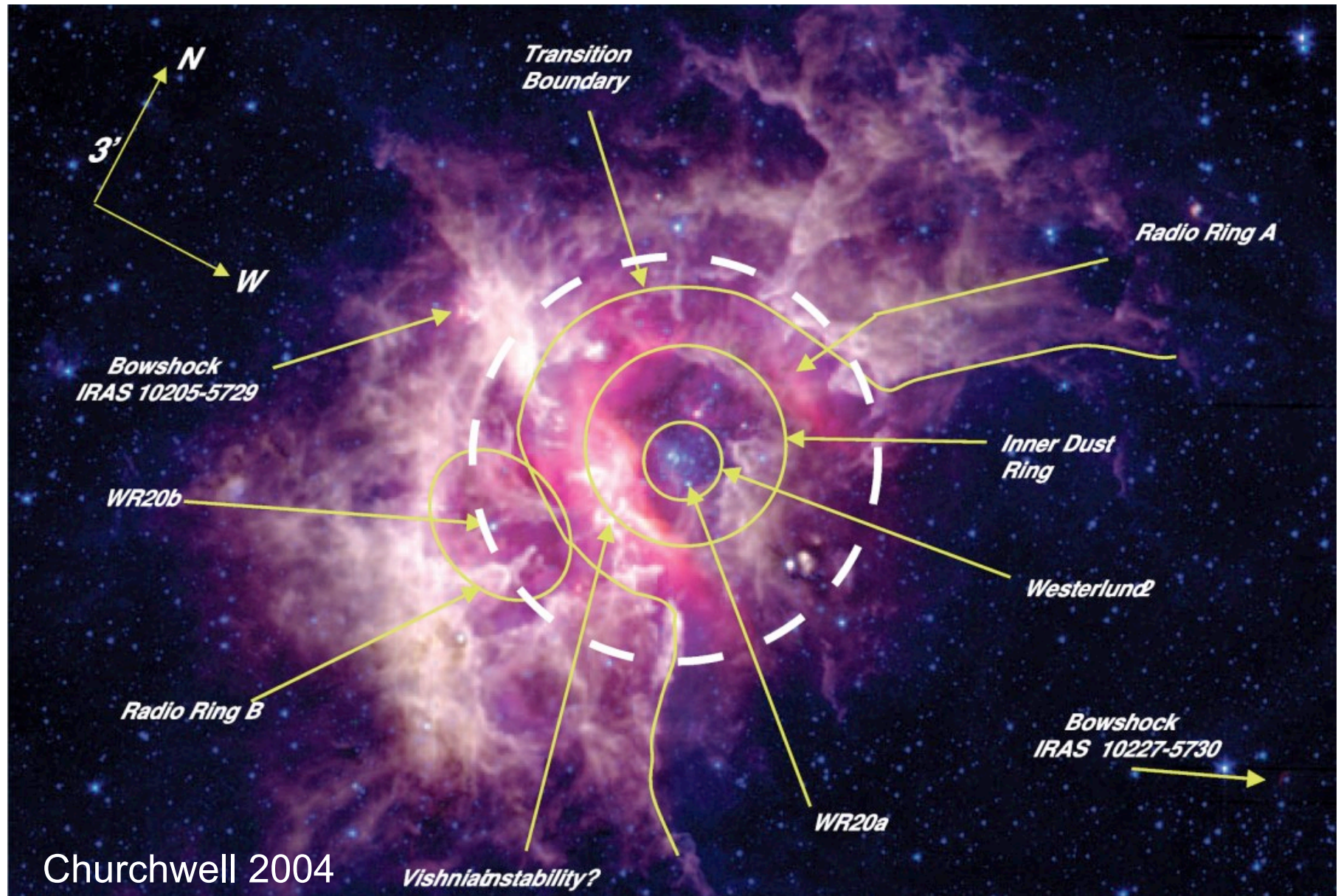
Total spectrum of all particles

Melrose & Pope (1993)

# Westerlund 2



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Churchwell 2004

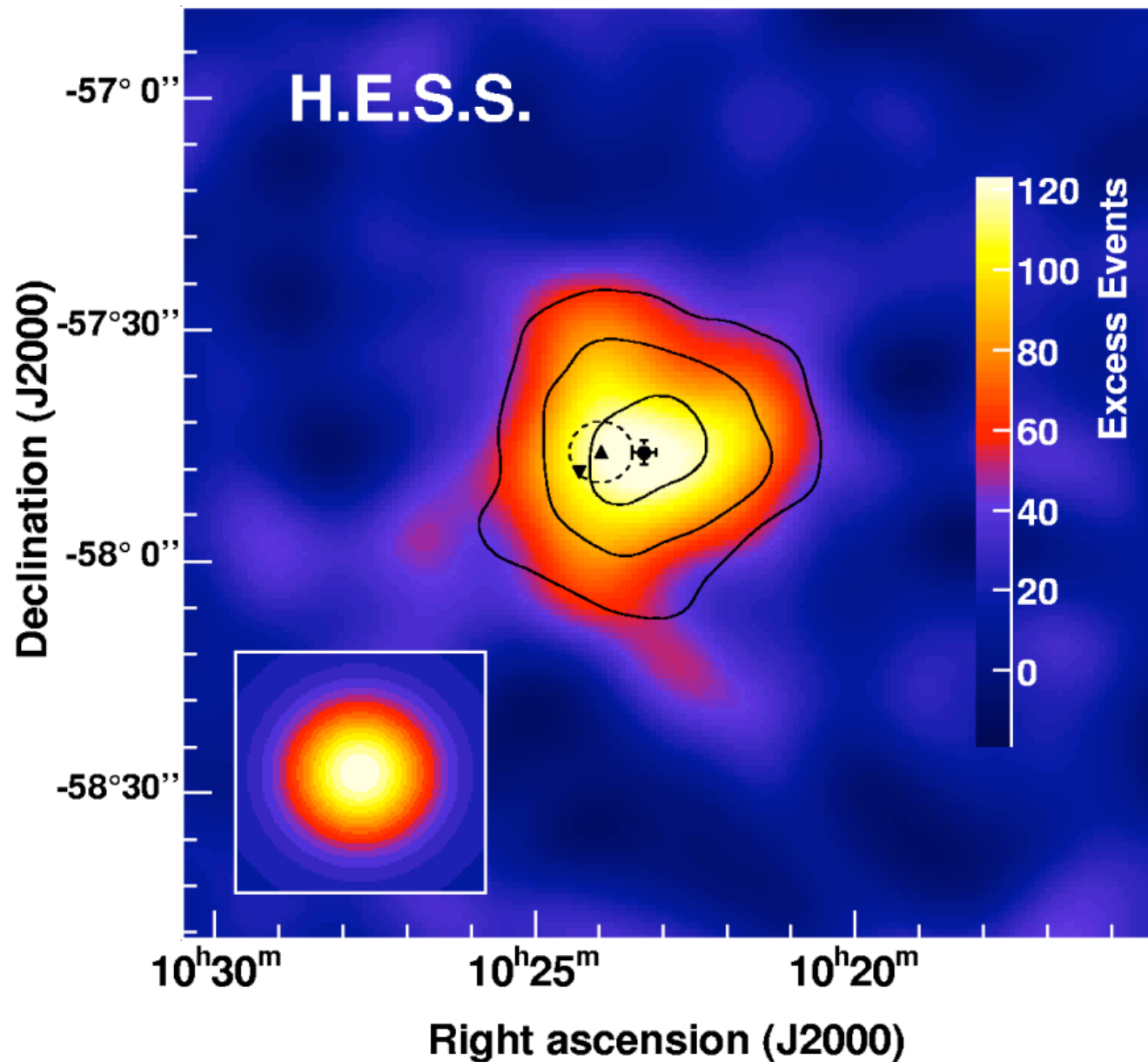
# HESS J1023-575



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Extended  
gamma-ray  
emission  
covering (but  
offset from)  
Westerlund 2

Due to  
collective  
effects of  
stellar winds  
in the cluster?





# Outstanding issues

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## (Electron) Injection

DSA is only applicable to particles which gyrate on a lengthscale larger than the lengthscale of the subshock ( $\sim$  a thermal particle gyroradius) – ie those which are already suprathermal

## B-field amplification

There should be some form of conversion of CR particle energy into magnetic turbulence in the precursor. But what form is the heating (adiabatic or Alfvén heating?)

If this process is efficient, the rate of work done on the upstream Alfvén turbulence of energy density  $U_A$  naturally scales with the CR pressure gradient:

$$\frac{dU_A}{dt} = v_A |\nabla P_{CR}|$$

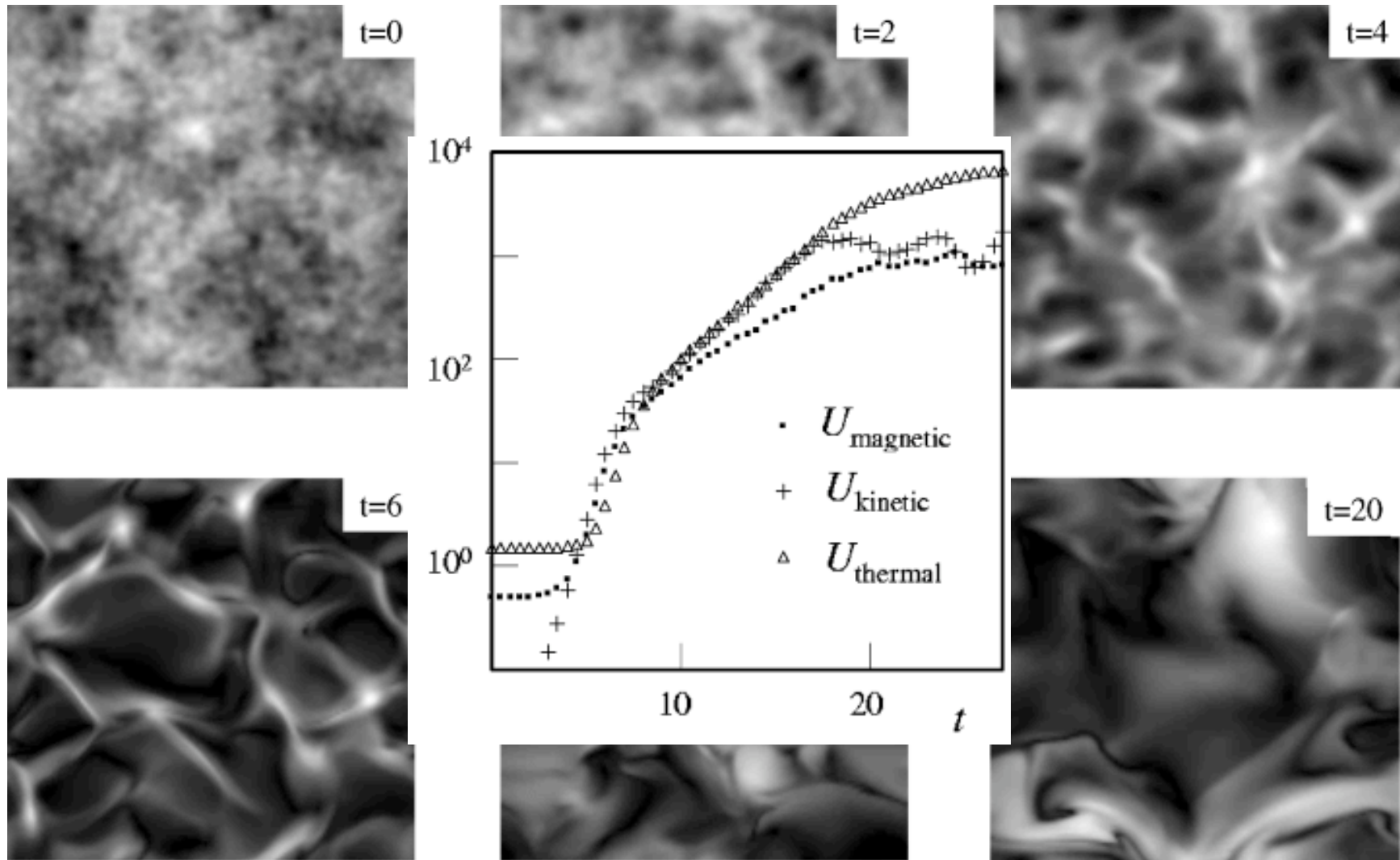
The associated field amplification should then scale as  $(\nabla B / B)^2 \sim M_A P_{CR} / \nabla u_2^2$

This becomes very effective for strong shocks with large CR pressures

# B-field Amplification



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Bell (2004)

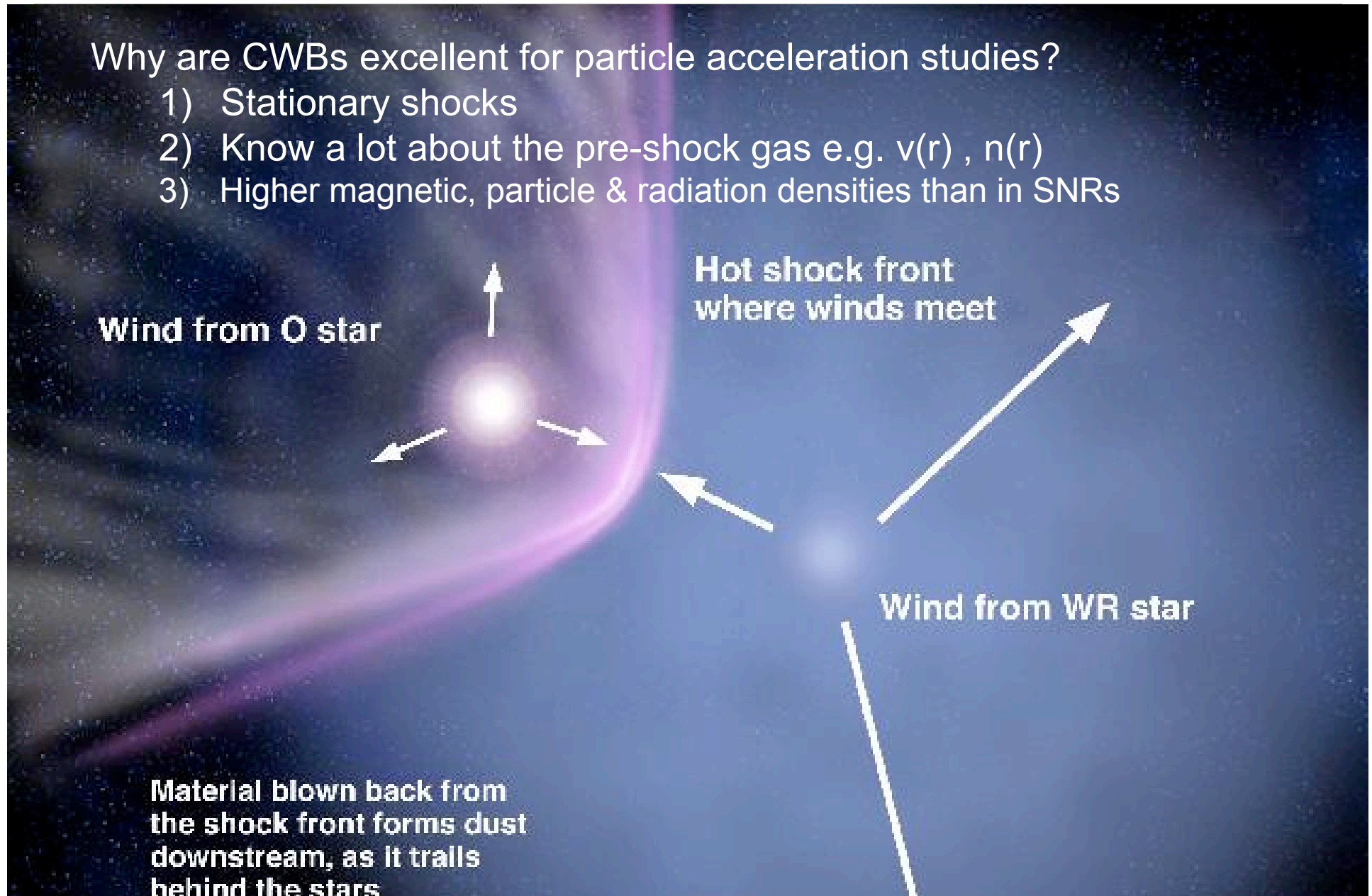


# Artists Impression of a Colliding Wind Binary

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Why are CWBs excellent for particle acceleration studies?

- 1) Stationary shocks
- 2) Know a lot about the pre-shock gas e.g.  $v(r)$  ,  $n(r)$
- 3) Higher magnetic, particle & radiation densities than in SNRs

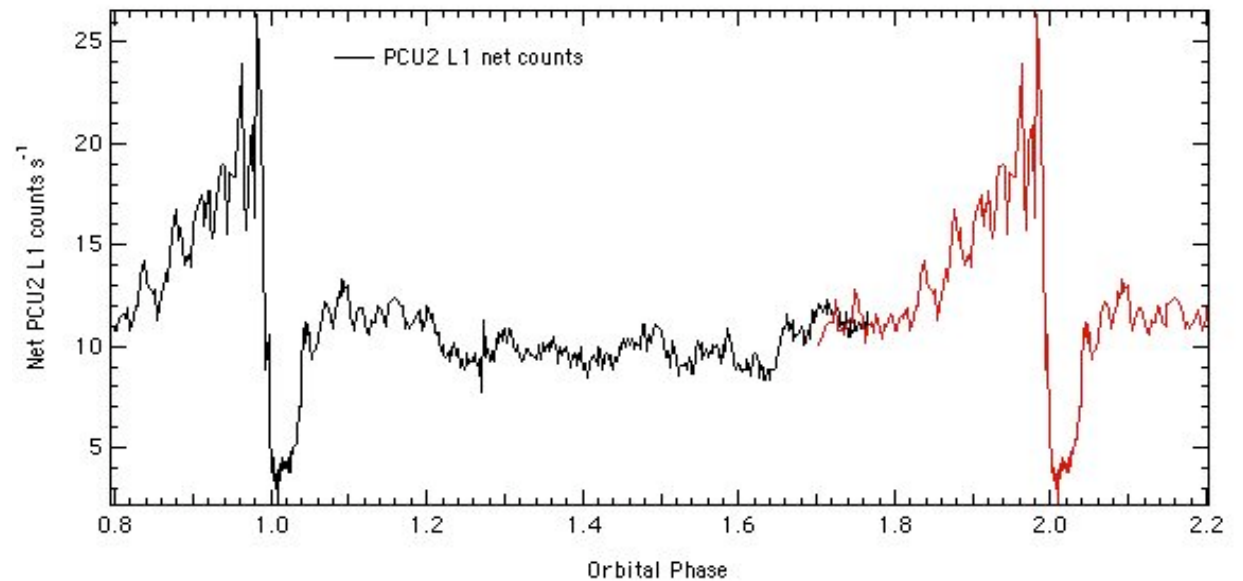
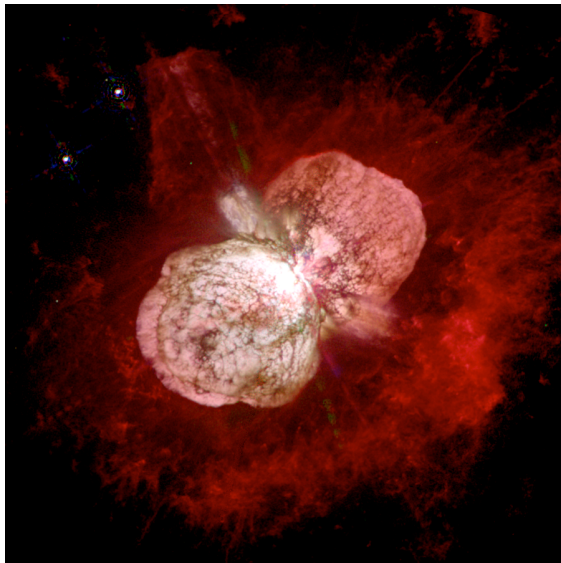


# CWBs probe wide range of parameters



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System	Orbital Period (d)	Separation (AU)	Density ( $\text{cm}^{-3}$ )	$\dot{M}_{\text{WR}}$	$\dot{M}_{\text{O}}$
WR 139 (V444 C)	4.2	0.2	$\sim 10^{10}$	$\ll 1$	?
WR 11 ( $\alpha^2$ Vel)	78.5	0.81-1.59	$\sim 10^9$	$\sim 0.5-1$	$\sim 250-500$
WR 140	2899	$\sim 1.7-27.0$	$\sim 10^9-10^7$	$\sim 2-50$	$\sim 150-2000$
WR 147	$> 10^5$	$> 410$	$\square 10^4$	<b><math>&gt; 30</math></b>	<b><math>&gt; 1000</math></b>



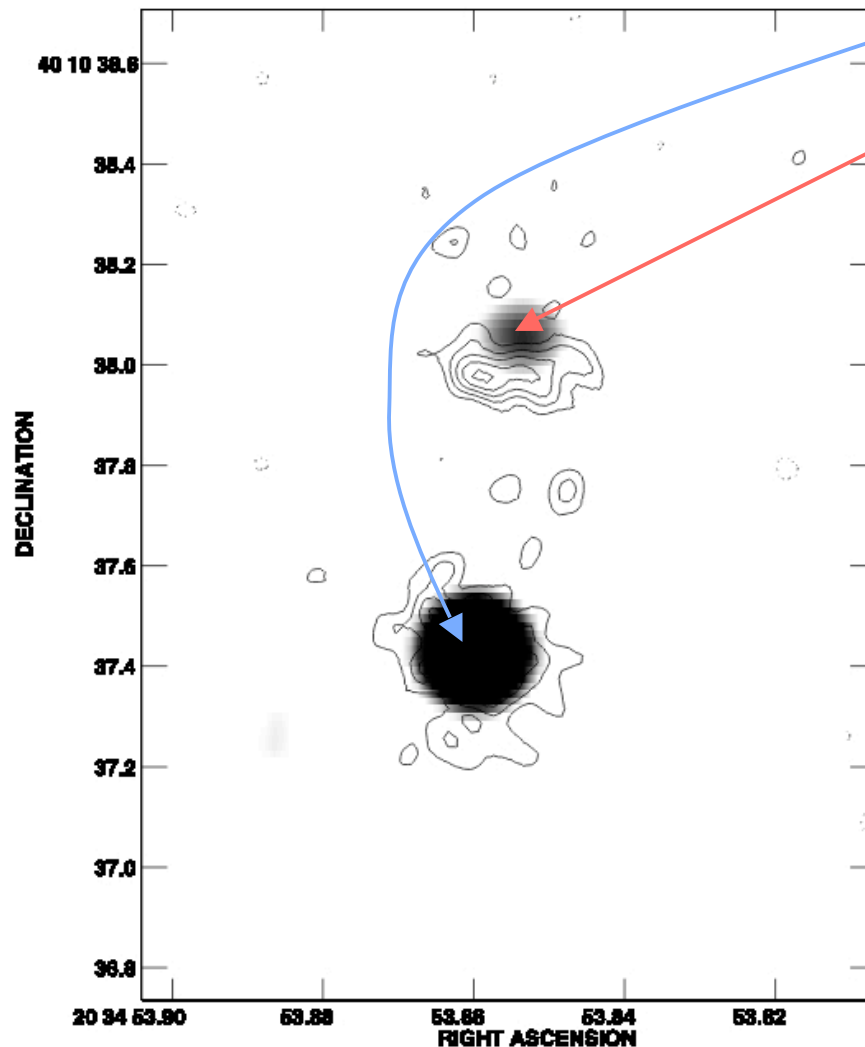
Corcoran et al.





# Radio structure of the WR+OB CWB - WR 147

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Two components, one thermal  
one non-thermal

High resolution observations  
- MERLIN @ 5GHz:

50 mas = 77AU @ 650pc

WR+OB binary

NT emission => relativistic  
electrons + magnetic fields

NT emission consistent  
with wind-collision position

Williams et al. (1997)



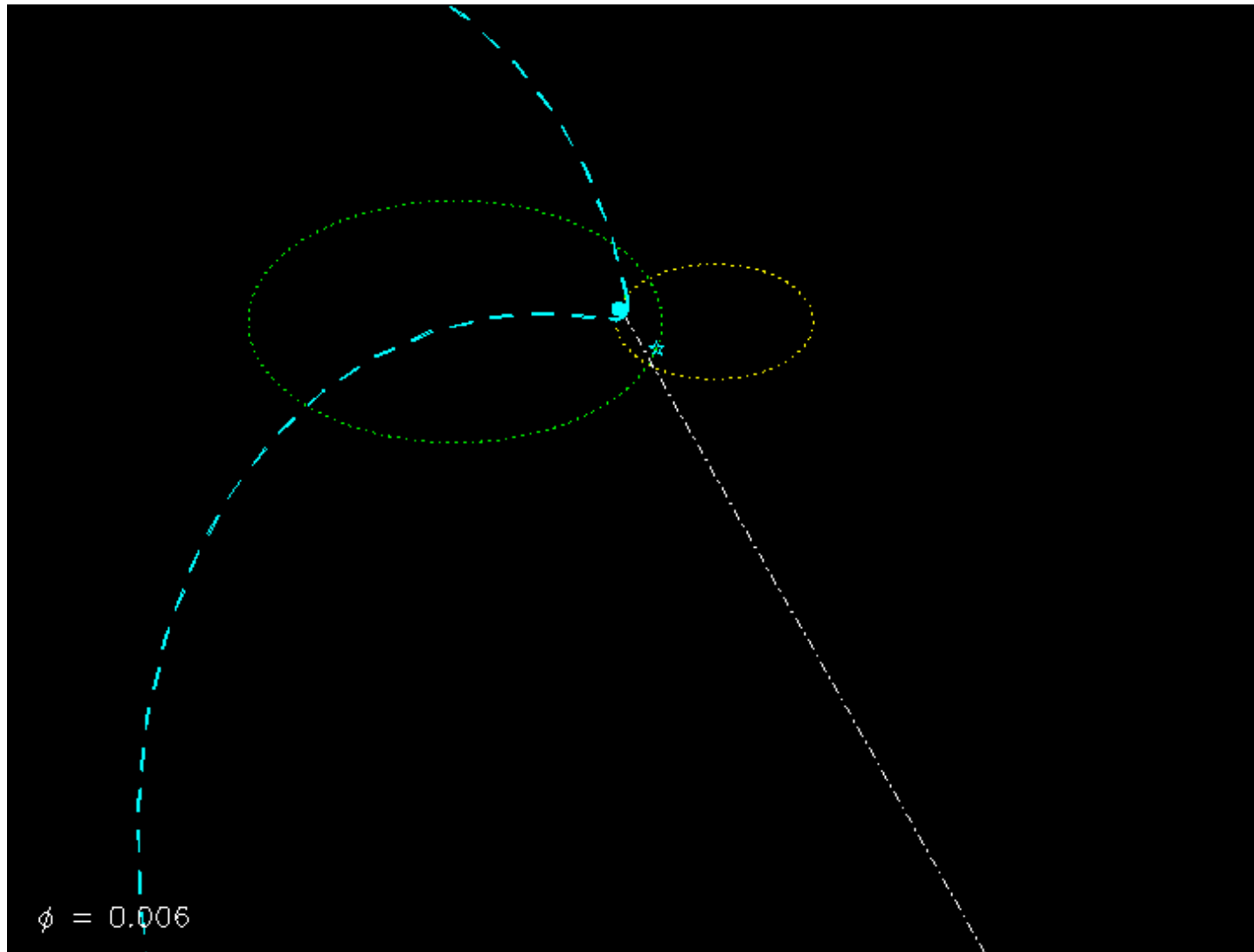
WR 140 is the best studied WR+OB binary

- WR + O in a 7.9 year, eccentric ( $e=0.88$ ) orbit - orbit size  $\sim 2-28$  AU
- X-ray spectra reveal non-equilibrium ionization, and (probably)  $T_e < T_i$
- Radio-bright; dramatic variations in radio emission as orbit progresses
- WCR resolved by VLBI
- Orbit well defined
- IC cooling important
  - Flow time  $\sim R_{OB}/v_{WR} \sim 100$  hrs at apastron
  - IC Cooling  $t_{IC} \sim 12$  hrs at apastron (at periastron  $\sim 250$  times shorter!)
  - IC cooling important at all radio frequencies under consideration
- High eccentricity + good data
  - excellent lab for studying shock phenomena

# Cartoon of the colliding-wind region in WR140



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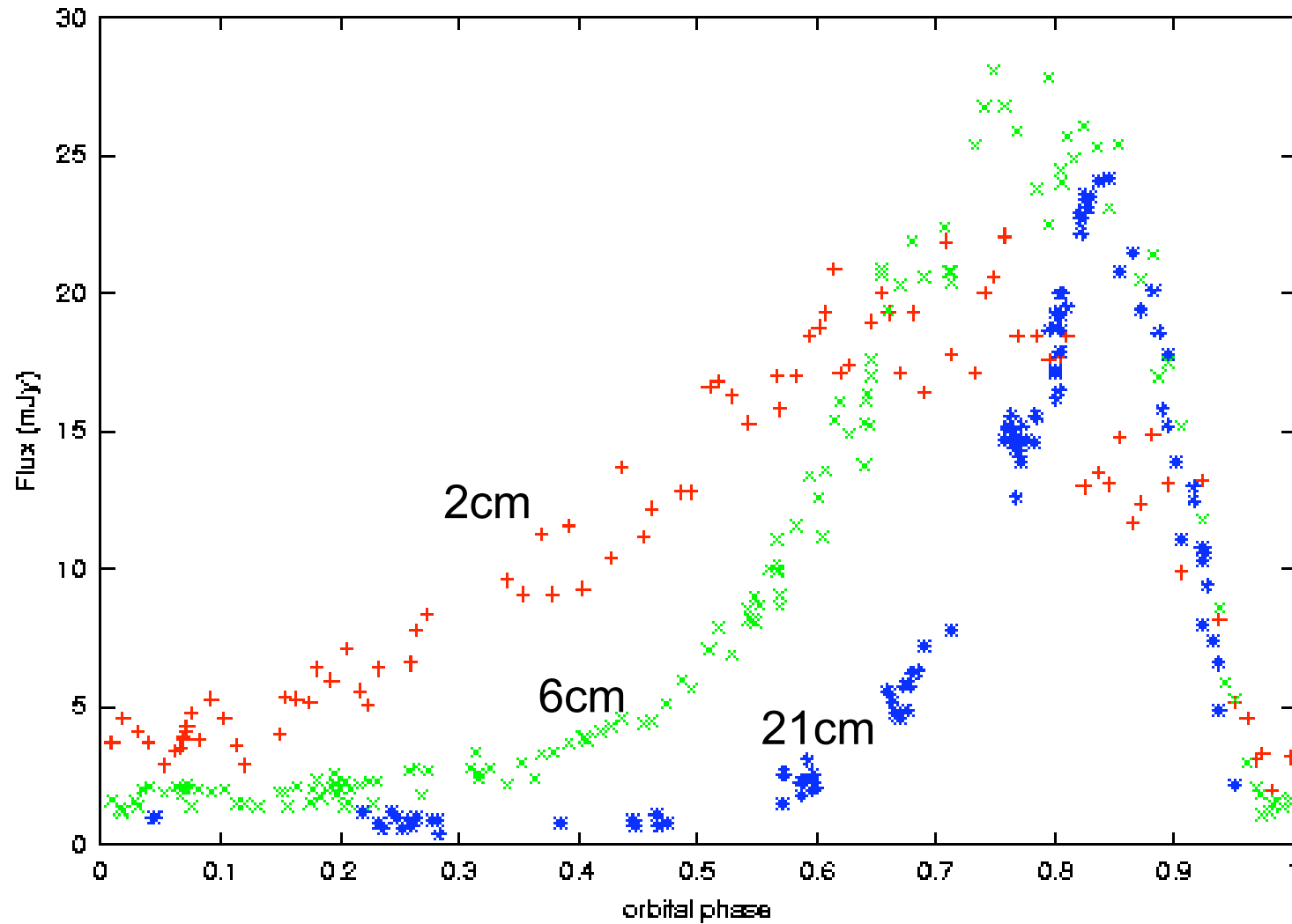


Orbit parameters from Williams et al. 1990 - interaction region based on Eichler & Usov 1993

# The radio light curve of WR140



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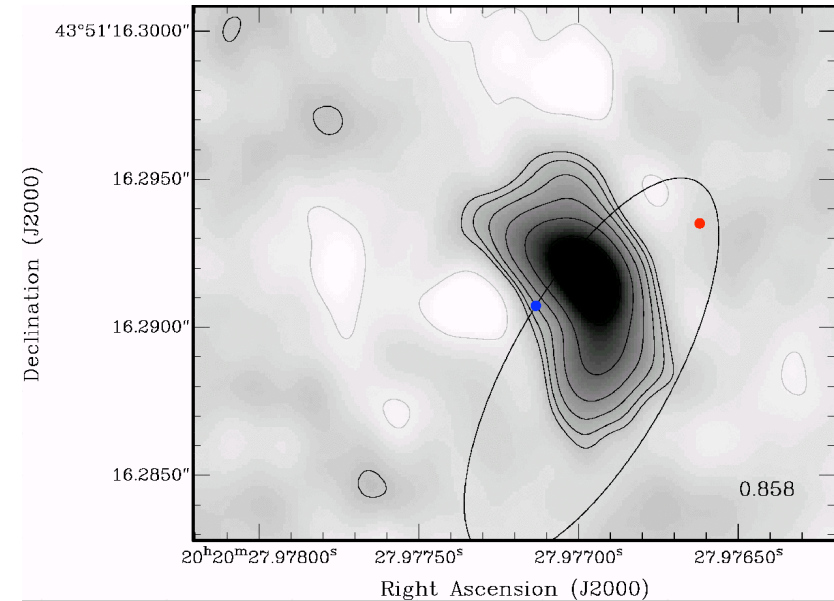


8 years of VLA (White & Becker 1995) +  
WSRT (Williams et al 1991) data



# VLBA images

State of the Art imaging!  
23 epochs @ 3.6 cm  
Phase  $\sim 0.74 \rightarrow 0.93$   
(Jan 1999 to Nov 2000)  
Resolution  $\sim 2$  mas  
Linear res  $\sim 4$  AU



Declination (J2000)

43°51'16.3000"

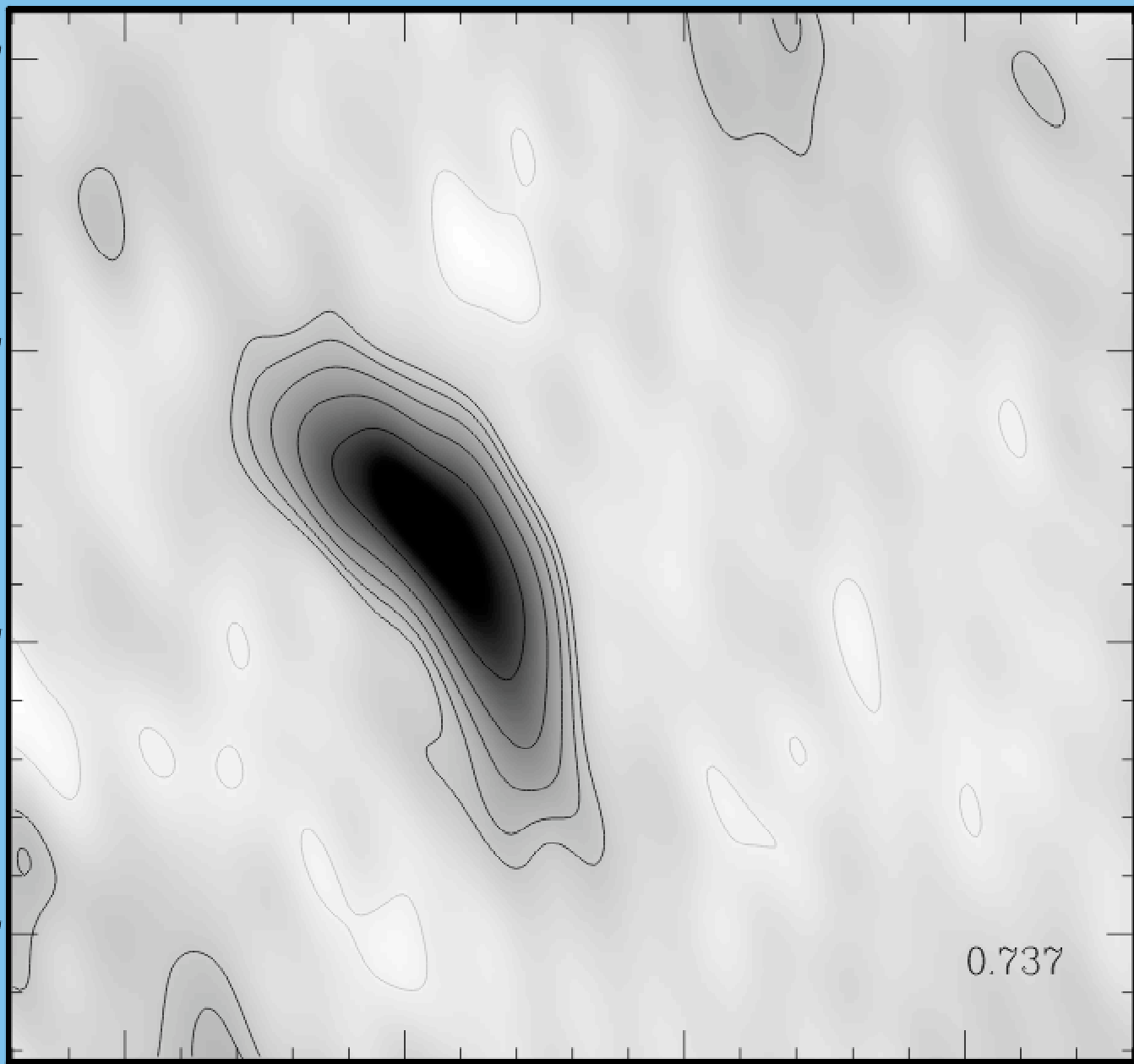
16.2950"

16.2900"

16.2850"

20<sup>h</sup>20<sup>m</sup>27.97800<sup>s</sup> 27.97750<sup>s</sup> 27.97700<sup>s</sup> 27.97650<sup>s</sup>

0.737



# VLBA images

State of the Art imaging!

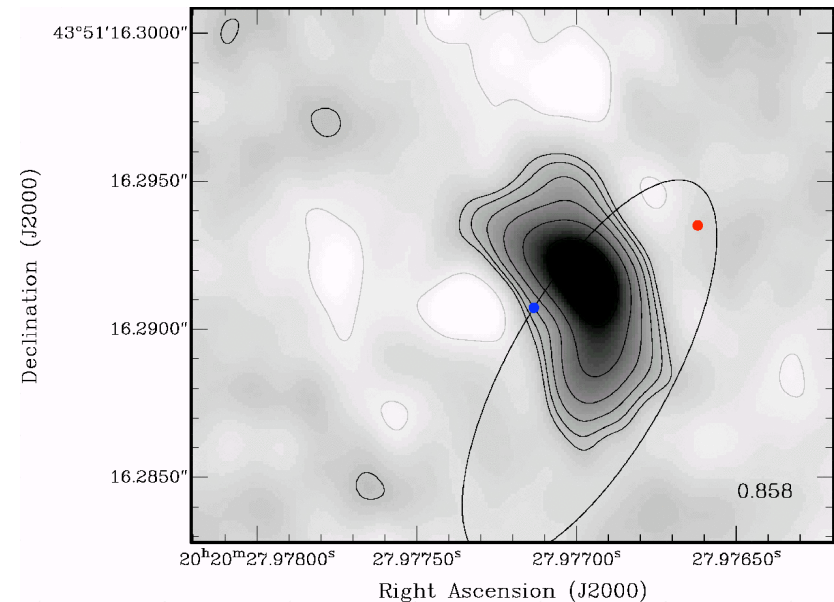
23 epochs @ 3.6 cm

Phase  $\sim 0.74 \rightarrow 0.93$

(Jan 1999 to Nov 2000)

Resolution  $\sim 2$  mas

Linear res  $\sim 4$  AU



- Non-thermal emission ( $T_b \sim 10^7$  K)  $\Rightarrow$  wind-collision region
- Resolved – “curved” emission region
  - cannot determine if NT arises in shocks or at CD
- Observe rotation and pm of emission region
  - gives full orbit definition – most importantly inclination
  - very important modelling constraint !
    - ... but wind mtm ratio still unconstrained



# Previous models

Models of NT emission tend to be simple

Radio:

- **Point source** non-thermal emission, radially symmetric winds –

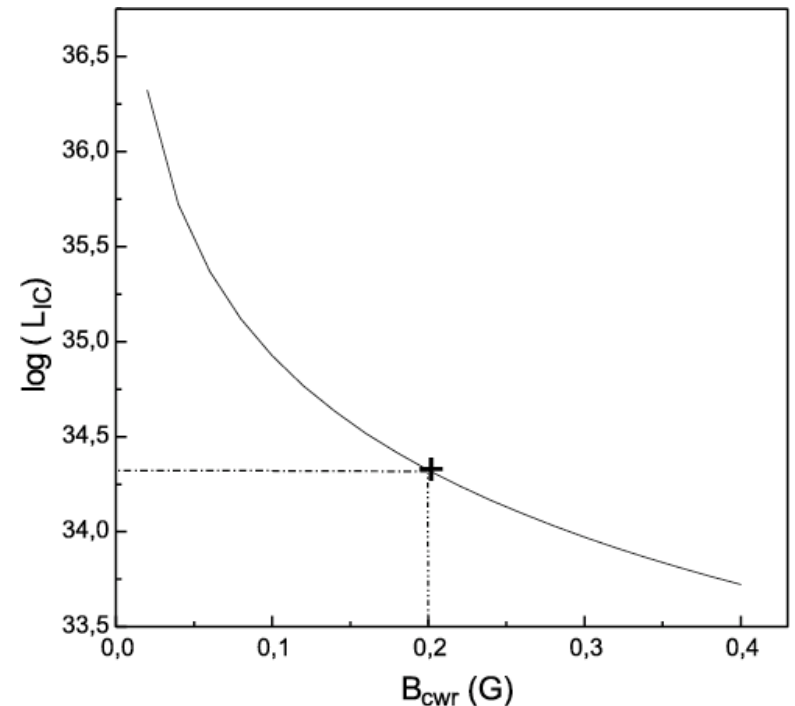
$$S_{\nu}^{obs} = S_{\nu}^{thermal} + S_{\nu}^{nt} e^{-\tau_{\nu}^{ff}}$$

- maintains analytic solutions

- **No consideration cooling mechanisms** (e.g. IC cooling – important - even for wide systems c.f. 146, 147) or other absorption

NT X-ray/\_-ray:

$$\frac{L_{sync}}{L_{ic}} = \frac{U_B}{U_{ph}}$$



Benaglia & Romero (2003)

**Issues:**  $L_{ic}$  is highly sensitive to the assumed B-field  
 Need the intrinsic (NOT observed)  $L_{sync}$

**Model fits to the radio data directly determine the NT particle population**





# Modelling radio emission from CWBs

## Hydro modelling of CWBs

- radially symmetric, terminal velocity isothermal winds
- axis-symmetric WCR

## Treatment of non-thermal emission

- not determined from 1<sup>st</sup> principles!  $U_{\text{rel}} = \beta_{\text{rel,e}} U_{\text{th}}$  and  $U_{\text{B}} = \beta_{\text{B}} U_{\text{th}}$

Tangled magnetic field

Assume shock acceleration

- power-law energy distribution at the shocks (**p is a free parameter**)

Electron energy spectrum evolves downstream due to IC cooling.

Spatial distribution of emission & absorption – determined by plasma spatial distribution from hydro

Constrained by radio spectra and images

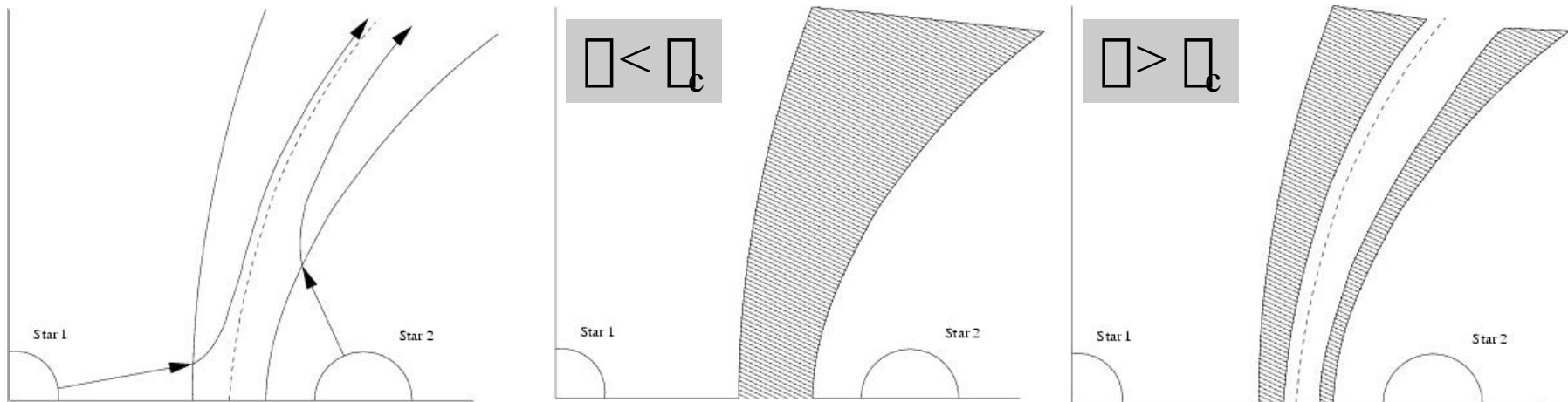
# Inverse Compton cooling



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Rate of energy loss:  $\frac{d\tilde{\epsilon}}{dt} \propto \tilde{\epsilon}^2$

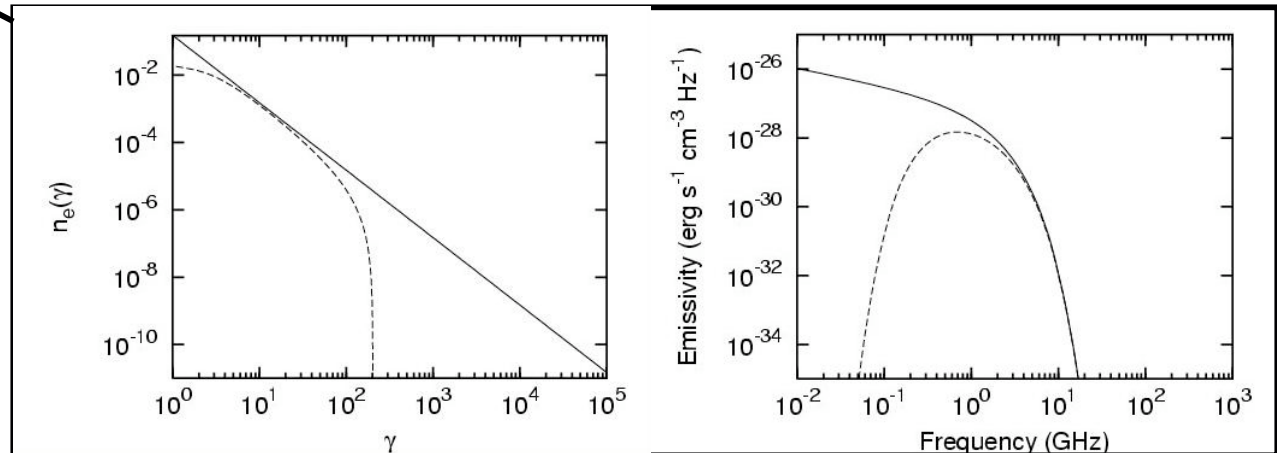
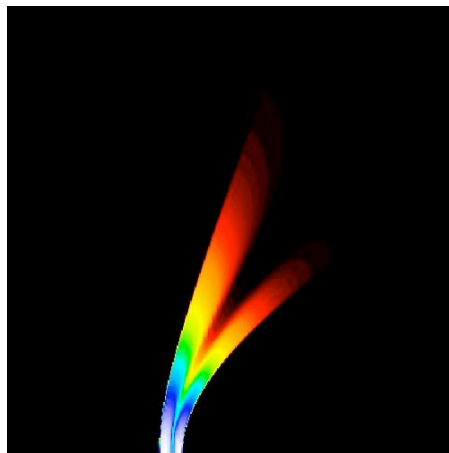
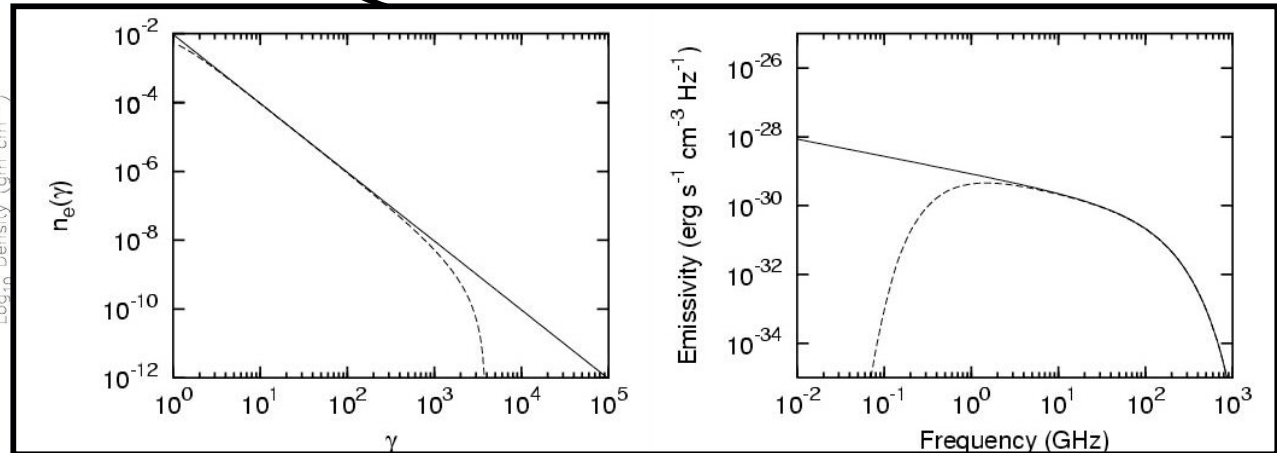
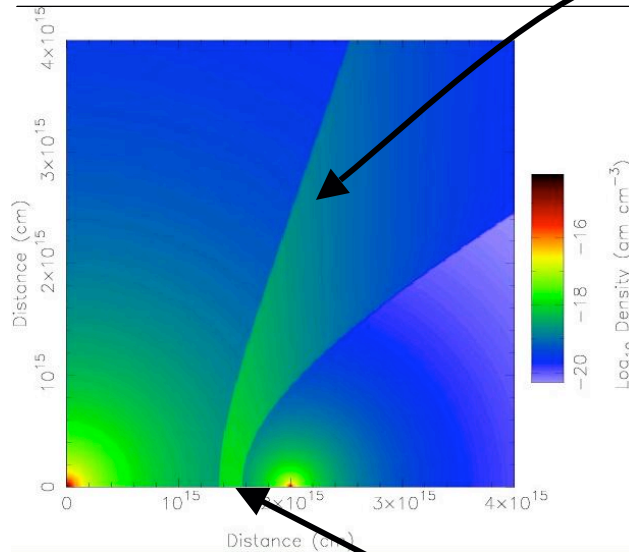
Distribution of relativistic electrons:



# Salient features of modelling IC cooled spectra



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1.6 GHz emission map



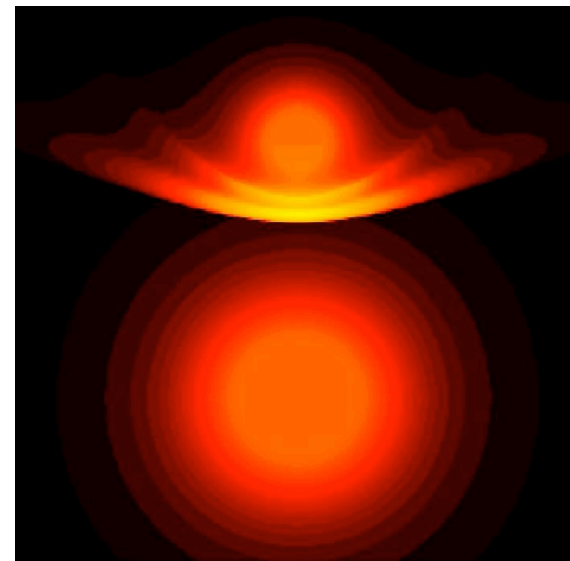
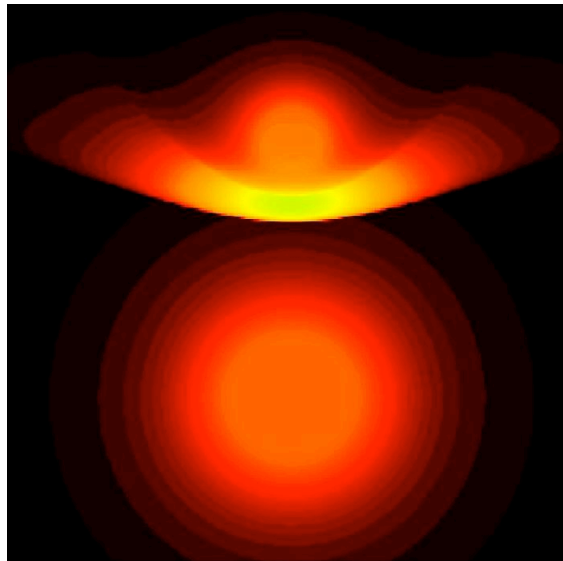
# Example synthetic emission maps

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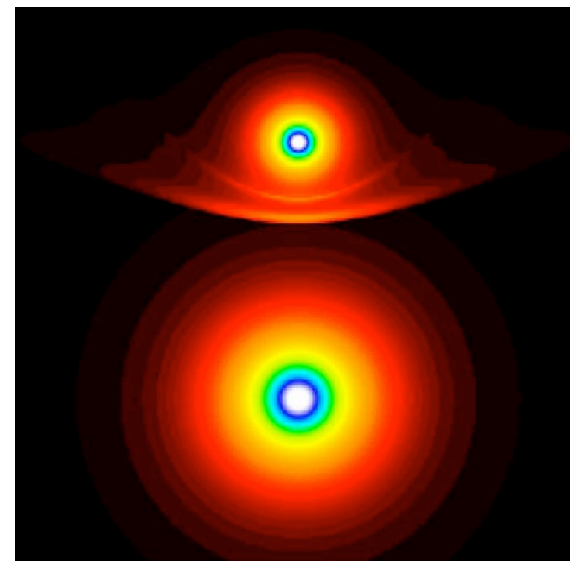
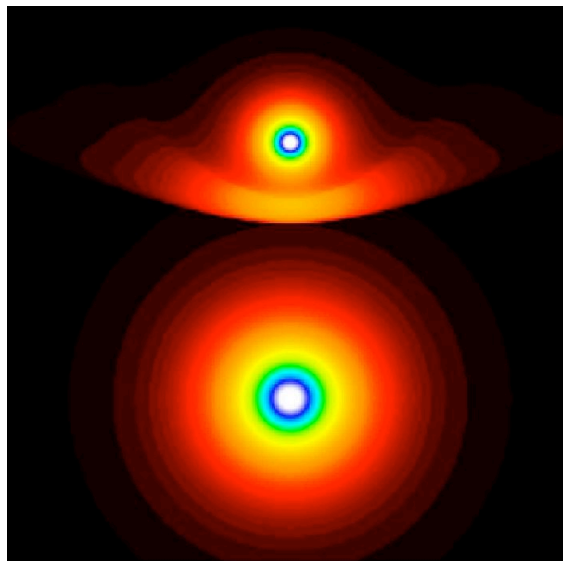
No IC cooling

With IC cooling

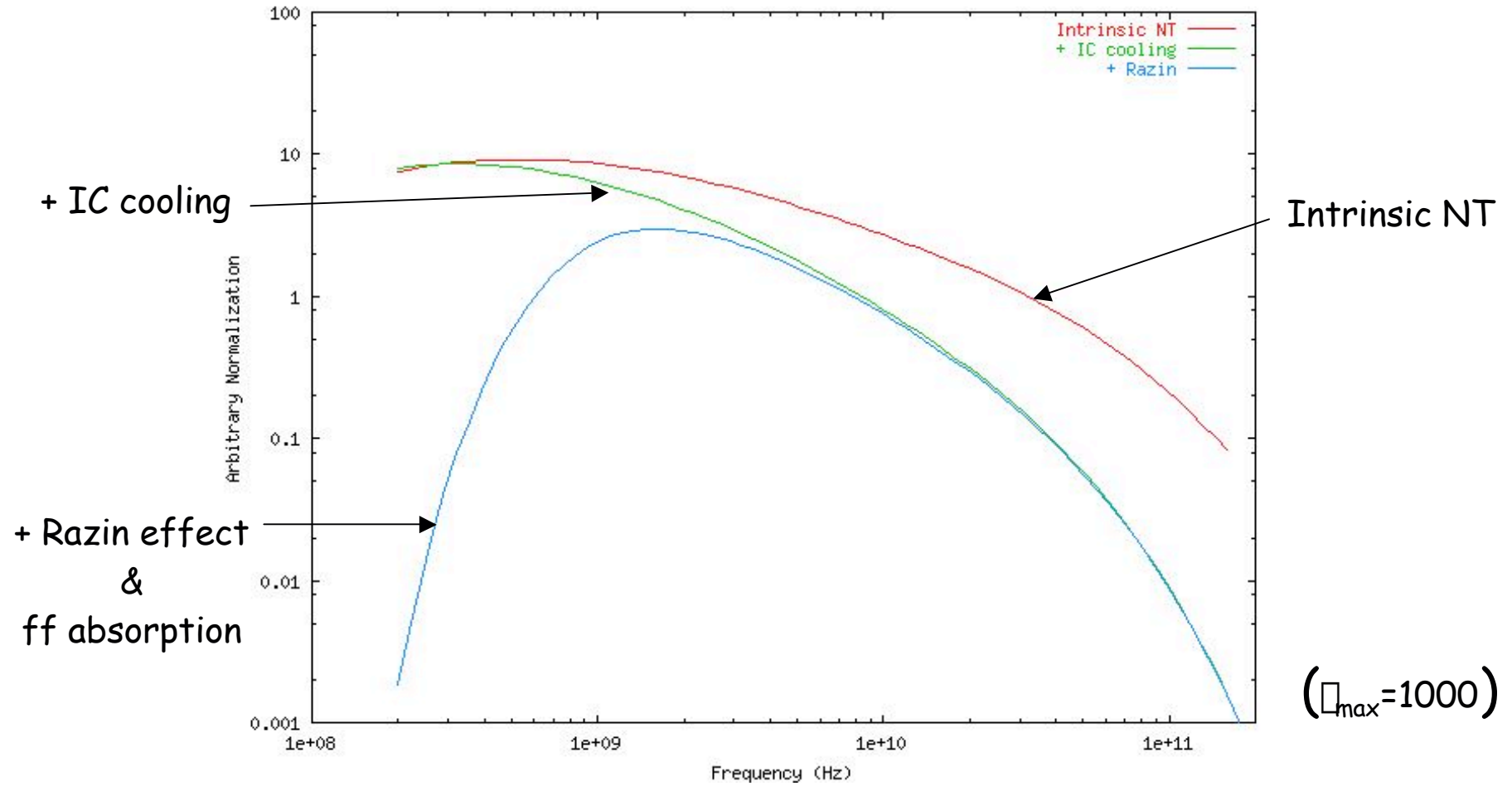
1.6 GHz



22 GHz



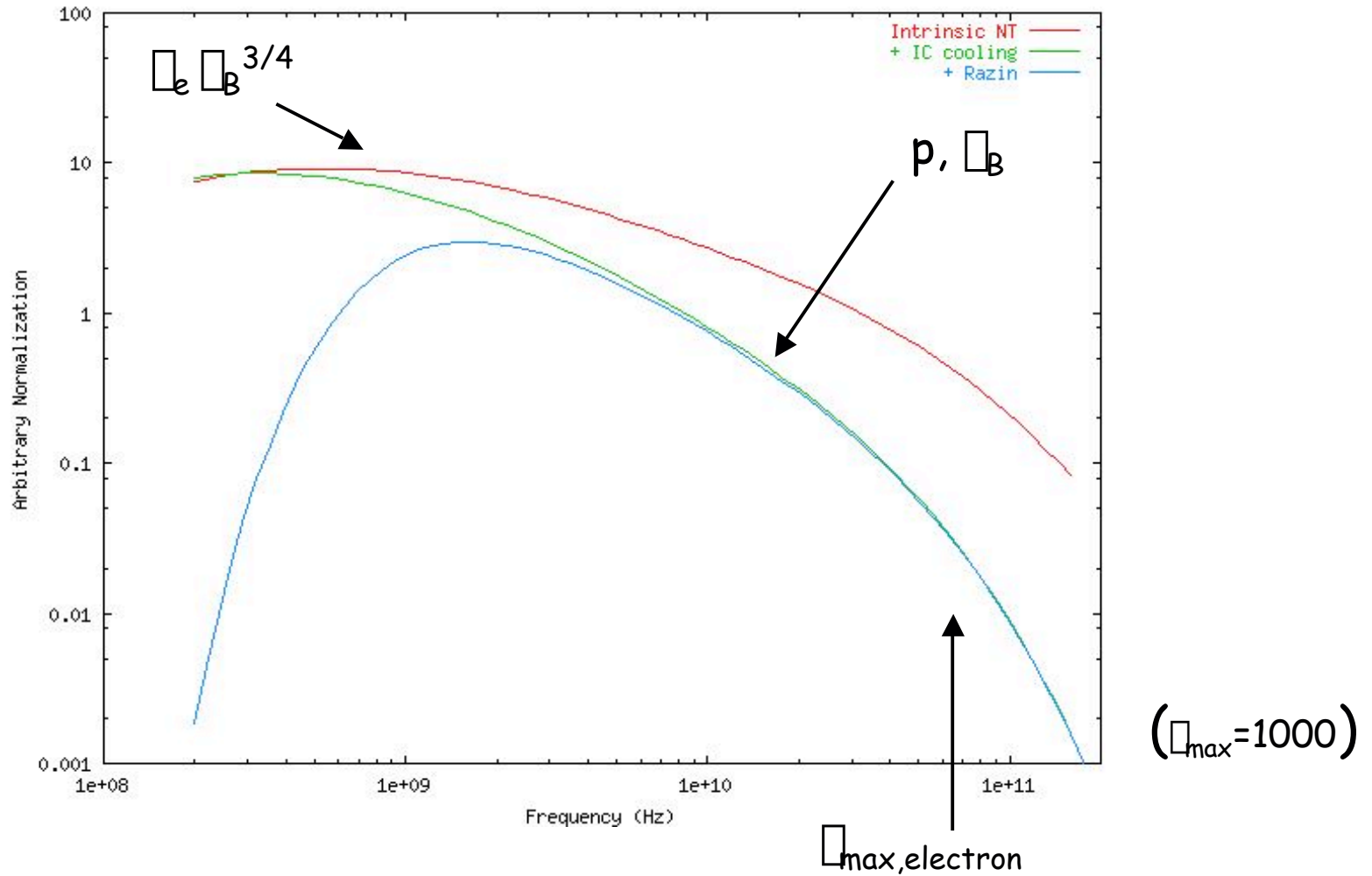
# Typical radio spectra



# Typical radio spectra

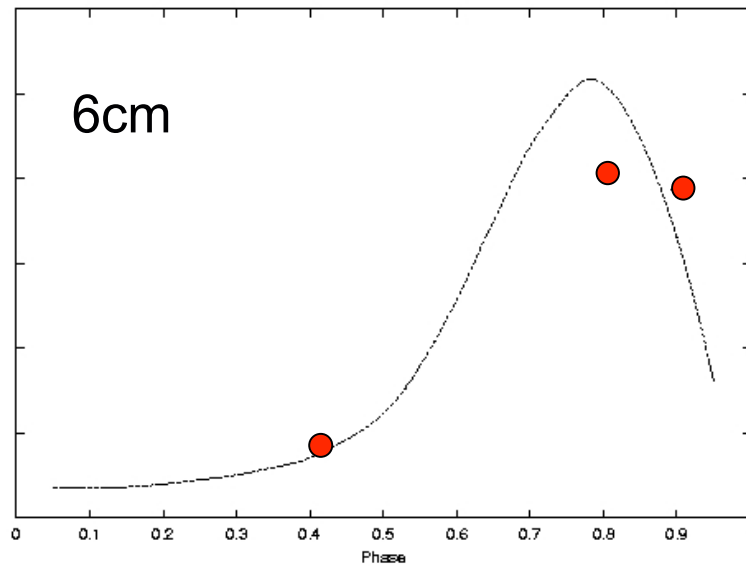
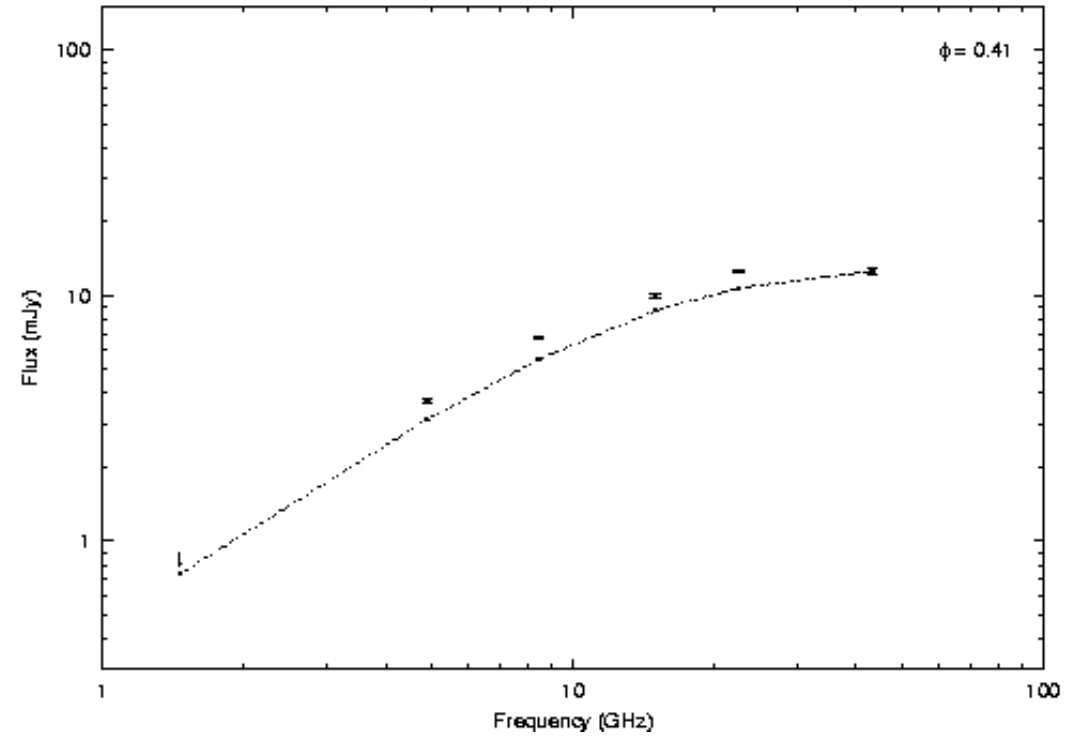
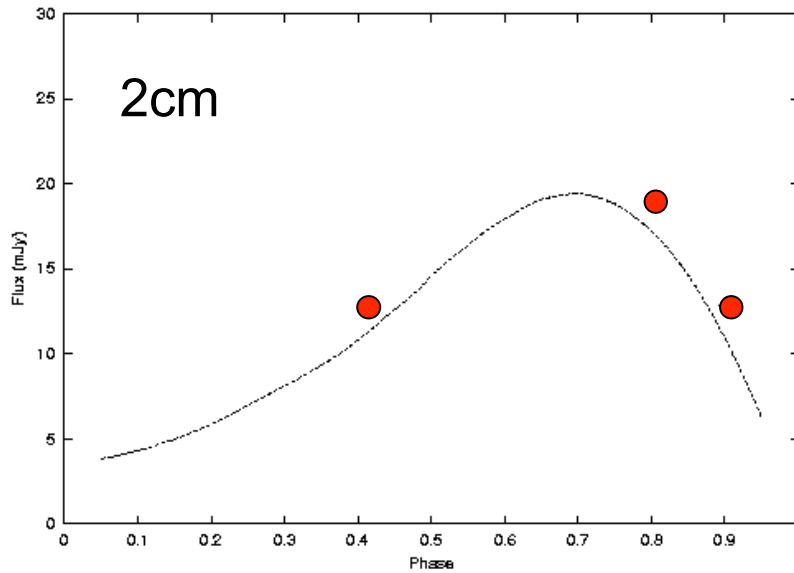


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# First stab at modelling WR140



Looking good

But...

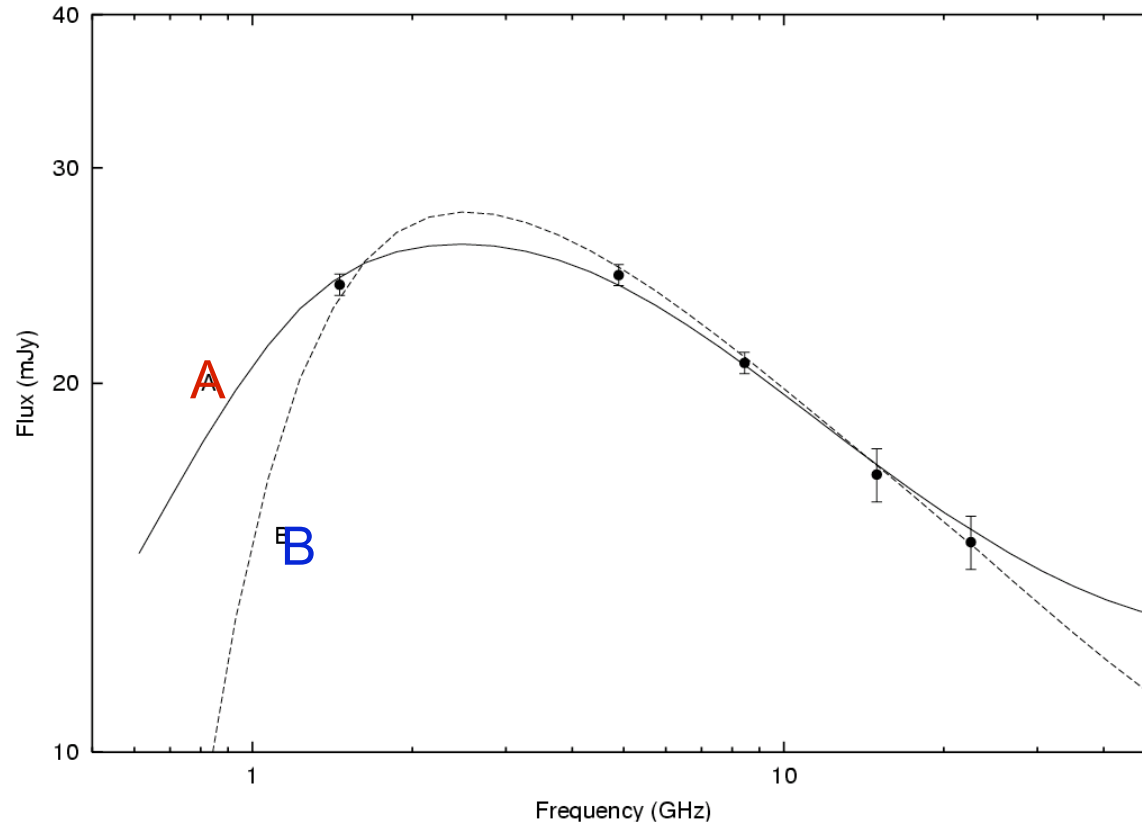
Relationship from one phase to another is  
**UNCLEAR** – NOT good!

Continues as a work in progress...

# Spectral fits at phase 0.837



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**Model A:**  $\alpha=0.22$ ,  $p=1.4$ ,  $\alpha_e=1.4 \times 10^{-3}$ ,  $\alpha_B=0.05$

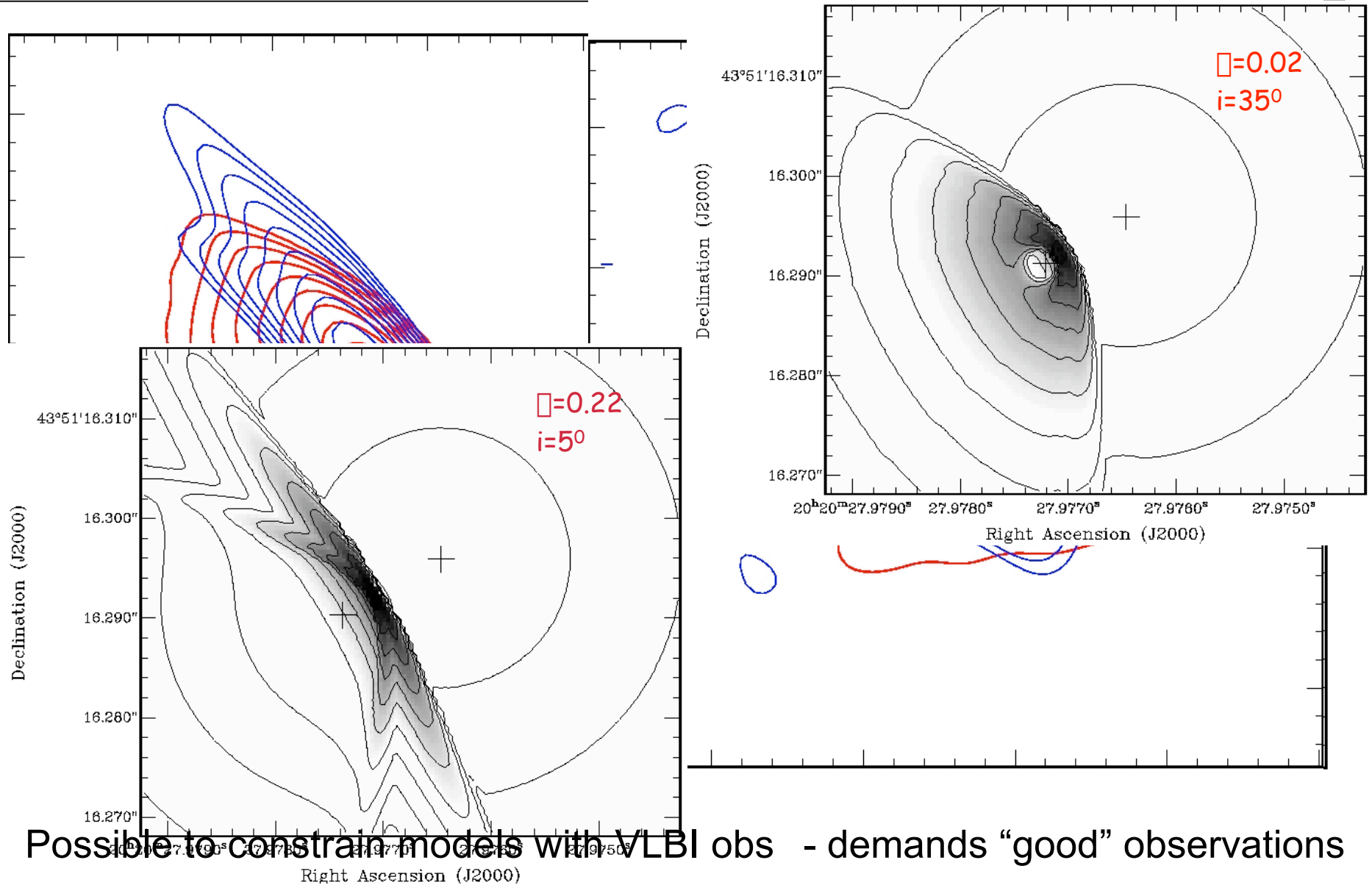
**Model B:**  $\alpha=0.02$ ,  $p=1.4$ ,  $\alpha_e=5.4 \times 10^{-3}$ ,  $\alpha_B=0.05$

A caveat –  $p$  and  $\alpha_B$  are degenerate parameters in these models

**Crucially, we cannot obtain fits with  $p = 2$ !**



# Modelling 8 GHz VLBA observations

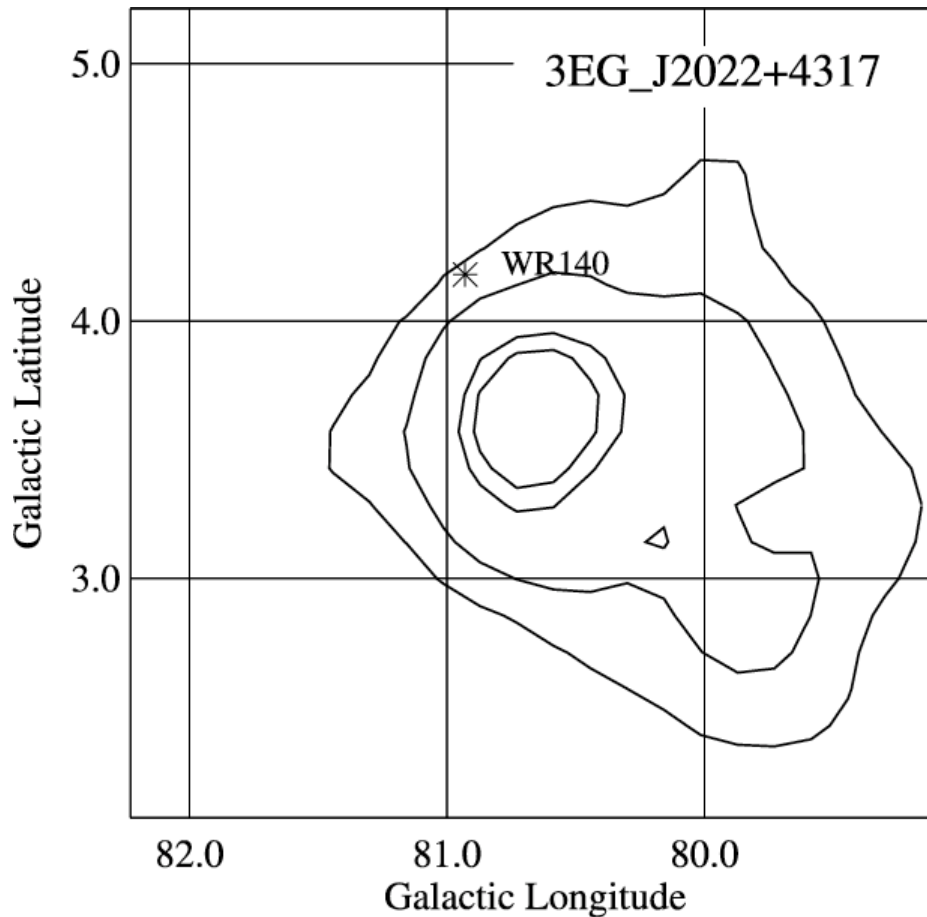


Possible to constrain models with VLBI obs - demands "good" observations

# MeV/GeV emission?



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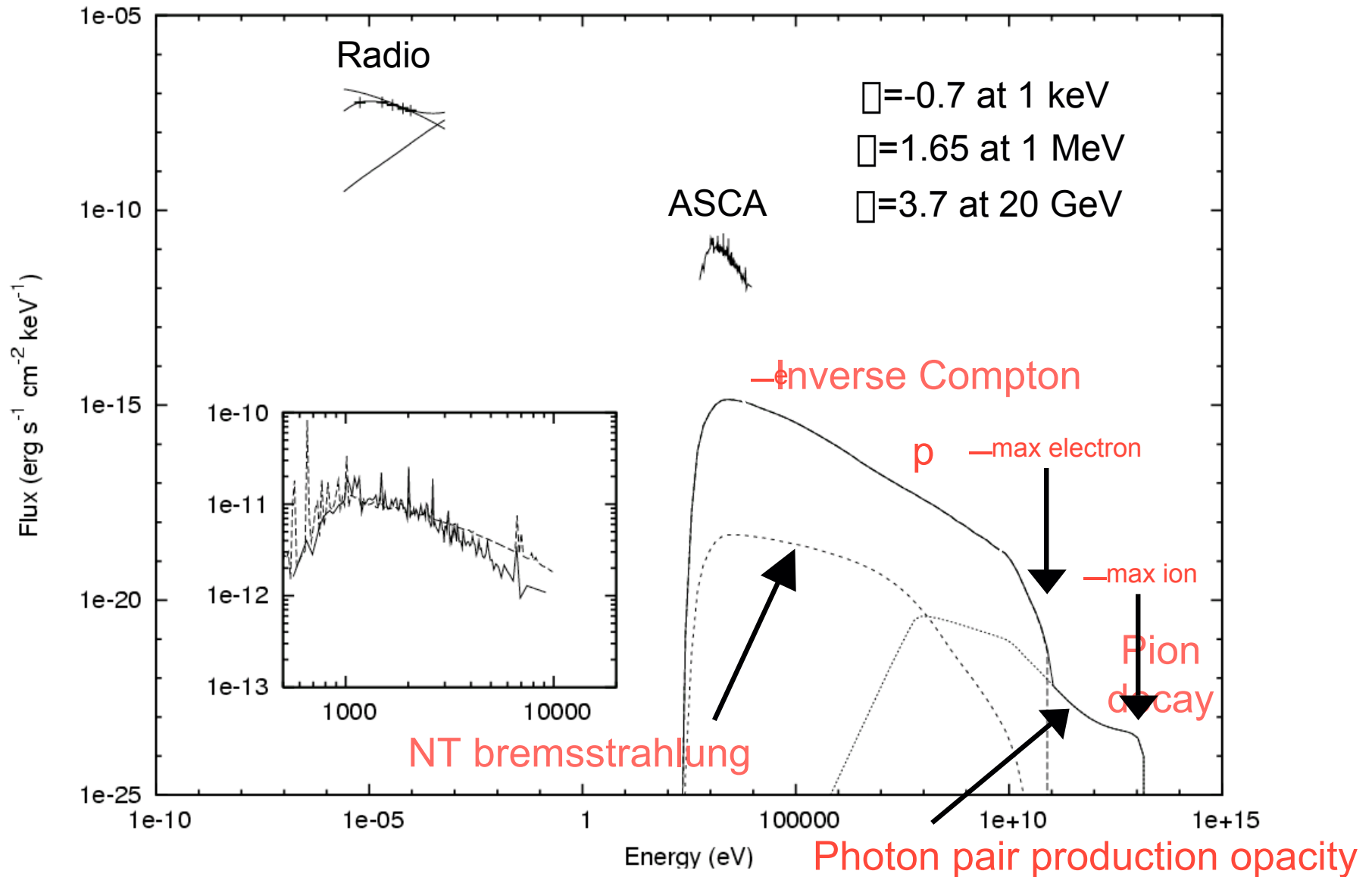
EGRET (100MeV – 20 GeV)

$$f_{\gamma} = (24.7 \pm 5.2) \times 10^{-8} \text{ ph s}^{-1} \text{ cm}^{-2}$$

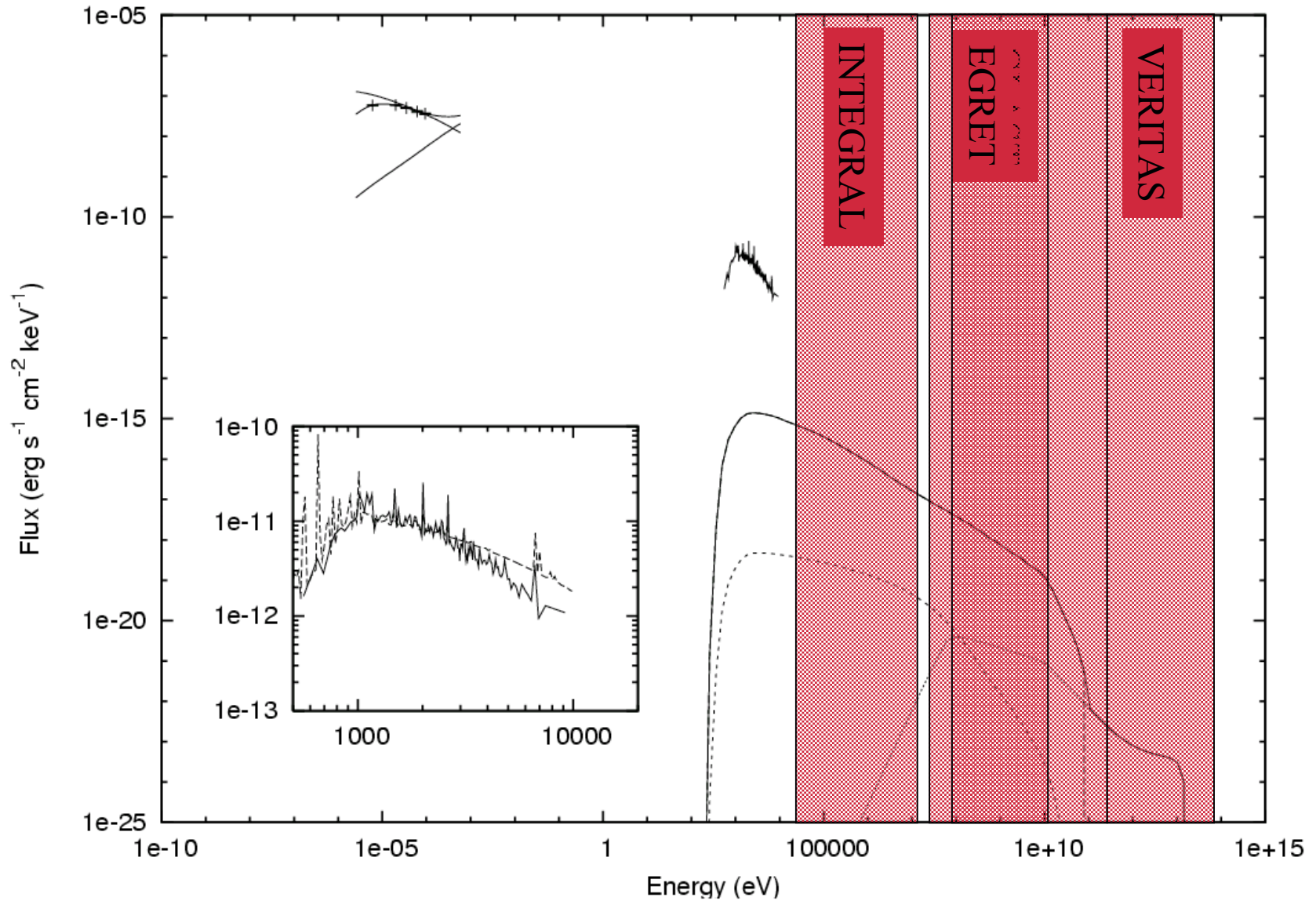
$$\Gamma = 2.31 \pm 0.19 \text{ (where } N(E) \propto E^{-\Gamma})$$

Benaglia & Romero (2003)

# High energy emission at phase 0.837



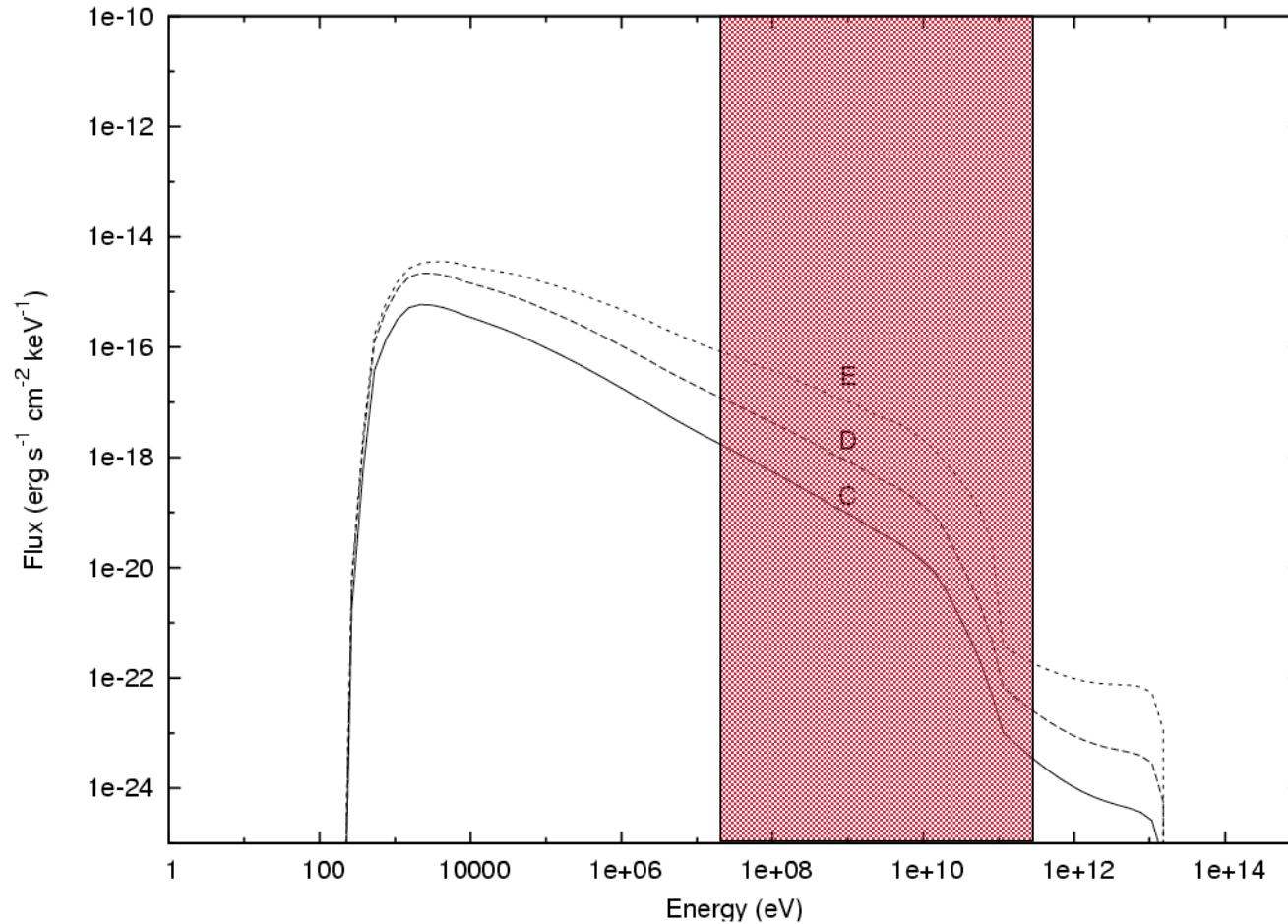
# High energy emission at phase 0.837



# Model discrimination



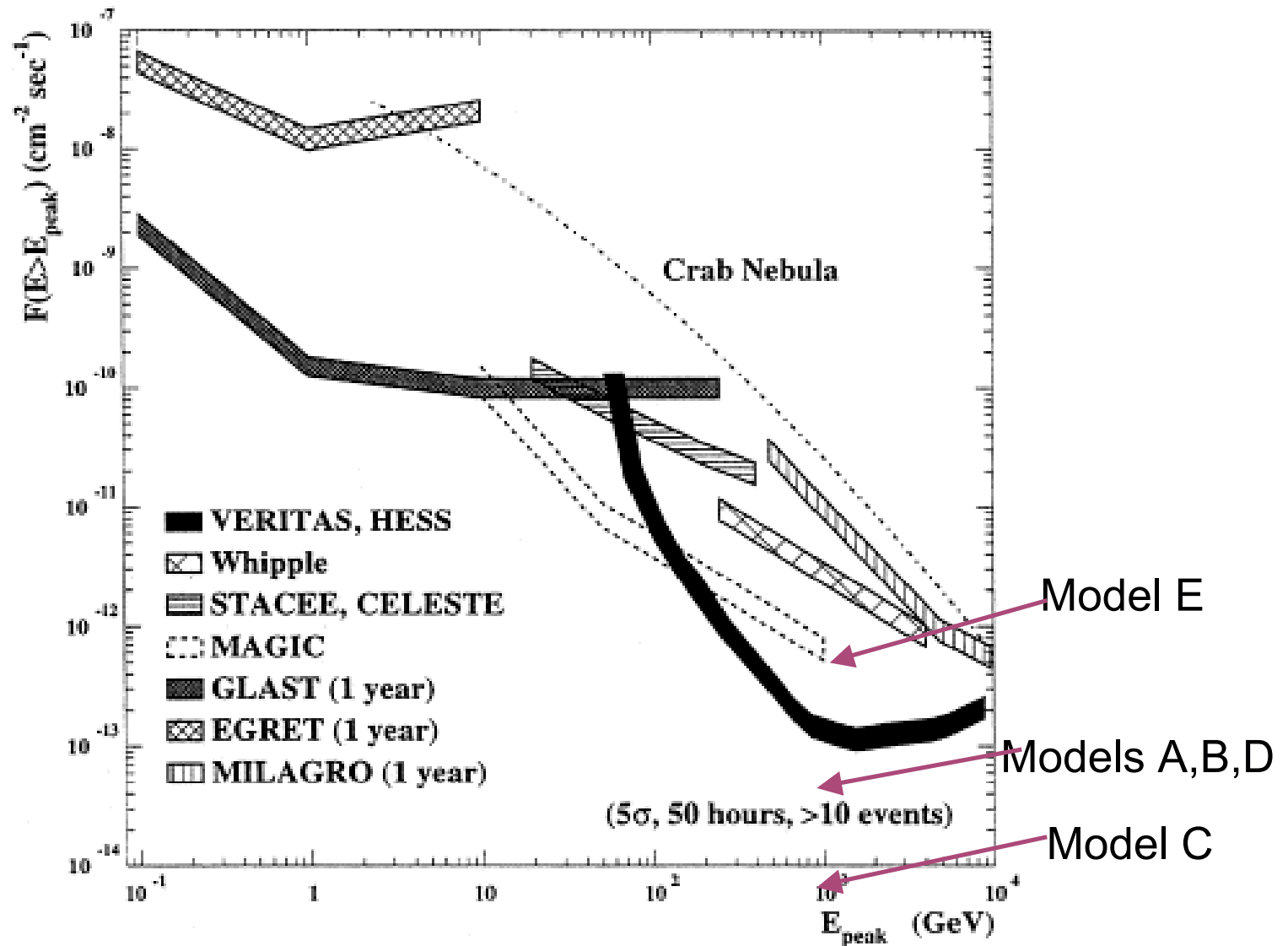
GLAST will be able to discriminate between models



Will place constraints on the spectral index and B-field

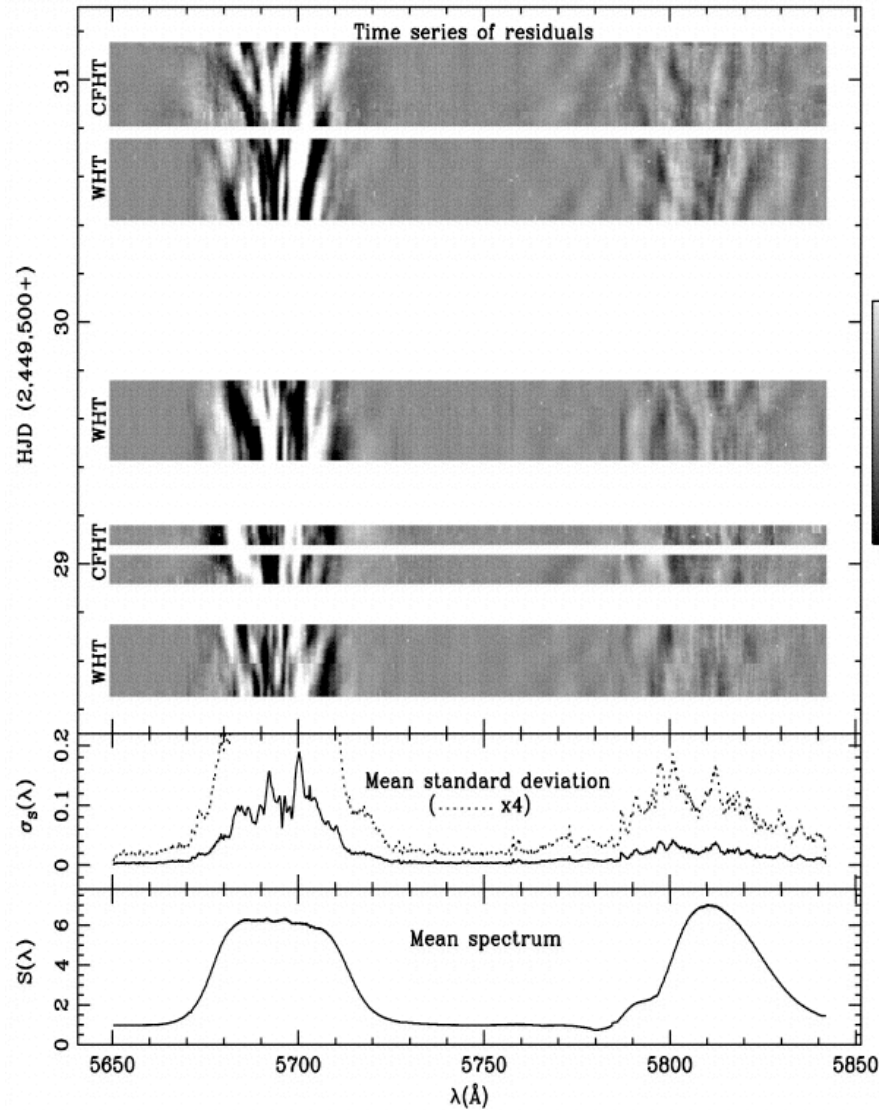


# Flux at TeV energies in VERITAS band

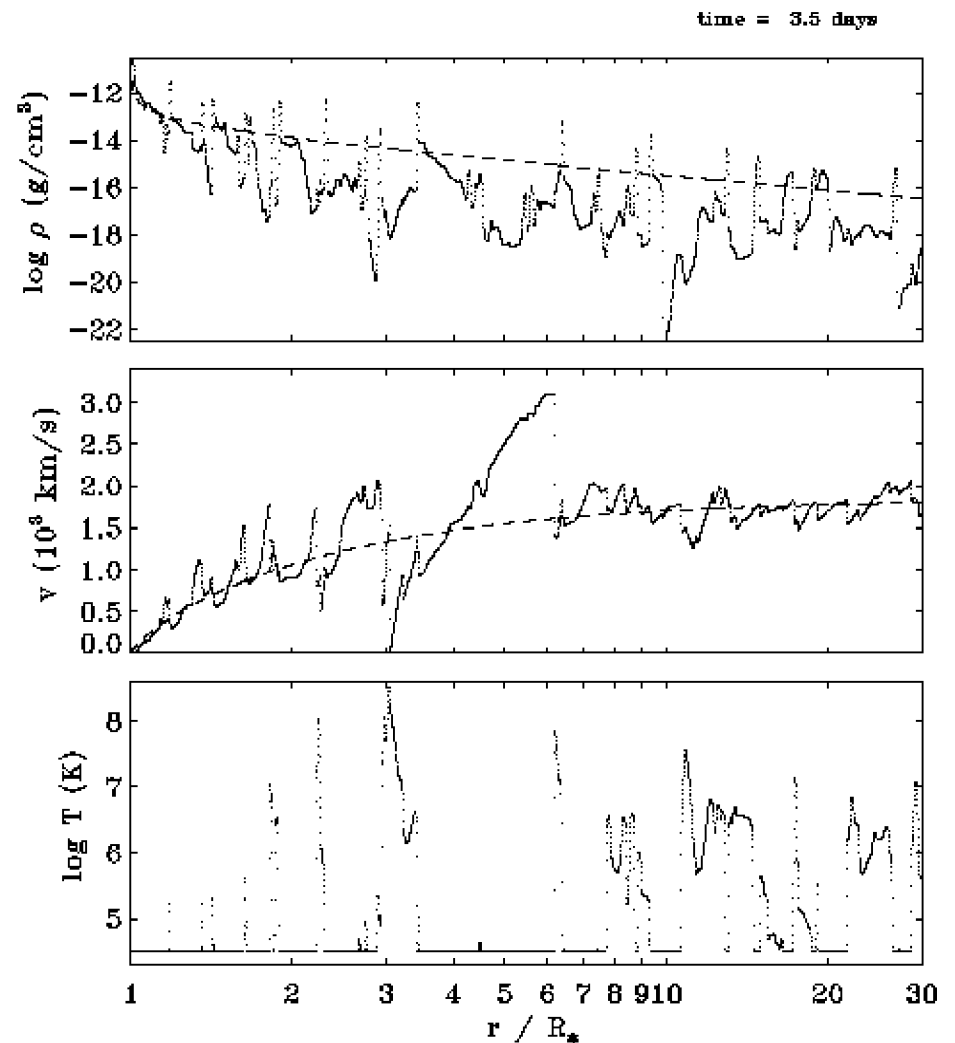




# Hot star winds are very clumpy



Lepine et al. (2000)

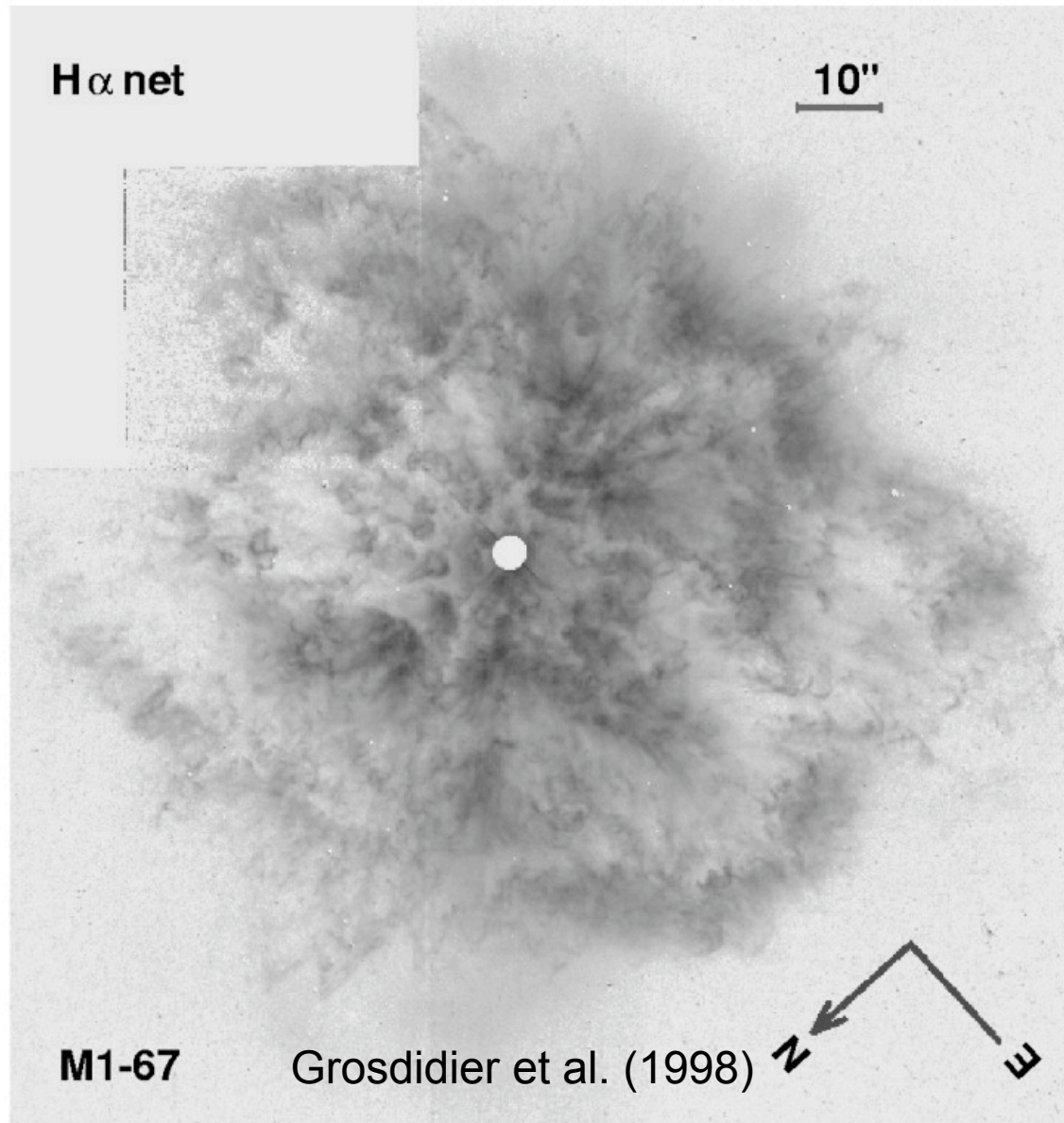


Feldmeier et al. (1997)

# Hot star winds are very clumpy



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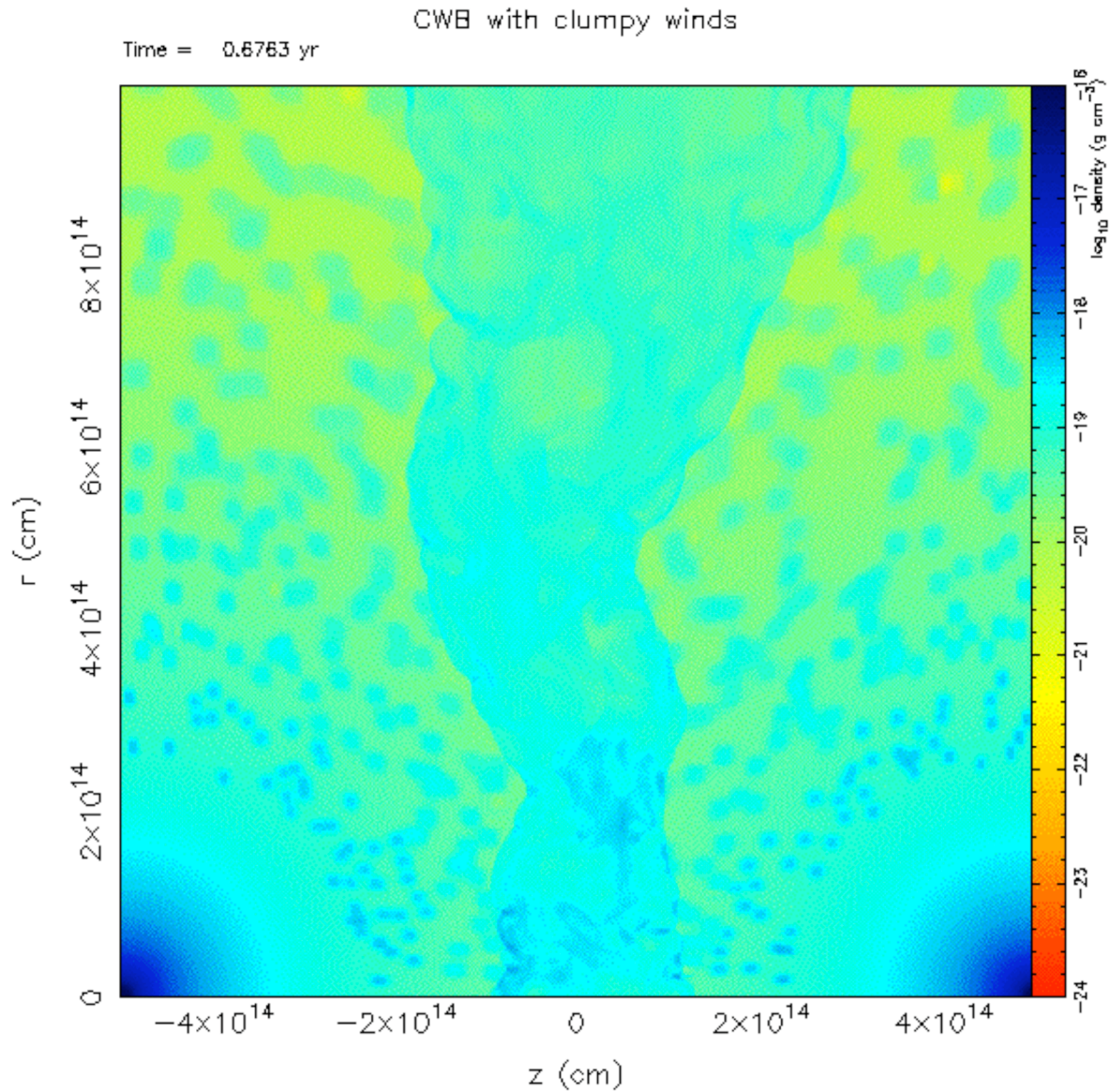




# Clump destruction in adiabatic CWBs



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Implications for  
particle accn?

Reconnection?

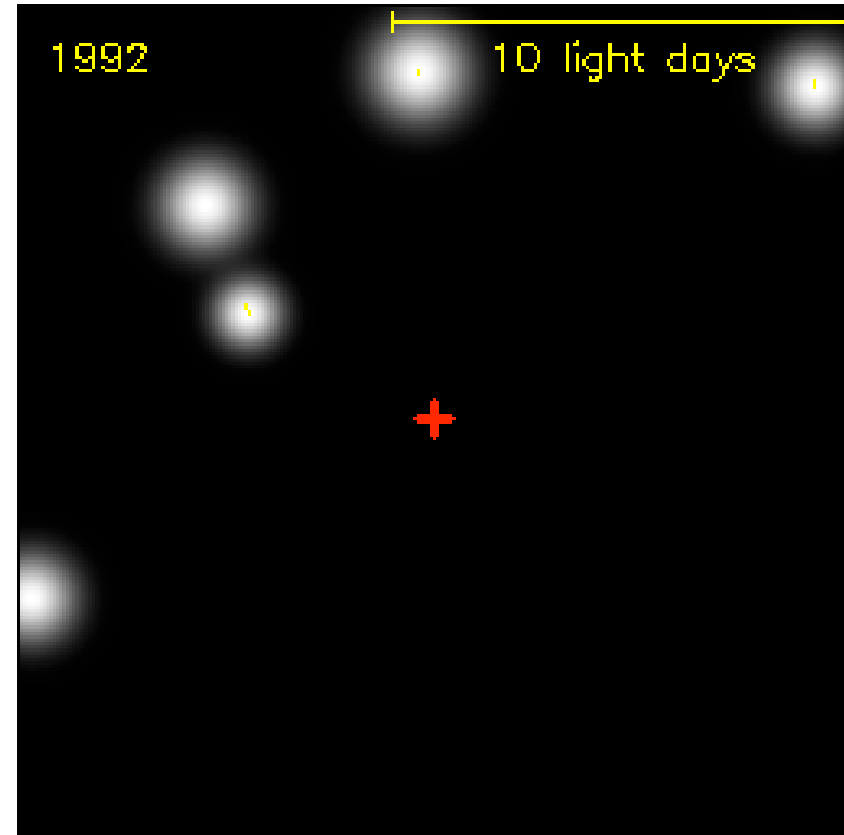
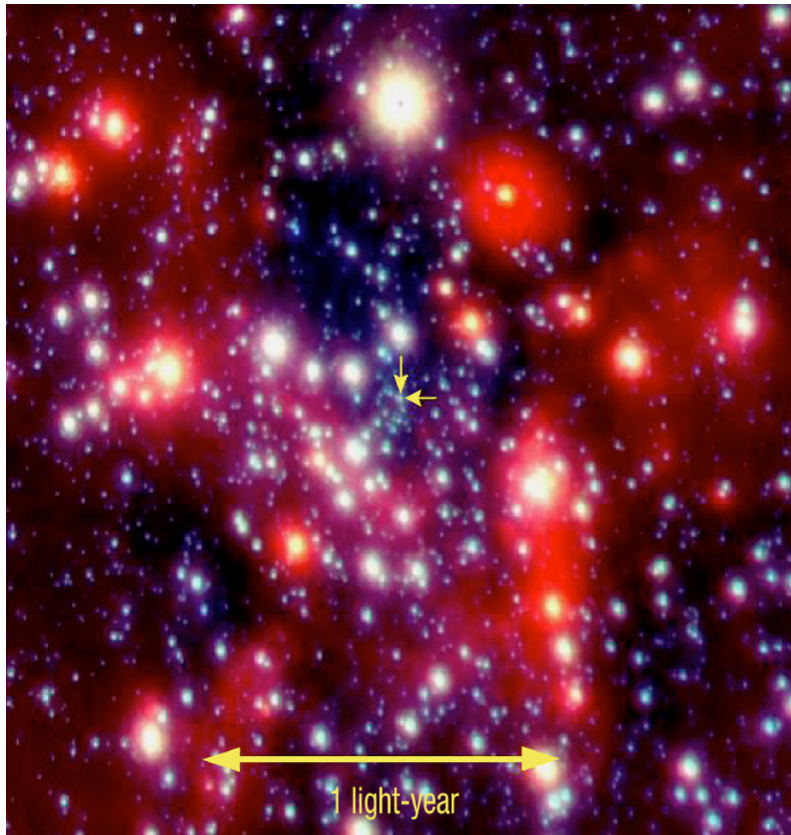
Stochastic accn?

# Colliding Winds in Stellar Clusters



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Stars seen in IR are rotating around a faint radio, IR and X-ray source:  
Sgr A\*



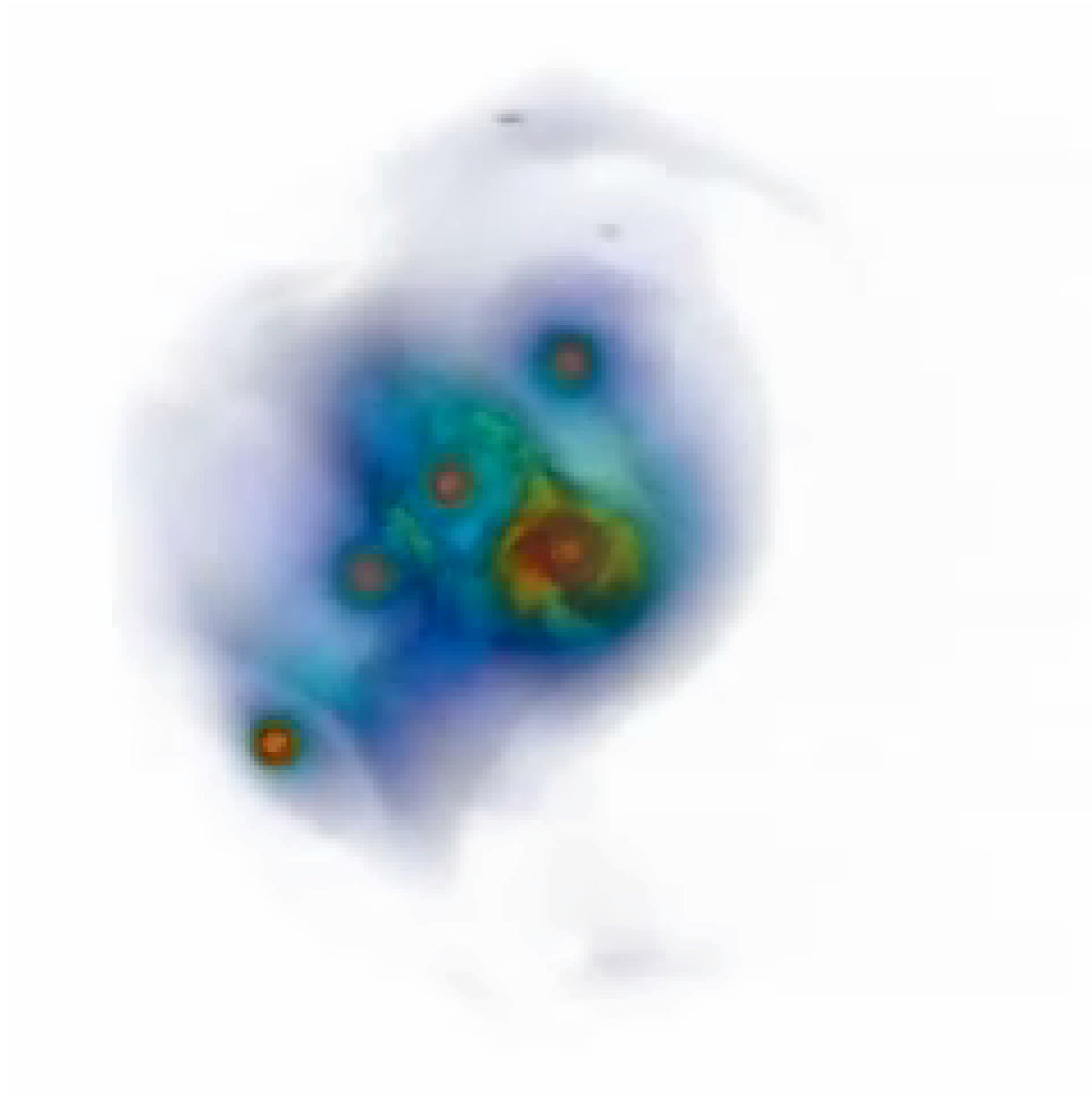
MPE / R. Genzel et al.

# Movie of the Galactic Center

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Coker &  
Pittard



# Conclusions

**Colliding winds** in early-type binaries are important laboratories for investigating shock physics and particle acceleration

Highly eccentric systems – like WR140 – are particularly useful

Models of radio/X-ray/\_-ray emission suggest...

- i) **adiabatic WCR gives clumping independent measure of  $\dot{M}$ 's**
- ii)  **$T_e < T_i$ , and/or shock modification**
- iii) **a low value of wind  $\dot{m}$  ratio**
- iv) **the NT electron distribution has  $p < 2$**   
**- reacceleration at shocks internal to WCR?**

...and have provided insight into particle acceleration efficiencies, and the strength of the B-field

Exciting period in the next few years (GLAST, VERITAS)

Expect to see large variations in the high energy NT emission with phase

## **Further details:**

Pittard & Dougherty (2006, MNRAS, 372, 801)