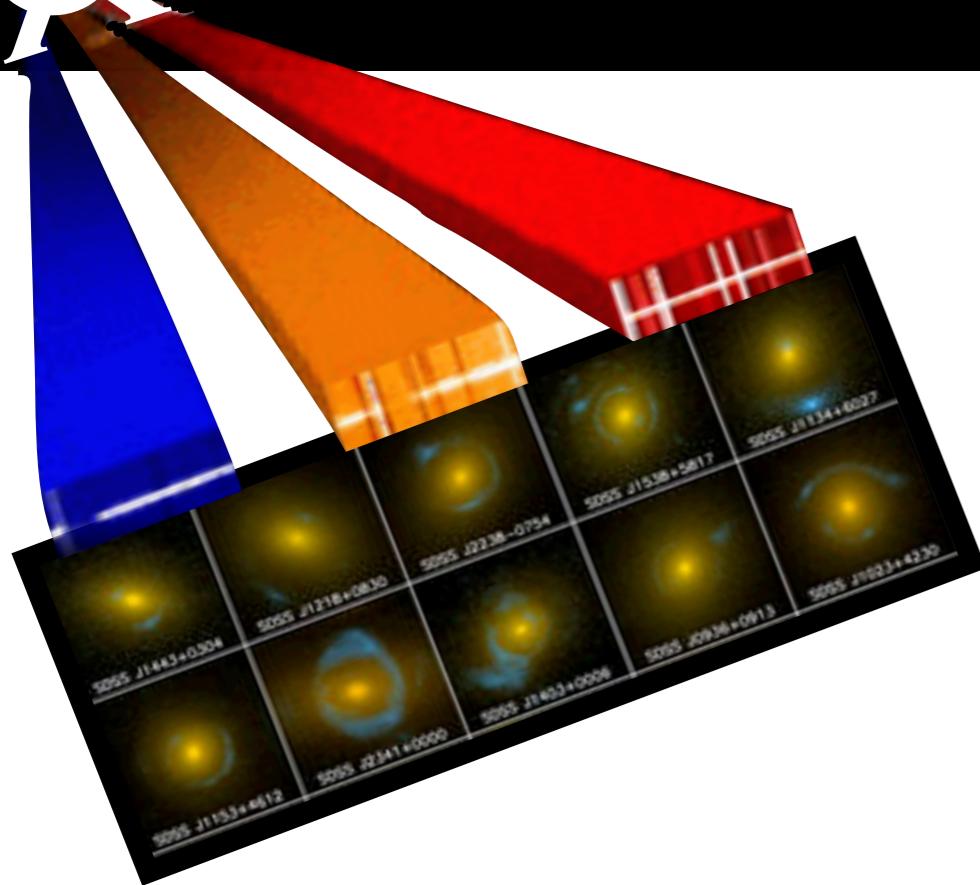


# Combined **Algorithm** for **Unified** **Lensing** and **Dynamics** **Reconstructi**ON****



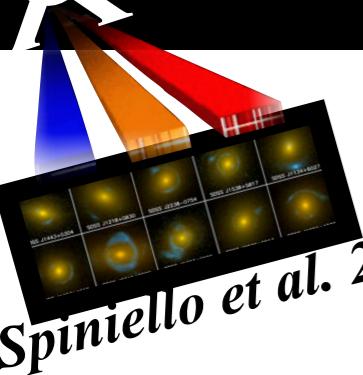
Strong lensing & Dynamics + Stellar population  
Constraining the Initial Mass Function  
and its lower cutoff mass

*Chiara Spinello*

M. Barnabè, L.V.E. Koopmans, S.C. Trager, T.Treu, O.Czoske



Kapteyn Astronomical Institute  
University of Groningen (NL)



Spiniello et al. 2011

## WHAT?

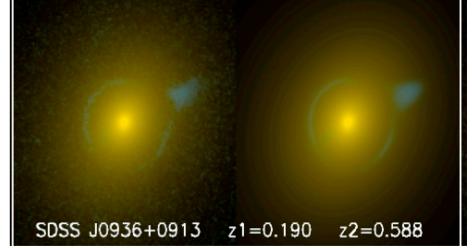
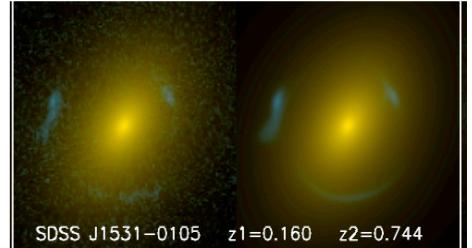
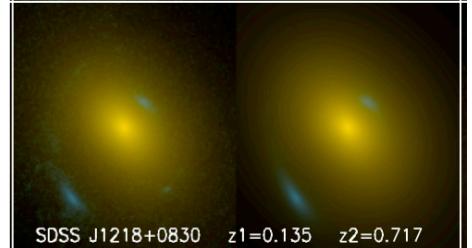
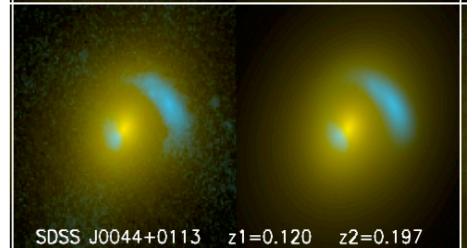
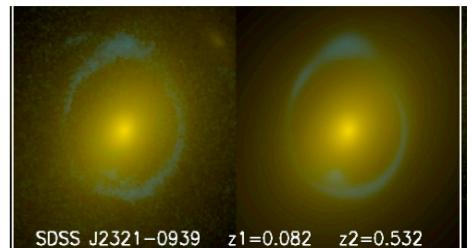
- ▶ ETGs  $z \sim [0.1-0.4]$  ,  $\sigma^* > 250$  km/s
- ▶ Strong gravitational lensing+ dynamics (CAULDRON)  
+ spatially resolved kinematics (XSH)
- ▶ Stellar population analysis (SSP modelling, line-strengths)

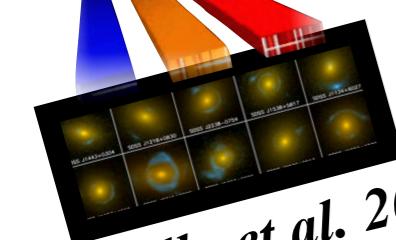
## SCIENTIFIC GOALS:

- ▶ Disentangle stellar and dark-matter content
- ▶ Mass distribution as function of galaxy mass and redshift
- ▶ Slope and lower cutoff mass of the  
Initial Mass Function (IMF) directly from spectra



Barnabè et al. 2012





Spiniello et al. 2011

## THE METHOD



Barnabè et al. 2012

We infer stellar masses from two  
independent methods:

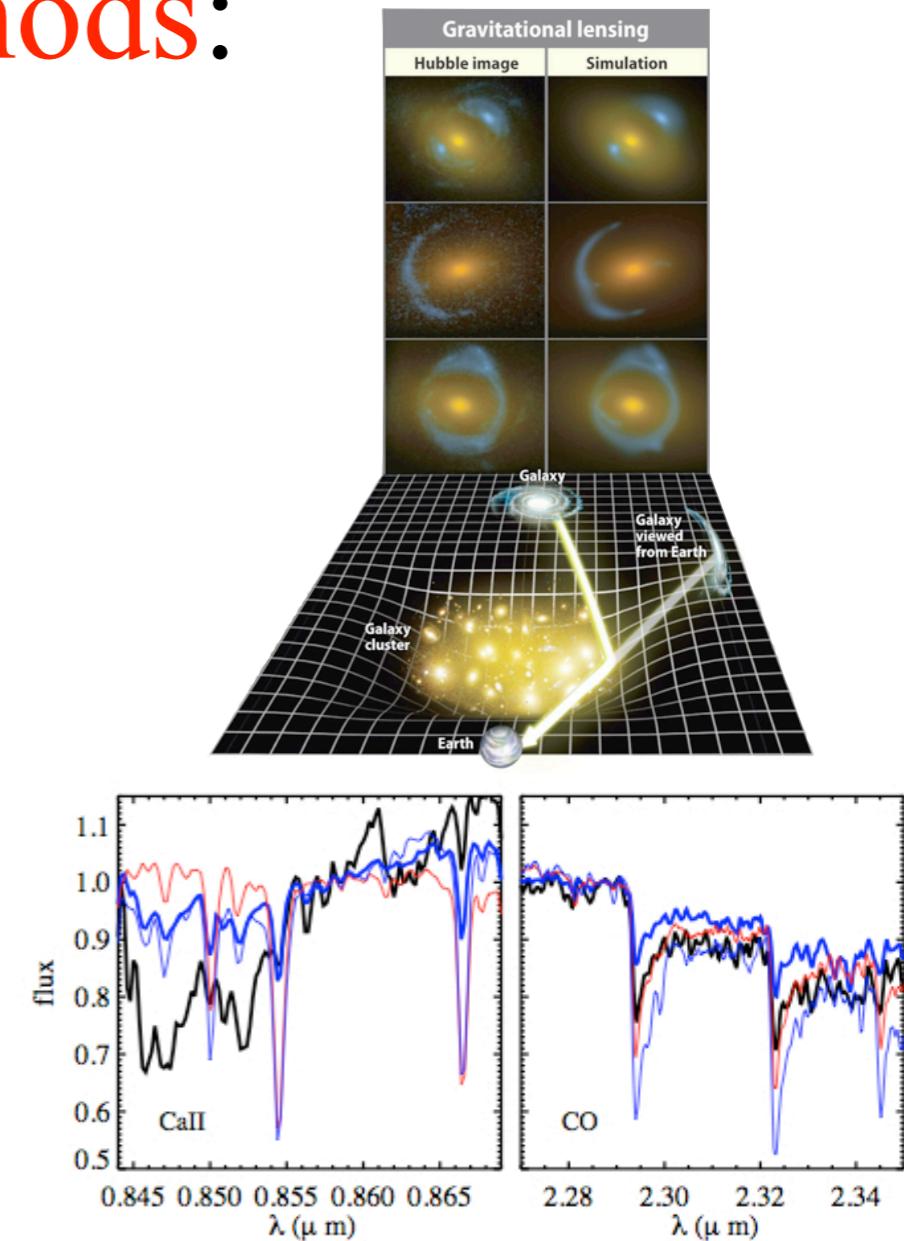
- 1. Joint self-consistent lensing  
+ dynamics analysis *Barnabè et al. 2012*

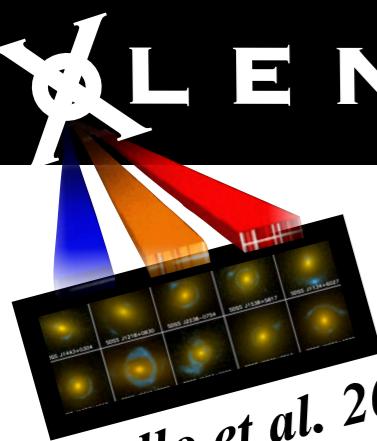
Tracing the mass

- 2. Spectroscopic Simple  
Stellar Population study

*Spiniello et al. 2013*

Tracing the light





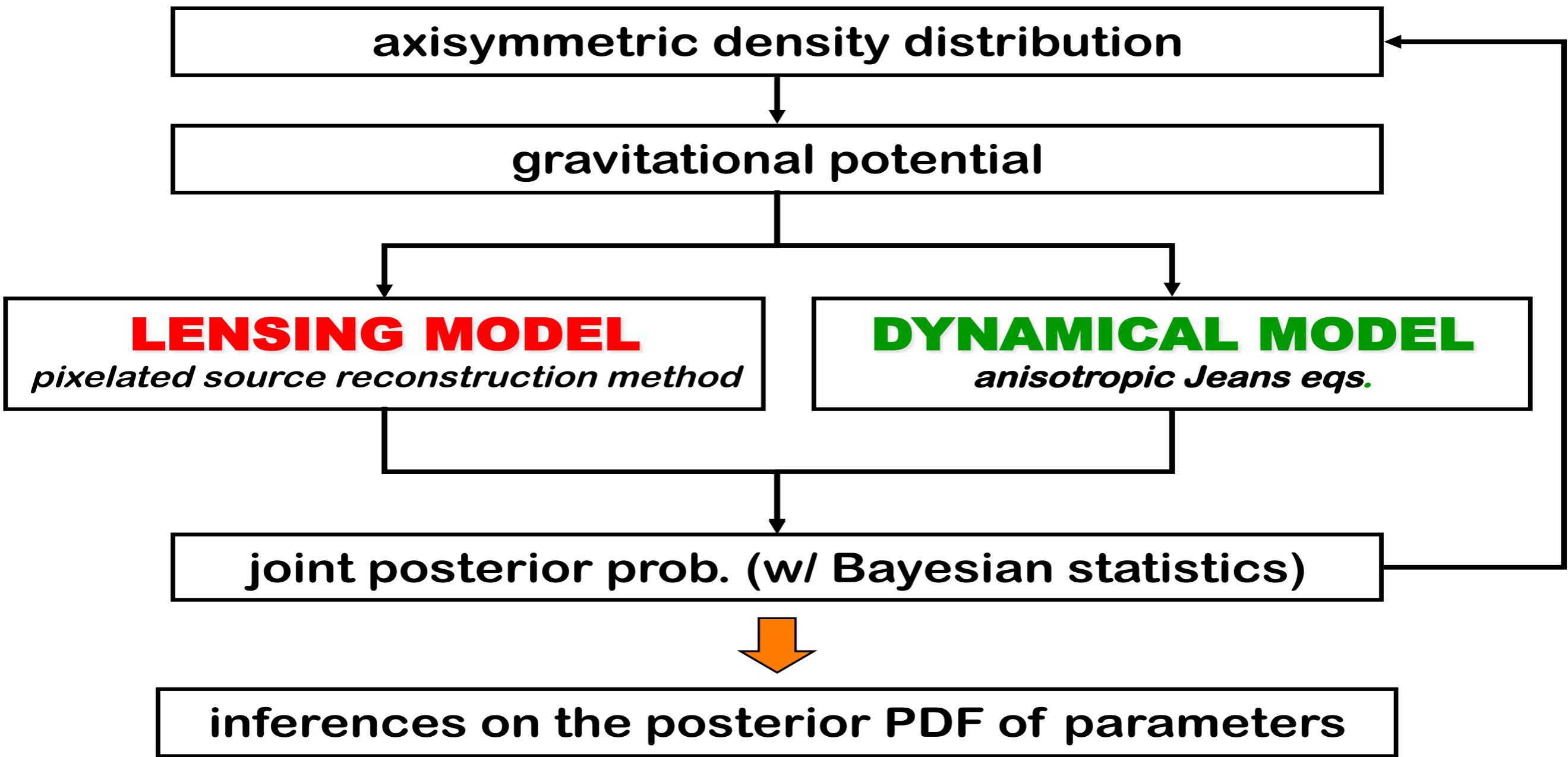
Spiniello et al. 2011

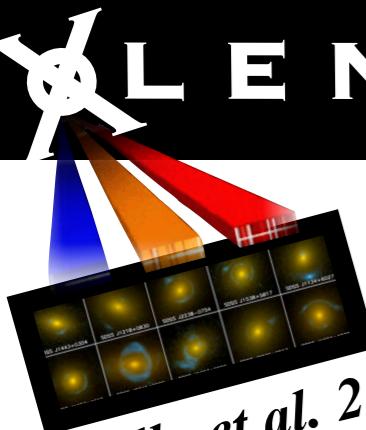
**THE METHOD 1.**  
**CAULDRON: COMBINED LENSING  
AND DYNAMICS ANALYSIS**

*Barnabè et al. 2012*



*Barnabè et al. 2012*





Spiniello et al. 2011



Barnabè et al. 2012

## DARK MATTER : Axisymmetric generalized NFW profile

$$\rho_{\text{DM}}(m) = \frac{\delta_c \rho_{\text{crit}}}{(m/r_s)^\gamma (1 + m/r_s)^{3-\gamma}}$$

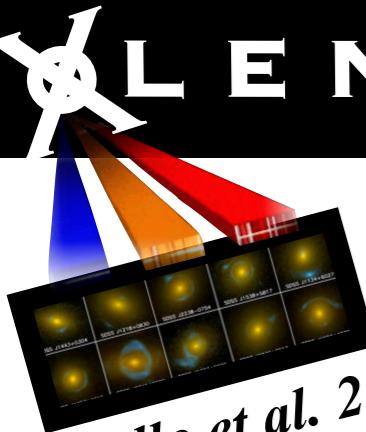
$$m^2 \equiv R^2 + \frac{z^2}{q_h^2} \quad \delta_c = \frac{200}{3} \frac{c^3}{\zeta(c, \gamma, 1)}$$

- Free parameters [#1-4]: **inner slope**  $\gamma$ , **three-dimensional axial ratio**  $q_h$ , **concentration**  $c$ , **virial velocity**  $v_{\text{vir}}$

## LUMINOUS MATTER : Decompose and de-project the galaxy high-res image in K-band using the *multi-Gaussian expansion (MGE) technique*

(by Emsellem et al. 99, Cappellari 2002)

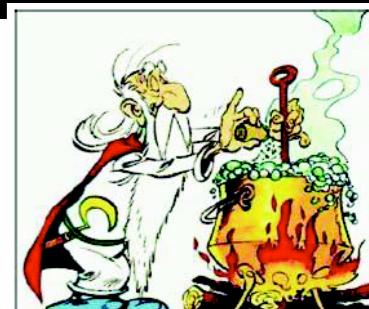
- Luminous mass distribution is self-gravitating, *not just a tracer*
- Free parameter [#5]: **baryonic mass**  $M_{\text{bar}}$



Spiniello et al. 2011

## THE METHOD 2. STELLAR POPULATION ANALYSIS: LINE-INDEX MEASUREMENTS

*Spiniello et al. 2013*



Barnabè et al. 2012

### We Measure indices:

that are more or less sensitive to different stellar population parameters  
(age, α/Fe, gravity, effective Temperature of RGB)

### 1. in the XLENS Galaxy Spectra

Current sample: 12 systems  $z \sim [0.1-0.5]$ ,  $\sigma^* > 250$  km/s

Pilot program : the most massive and the least massive  
XLENS galaxies

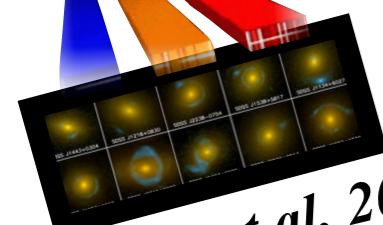
### 2a. in single spectra from the MILES Stellar Library

995 stars spectra ,

Sánchez-Blázquez, et al 2006

Wavelength Range: 3525-7500Å

Resolution: 2.50Å (FWHM)



Spiniello et al. 2011

## THE METHOD 2. STELLAR POPULATION ANALYSIS: LINE-INDEX MEASUREMENTS

Spiniello et al. 2013

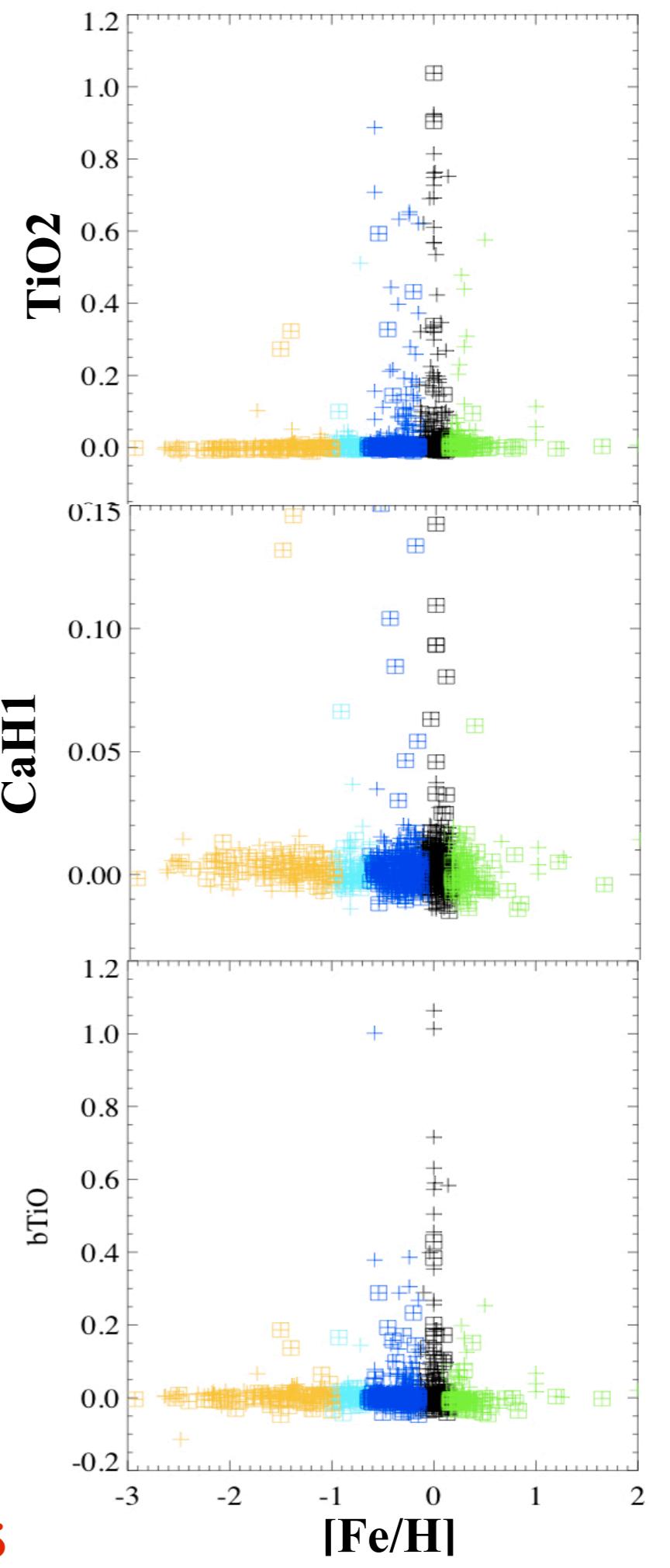
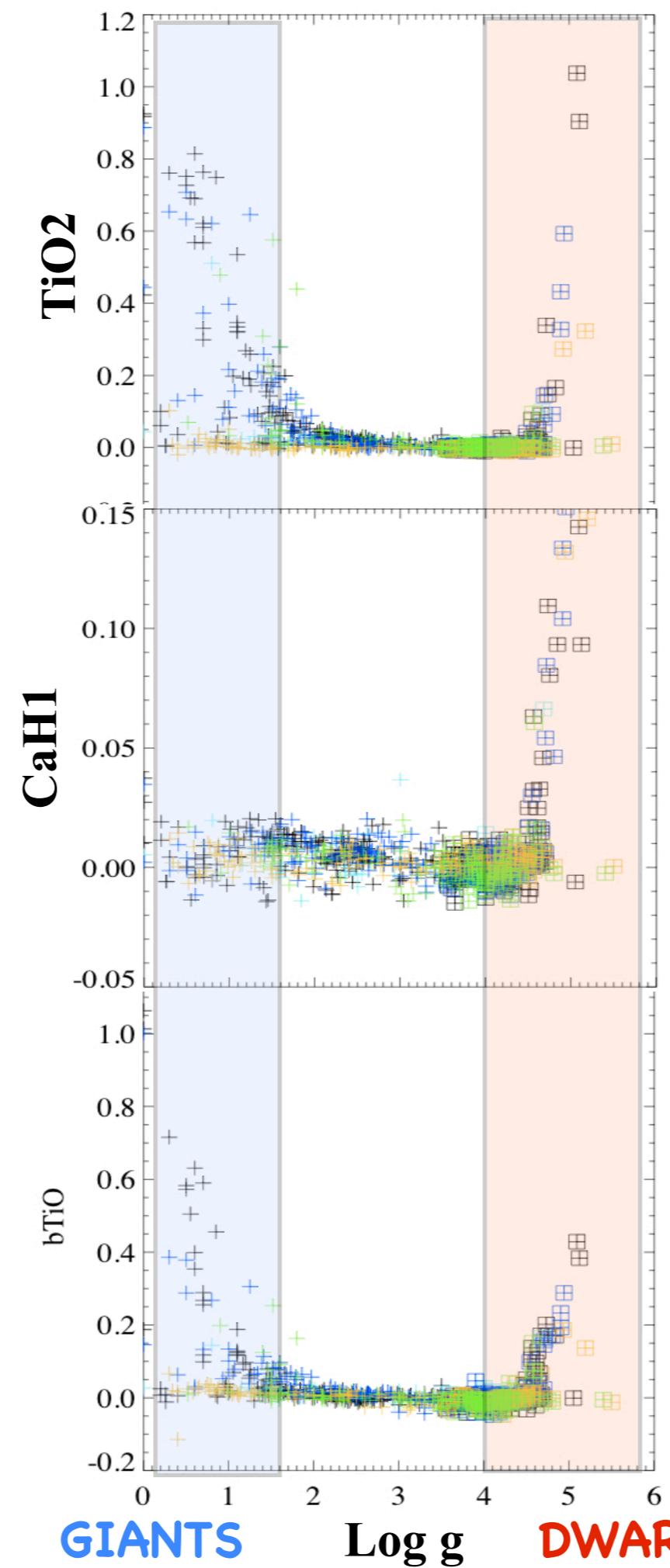
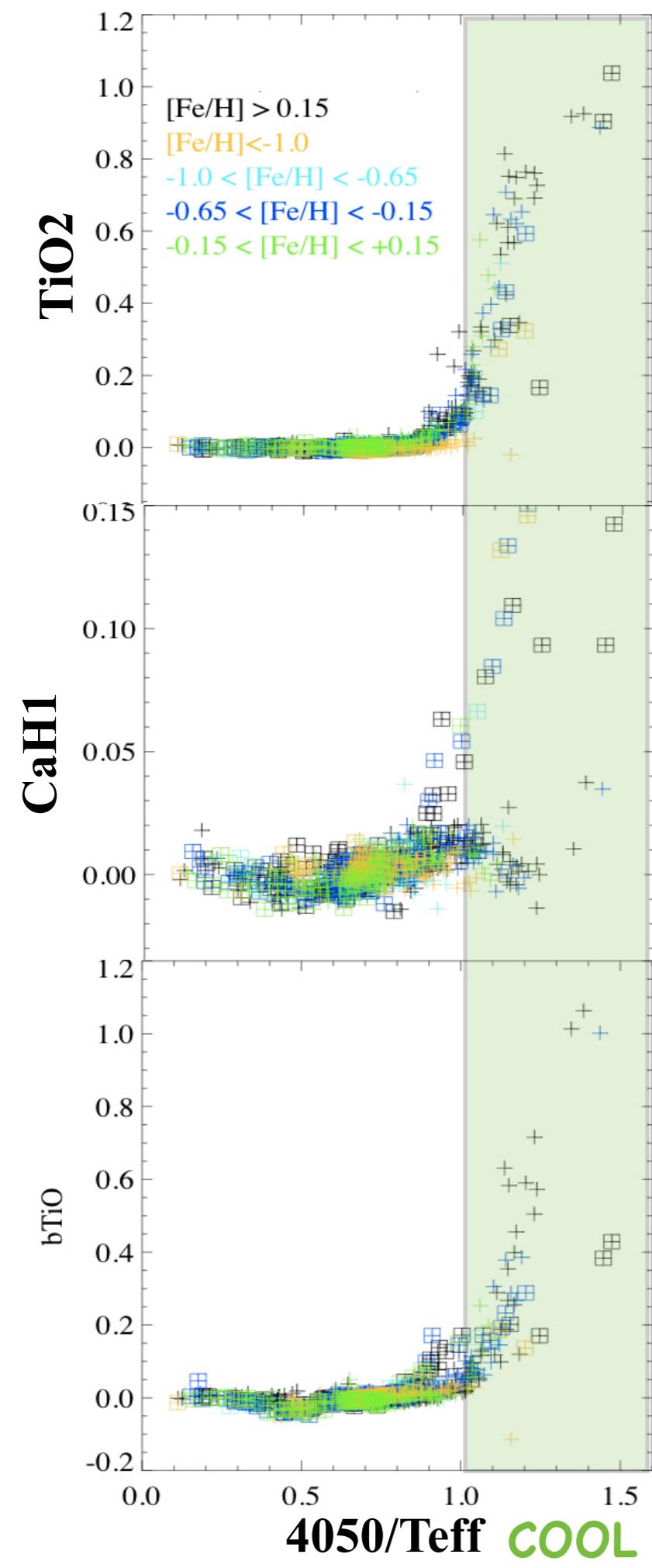


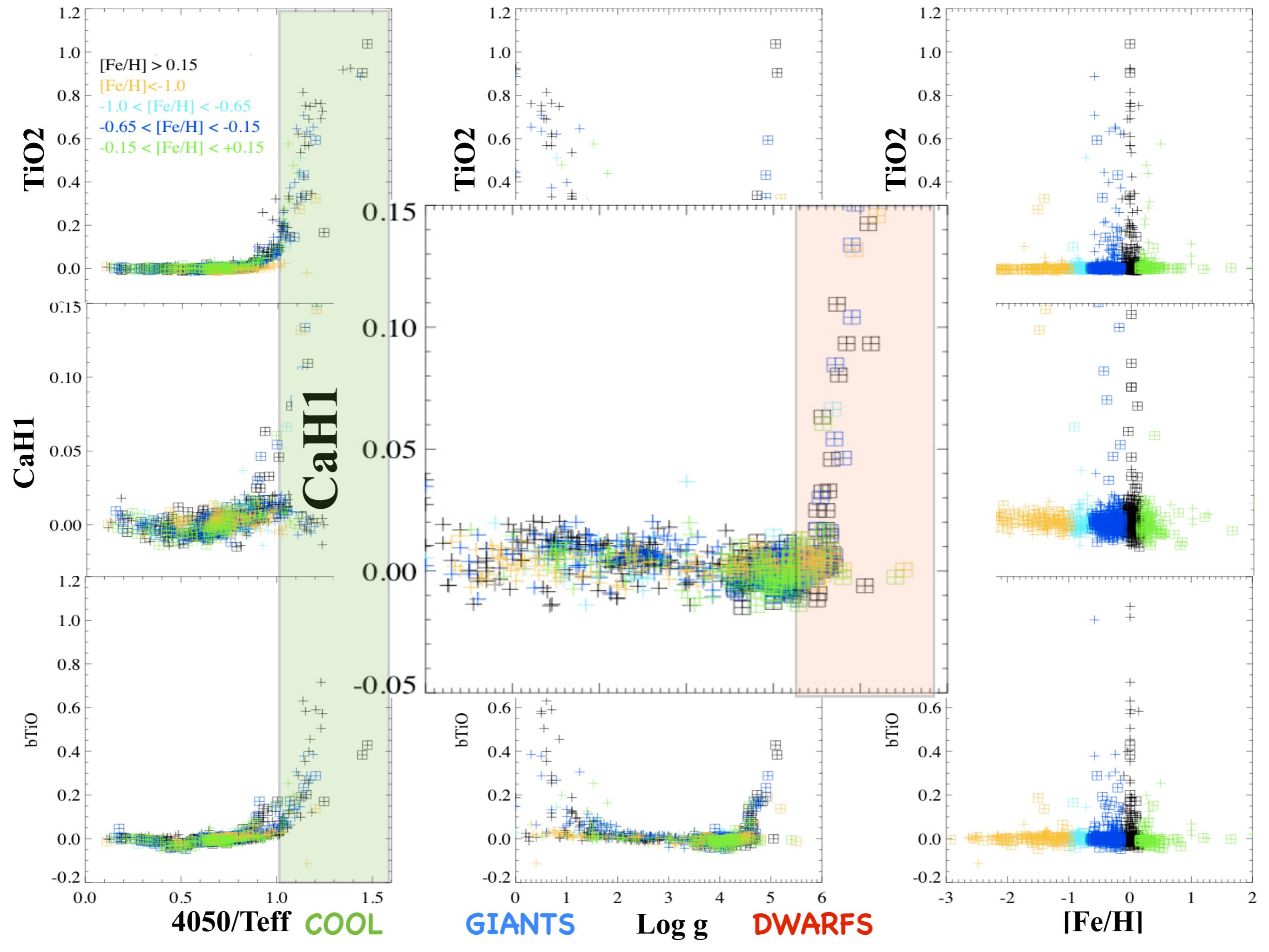
Barnabè et al. 2012

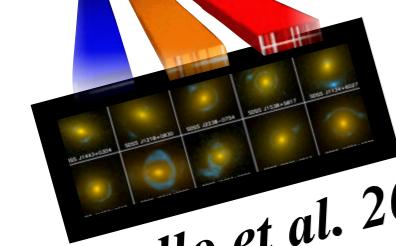
### Searching for (new) M-dwarfs indicators in the optical

Searching for indicators that :

- are strong in COOL STARS
- are GRAVITY-SENSITIVE
- do not depend strongly on metallicity and age  
(at least for population older than 7Gyr)







Spiniello et al. 2011

## THE METHOD 2. STELLAR POPULATION ANALYSIS: LINE-INDEX MEASUREMENTS

*Spiniello et al. 2013*



Barnabè et al. 2012

### We Measure indices:

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Pilot program : the most massive and the least massive  
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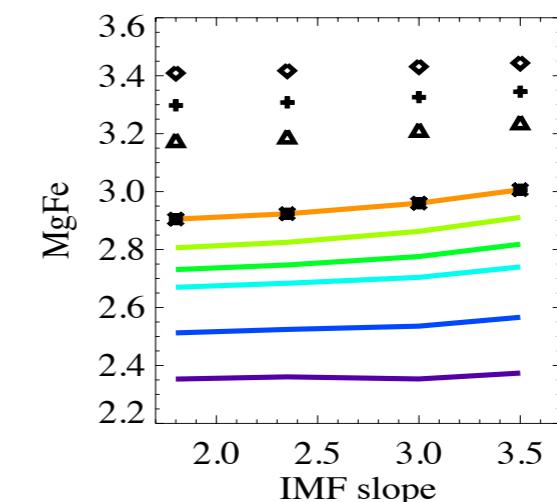
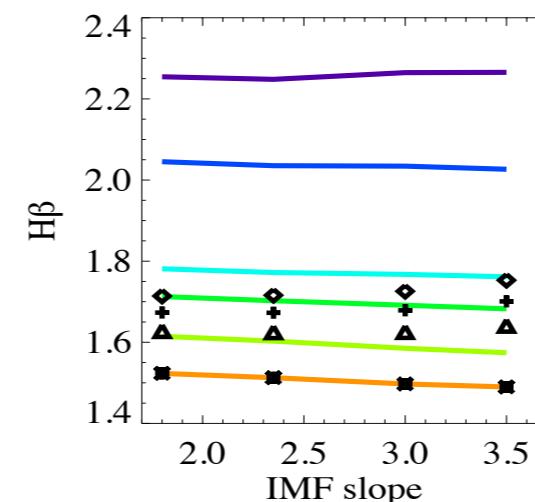
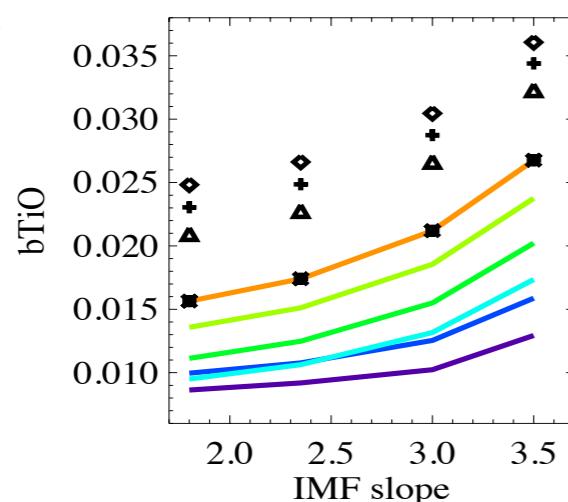
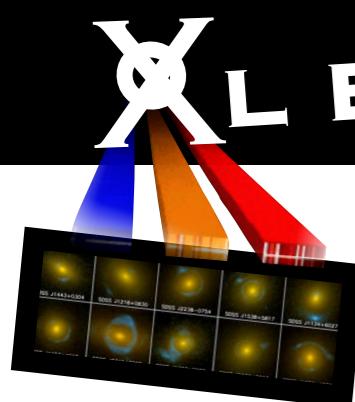
### 2b. in the CvD+12 Simple Stellar Population Models

Ages: {3-13.5}Gyr ,

$[\alpha/\text{Fe}]$  : {-0.2 - 0.4},

IMF slopes: {1.8 - 3.5} (Salp=2.35)

# X L E N S + Combined Algorithm for Unified Lensing and Dynamics Reconstruction



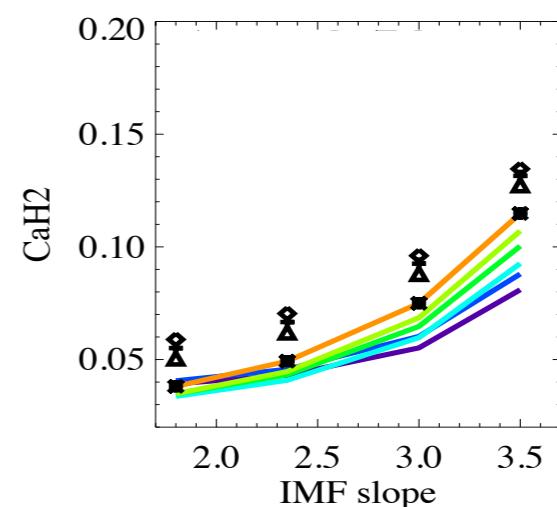
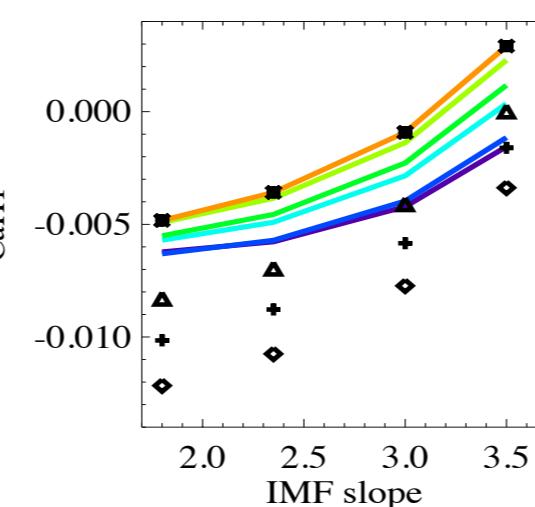
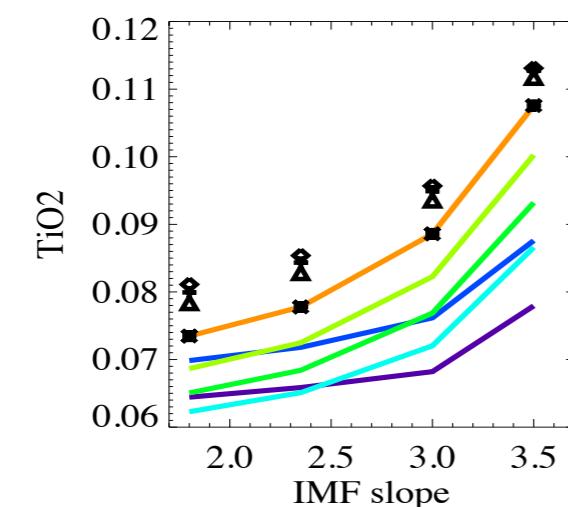
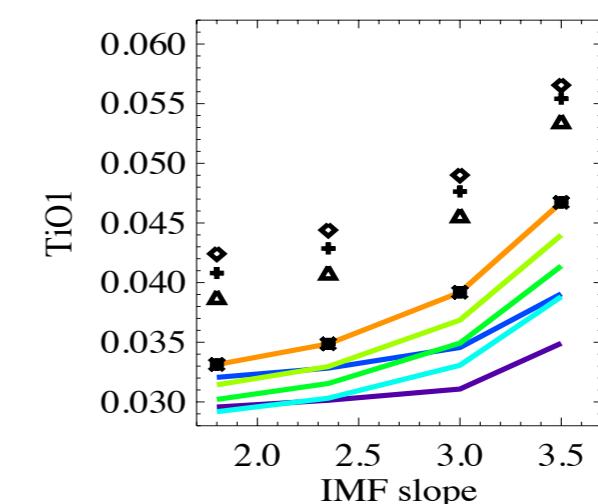
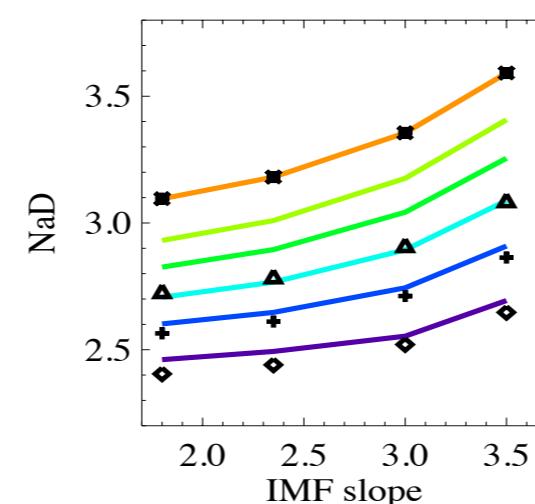
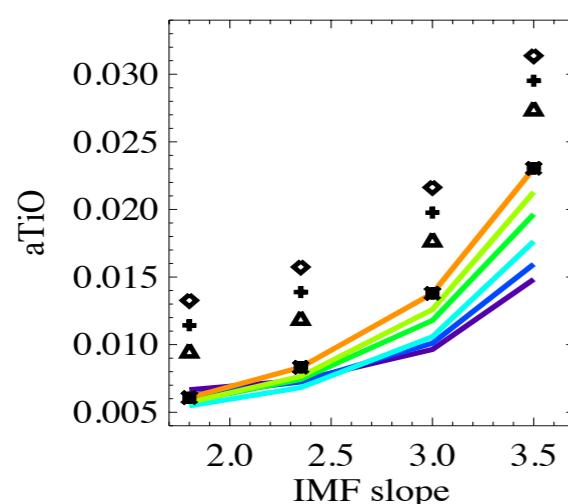
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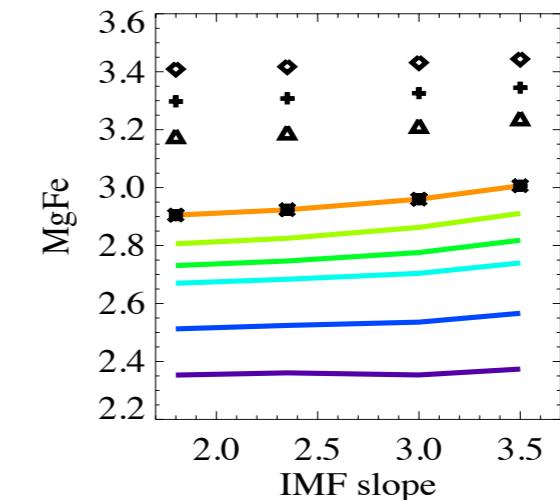
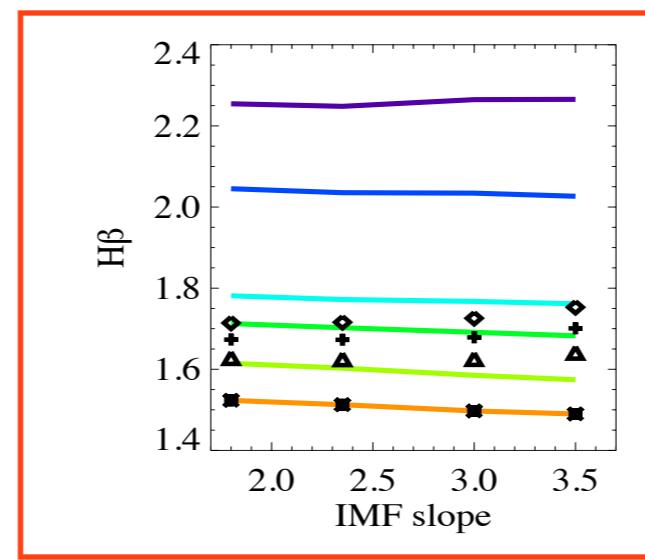
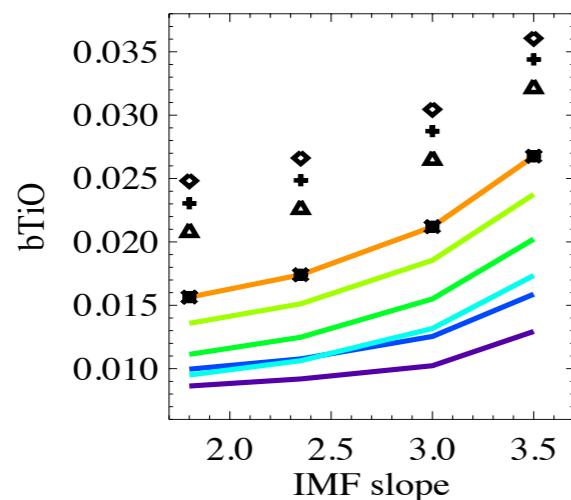
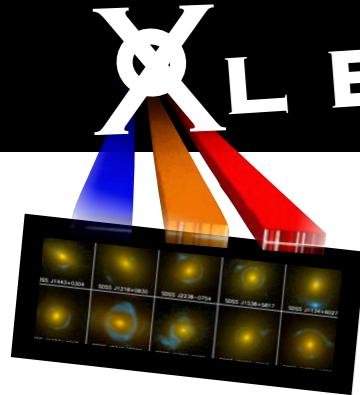
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Spiniello  
et al. 2013



# X L E N S + Combined Algorithm for Unified Lensing and Dynamics Reconstruction

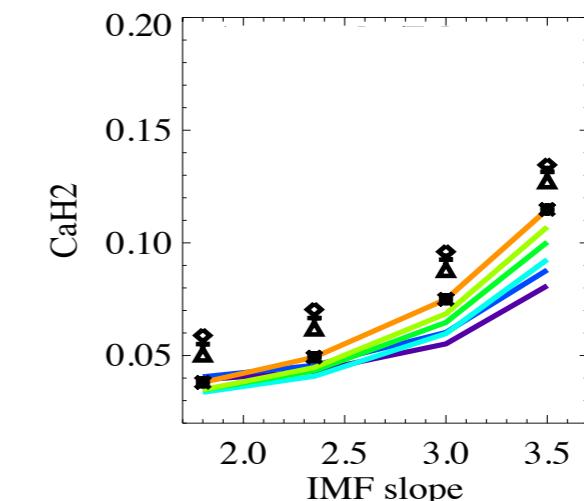
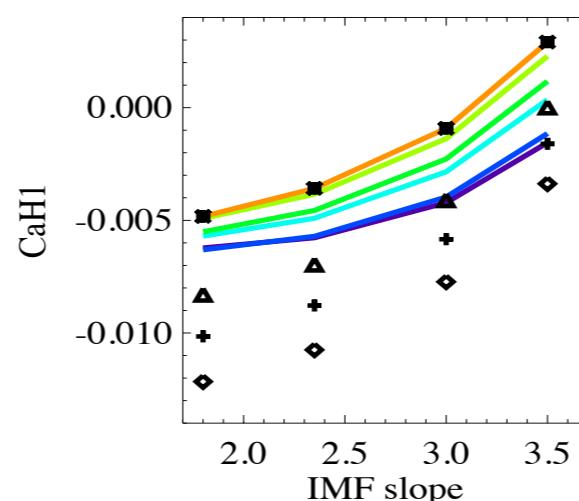
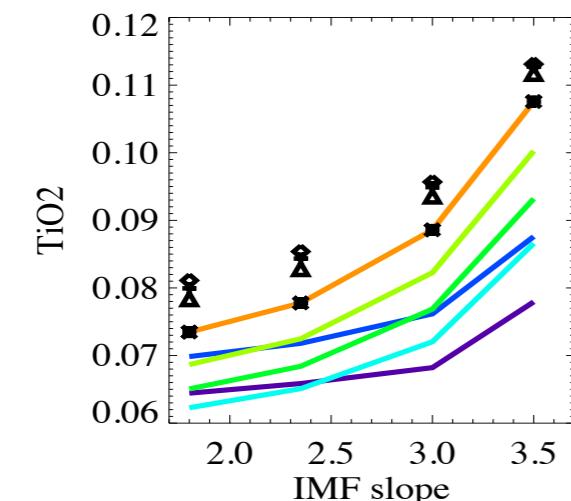
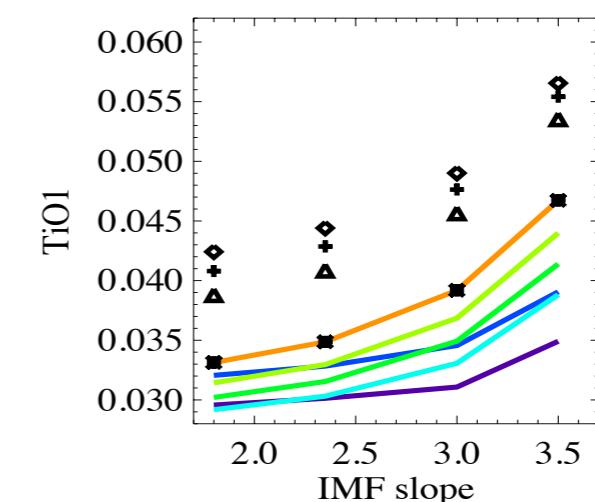
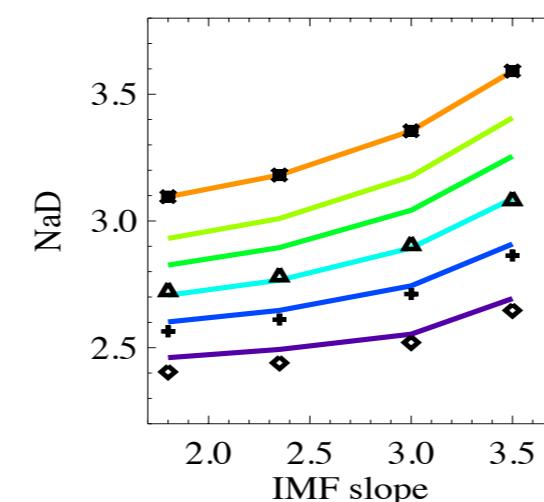
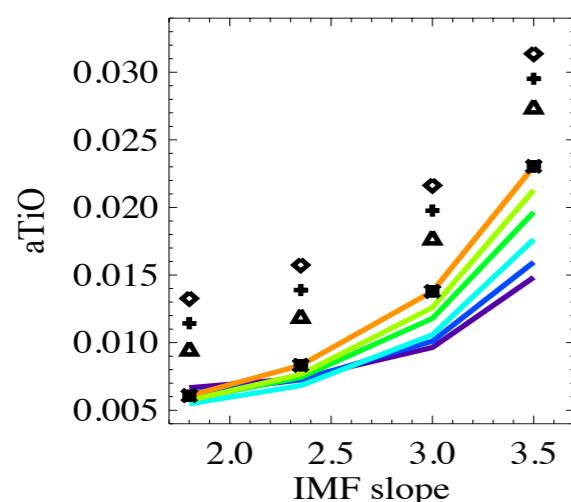


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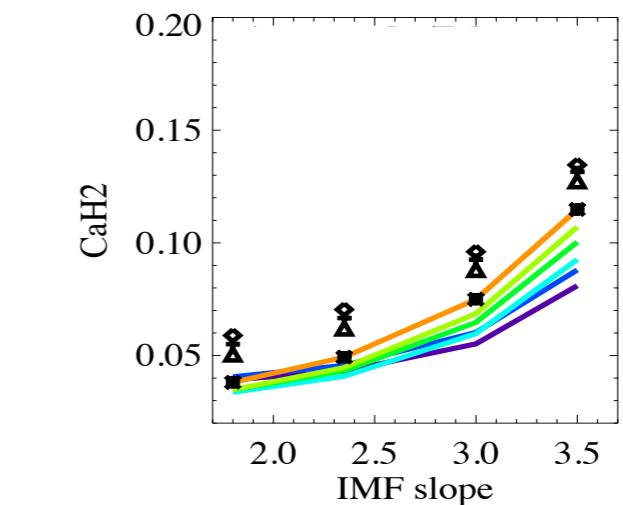
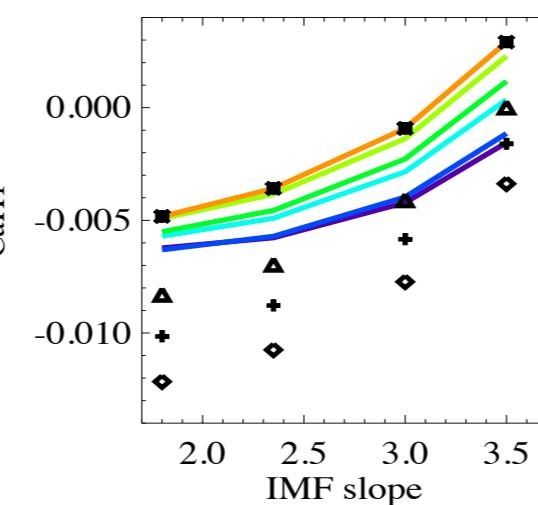
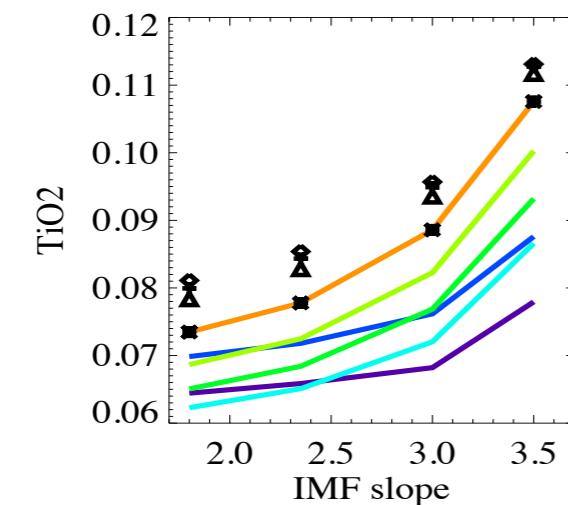
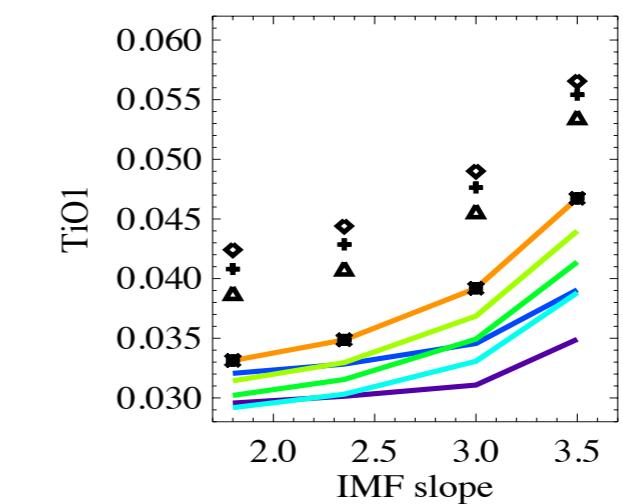
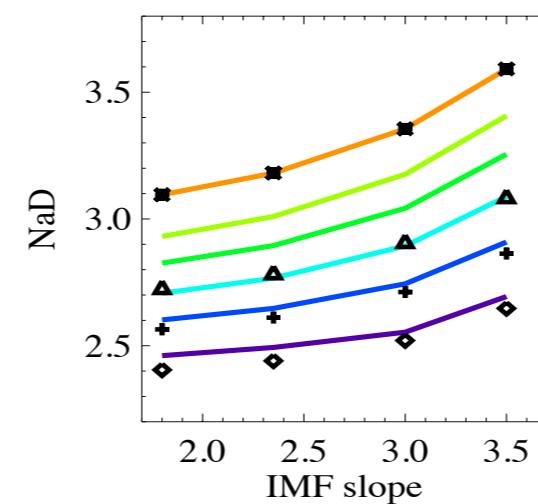
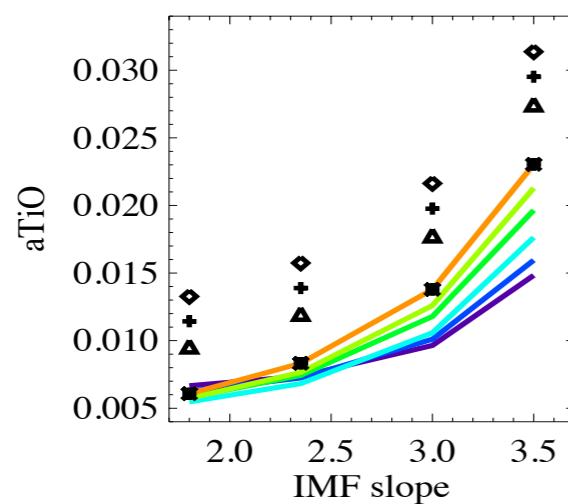
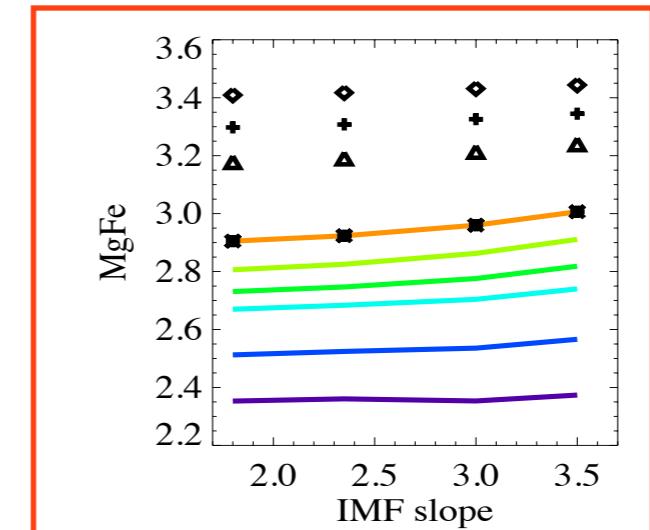
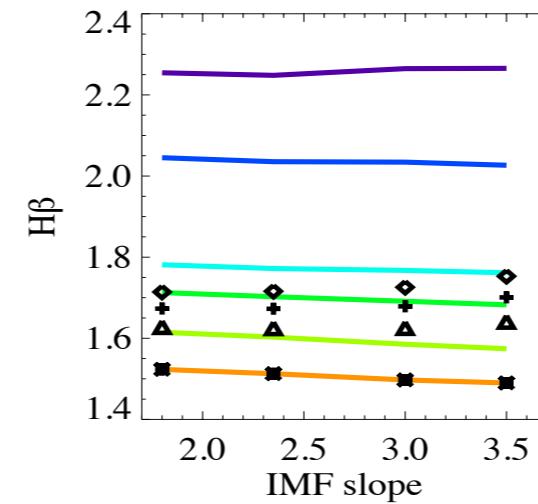
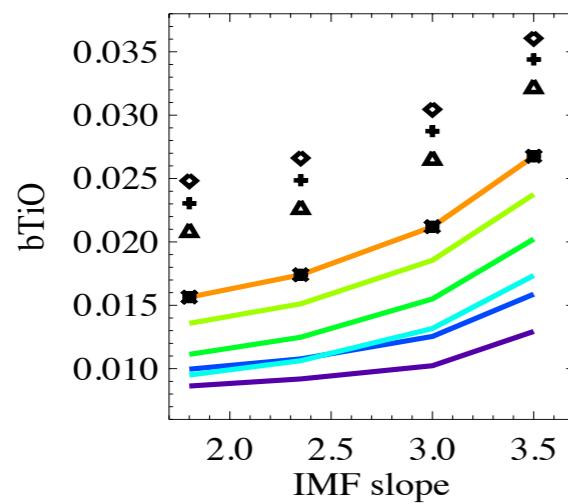
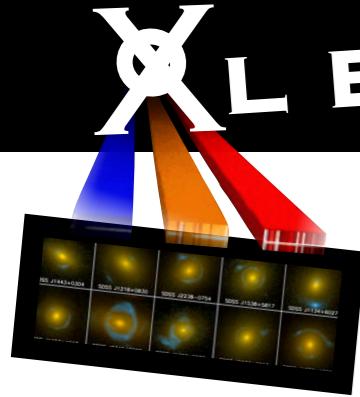
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# X L E N S + Combined Algorithm for Unified Lensing and Dynamics Reconstruction



Ages

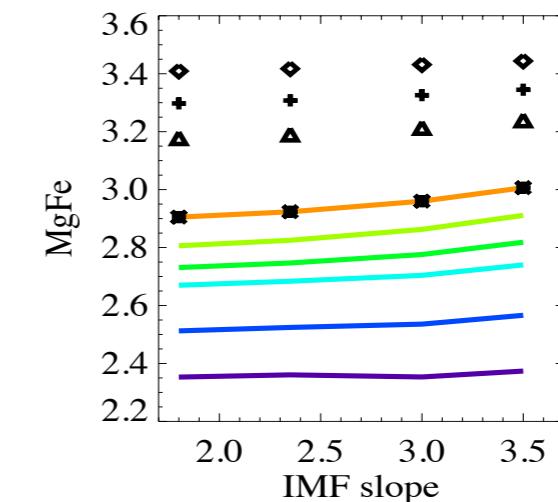
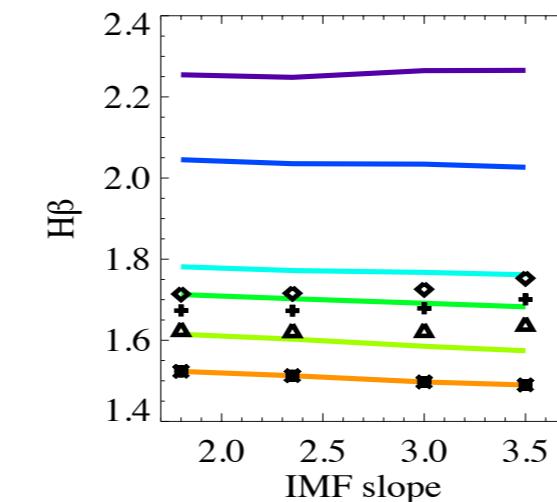
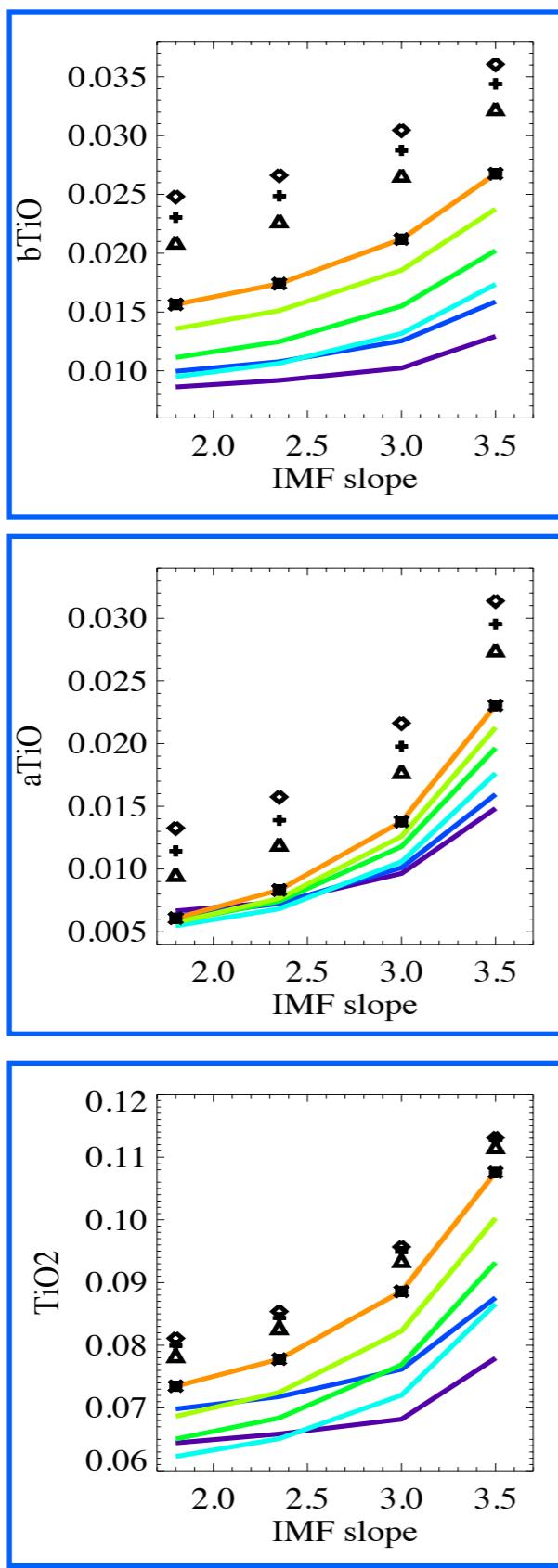
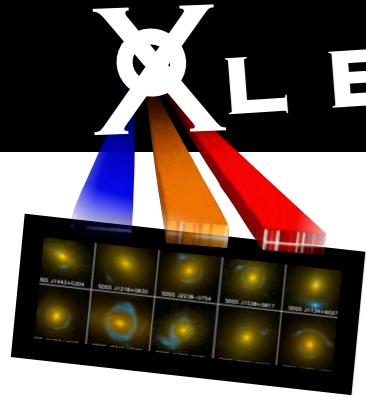
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Spiniello  
et al. 2013

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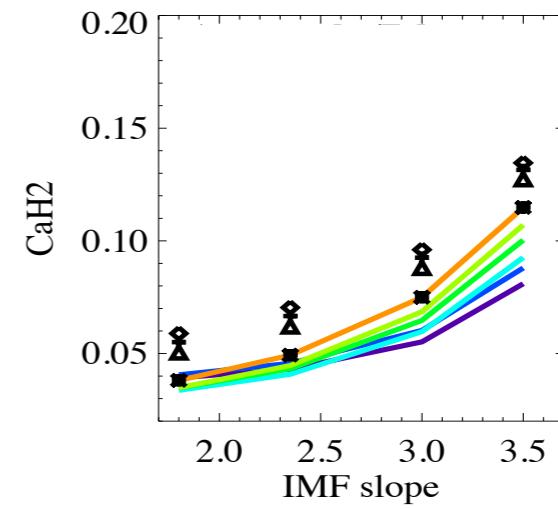
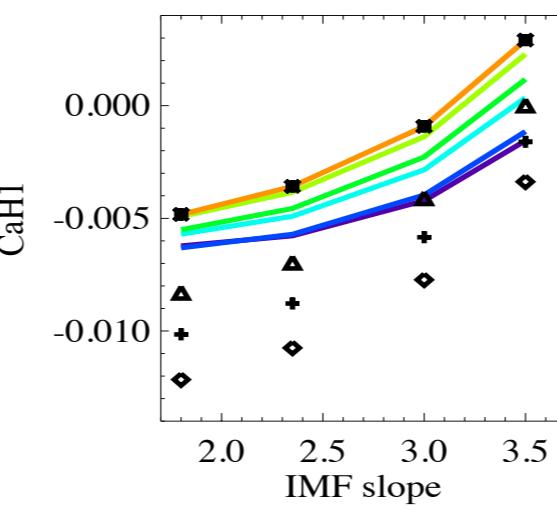
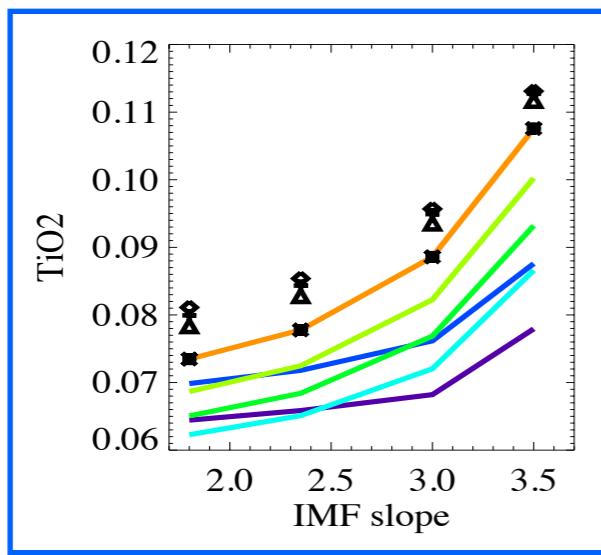
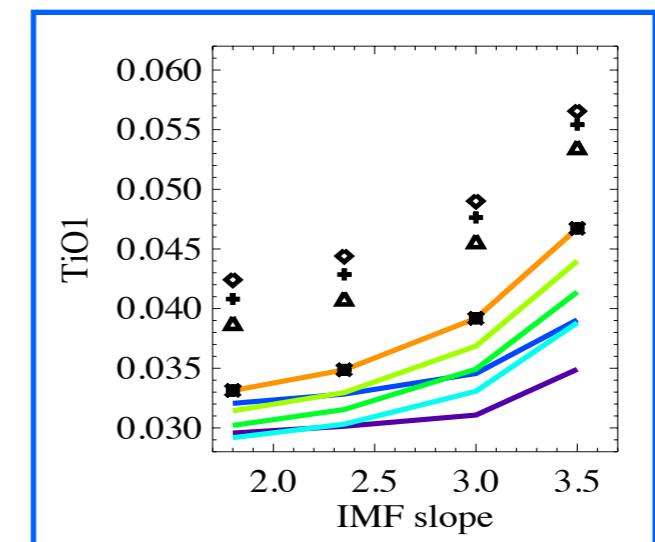
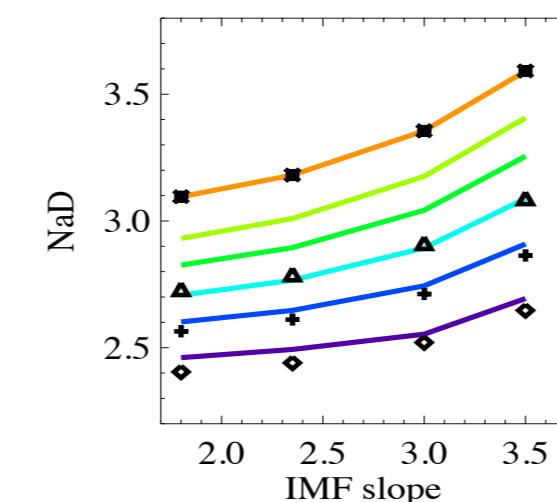
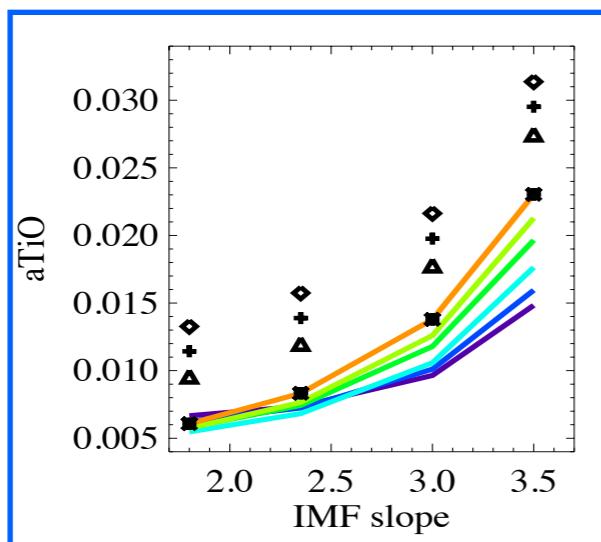


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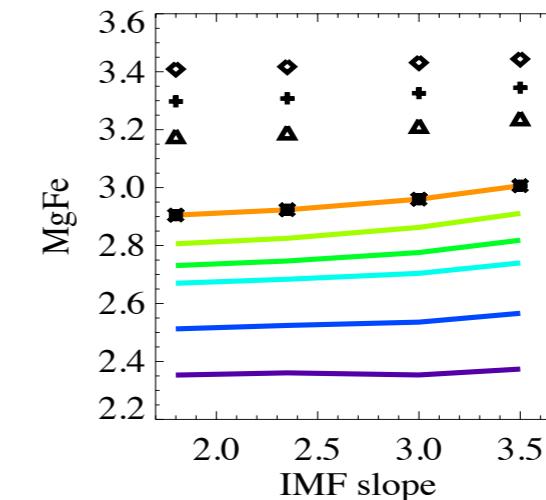
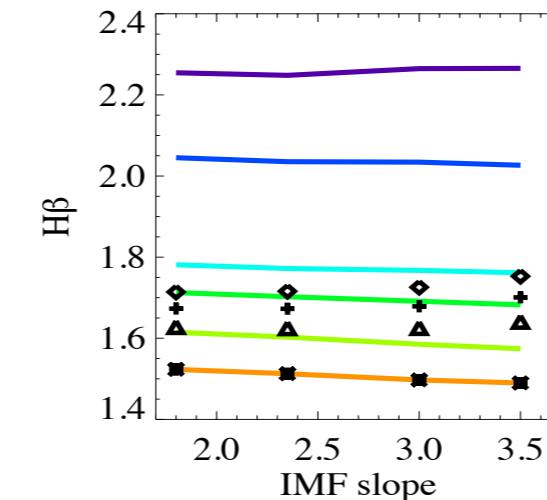
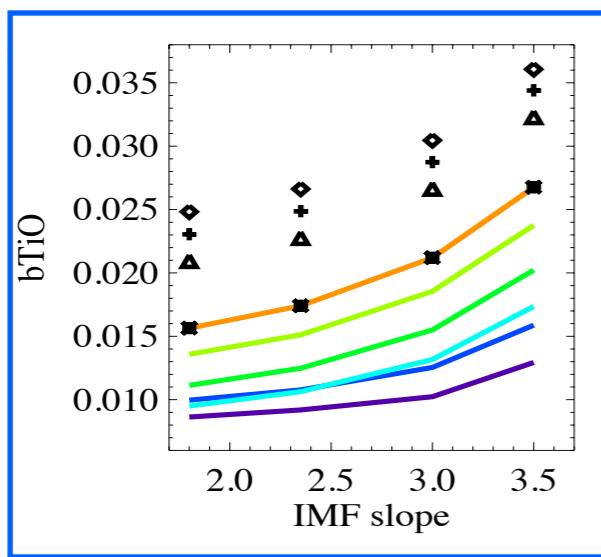
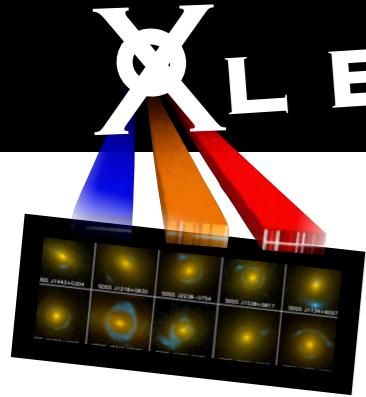
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Spiniello  
et al. 2013

# X L E N S + Combined Algorithm for Unified Lensing and Dynamics Reconstruction

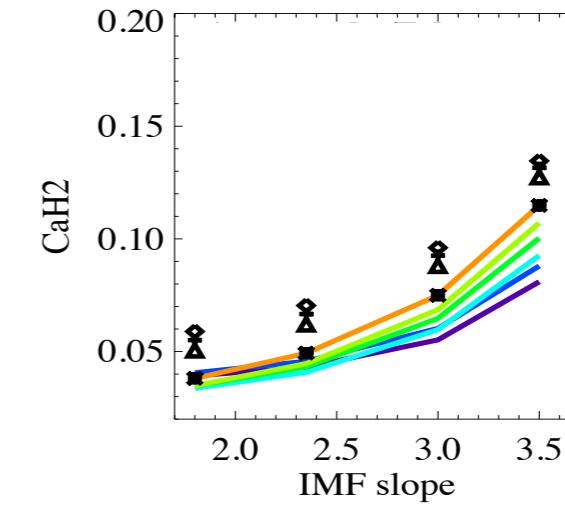
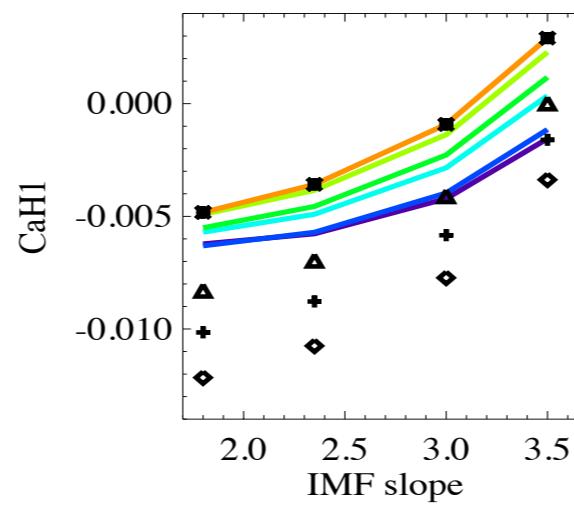
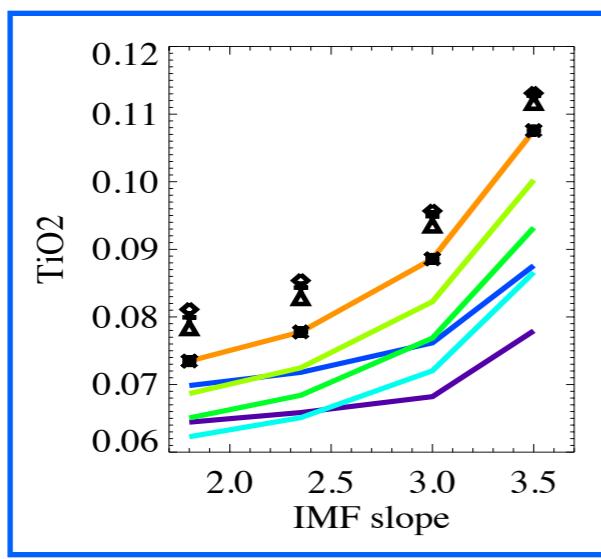
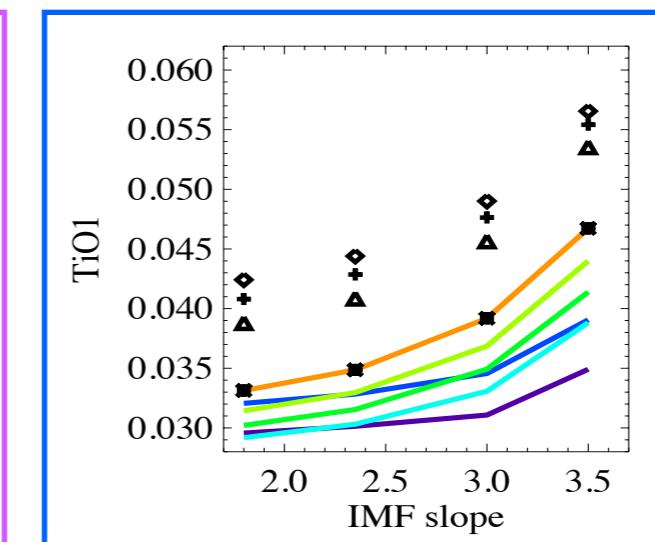
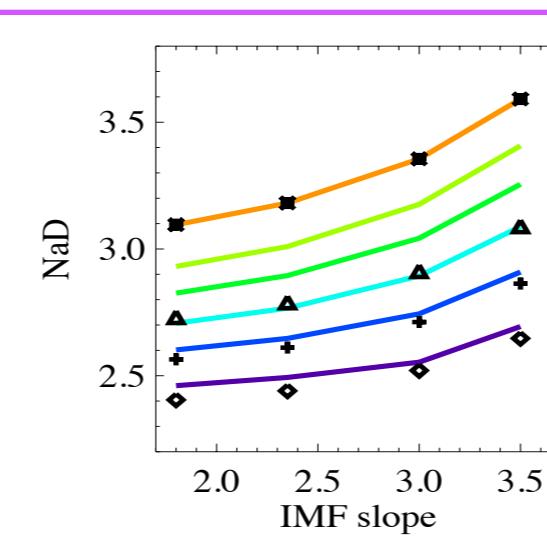
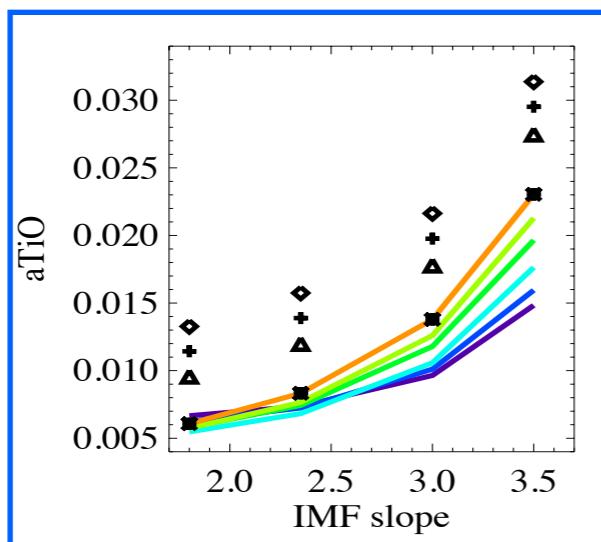


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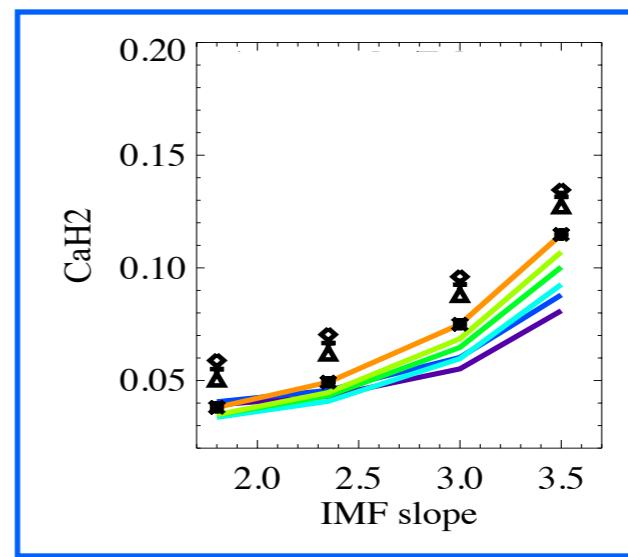
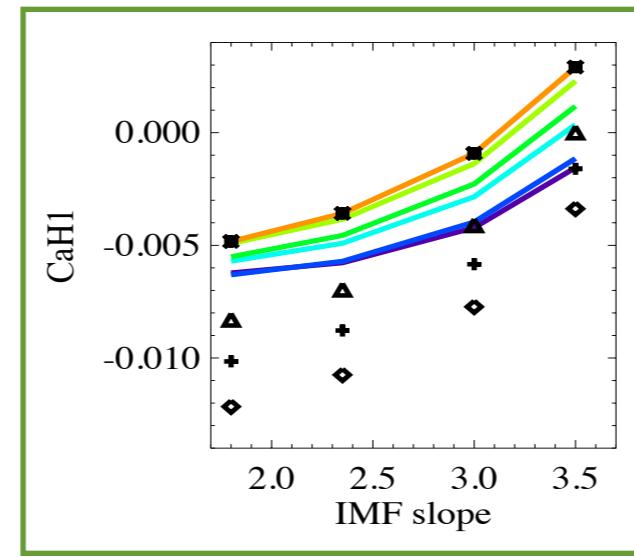
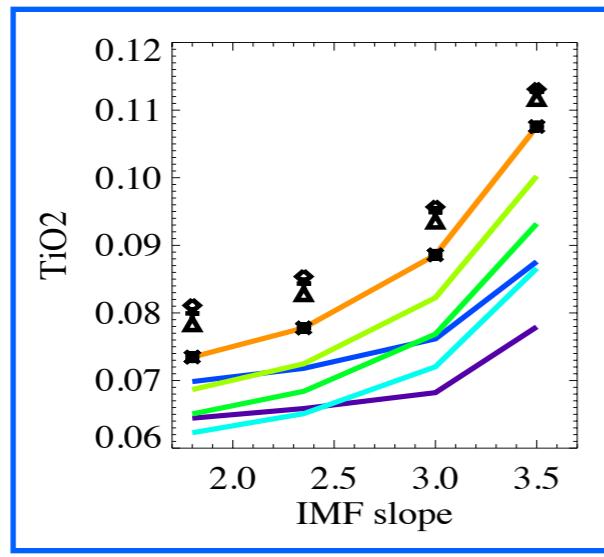
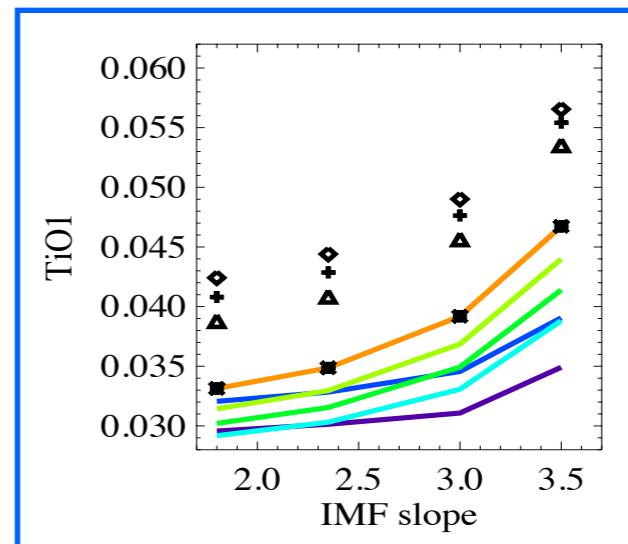
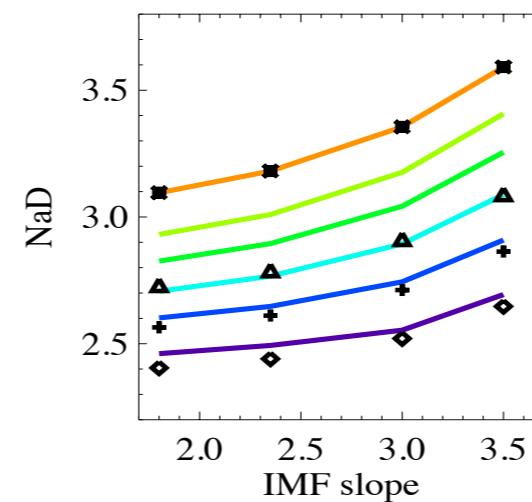
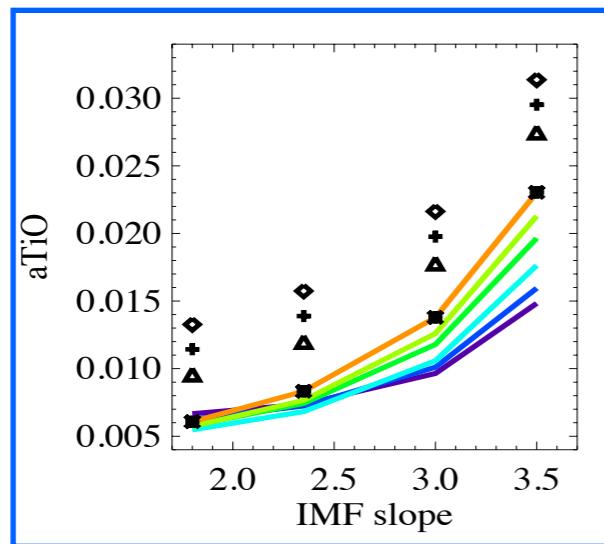
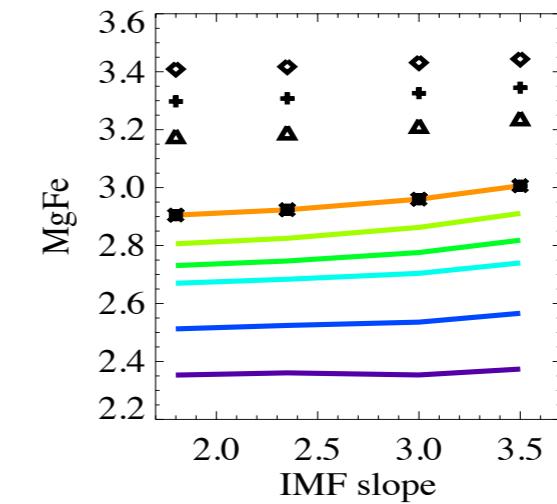
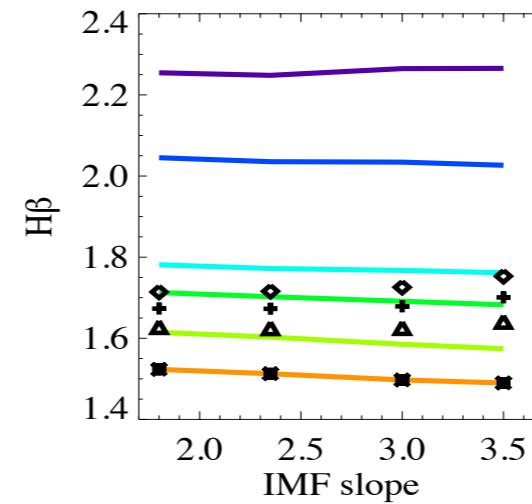
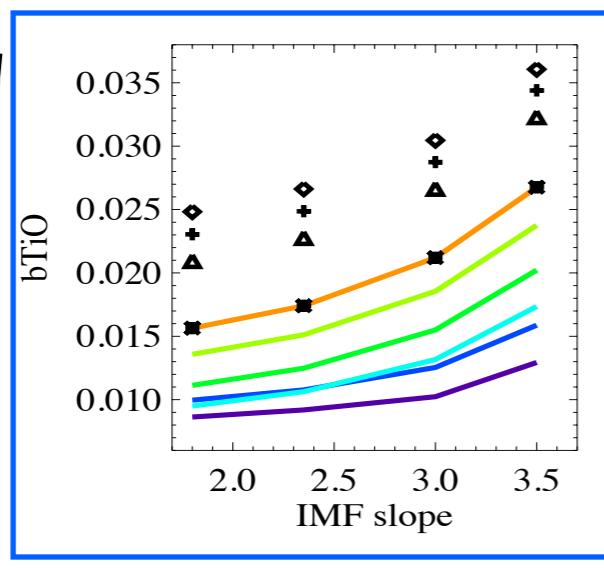
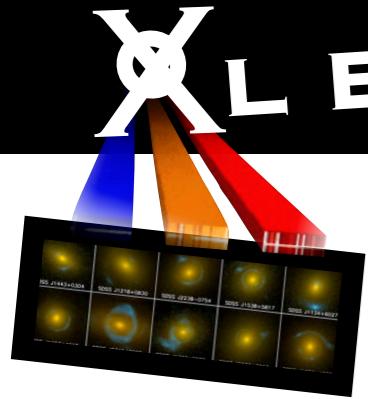
+0.0  
+0.2  
+0.3  
+0.4



Spiniello  
et al. 2013

X L E N S

+ Combined Algorithm for Unified Lensing and Dynamics Reconstruction



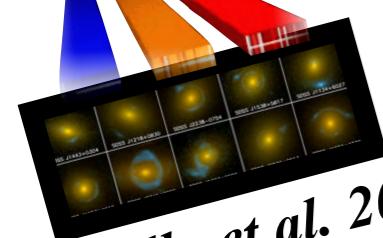
Ages

3.00000  
5.00000  
7.00000  
9.00000  
11.0000  
13.5000

$[\alpha/\text{Fe}]$

+0.0  
+0.2  
+0.3  
+0.4

Spiniello  
et al. 2013



Spiniello et al. 2011

## THE METHOD 2. STELLAR POPULATION ANALYSIS: LINE-INDEX MEASUREMENTS

Spiniello et al. 2013



Barnabè et al. 2012

We measure EWs of several indices :

H $\beta$ , Mgb, Fe5270, Fe5335, bTiO, aTiO, TiO1, TiO2,  
CaH1, CaH2, (and NaD)

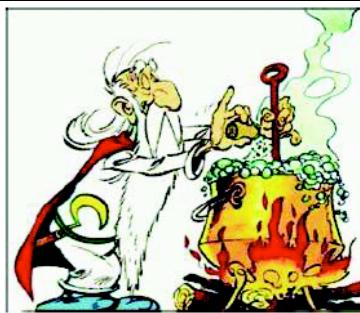
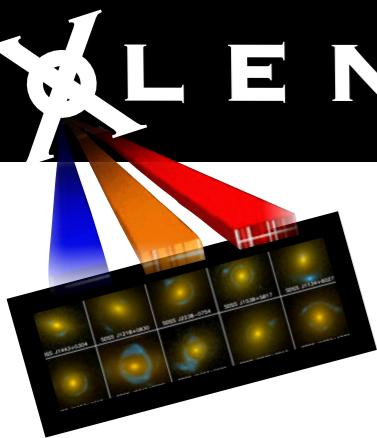
We compare each galaxy spectrum with grids of SSPs models

$8 \log(t)\{0.5 - 1.15\text{Gyr}\} \times 13 [\alpha/\text{Fe}]\{-0.2, +0.4\} \times 18 \text{ IMF}\{1.8, 3.5\} \times 9 \text{ Teff,RGB } \{-200\text{K}, 200\text{K}\}$

Probability density function (PDF)  
via the Likelihood function :

$$L \propto \exp(-\chi^2/2)$$

$$\chi_n^2 = \sum_{ind=1}^{10} \chi_{ind,n}^2 = \sum_{ind=1}^{10} \frac{(EW_{ind} - EW_n)^2}{\sigma_{EW_{ind}}^2}$$

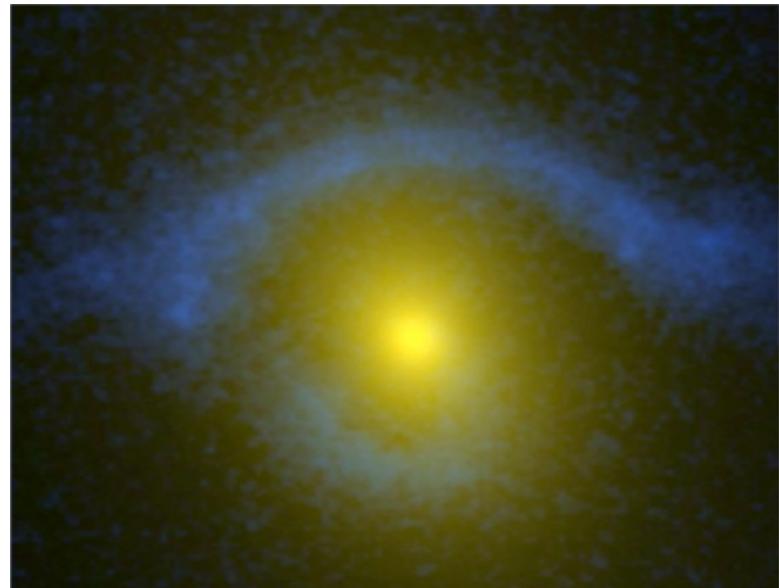


# FIRST RESULTS: A PILOT PROGRAM ON TWO MASSIVE XLENS GALAXIES

*Barnabè, Spiniello et al. 2013*

The most massive:

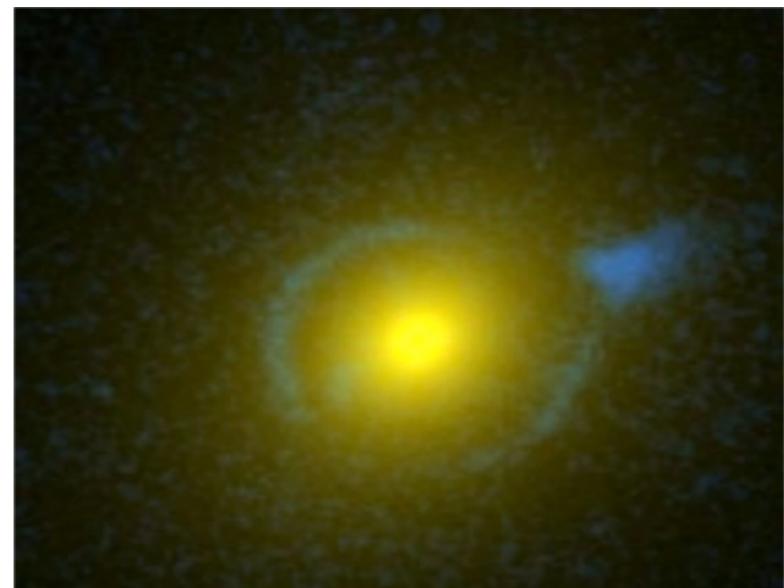
**SDSSJ0912**



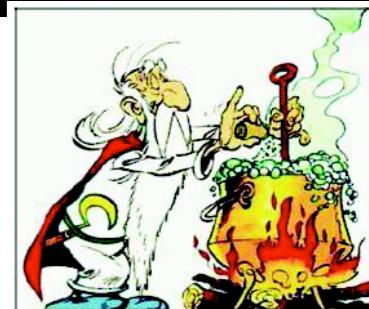
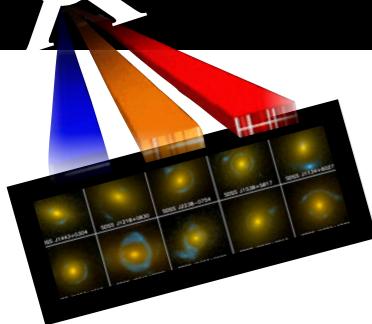
$\sigma \sim 330 \text{ km/s}$

The least massive:

**SDSSJ0936**

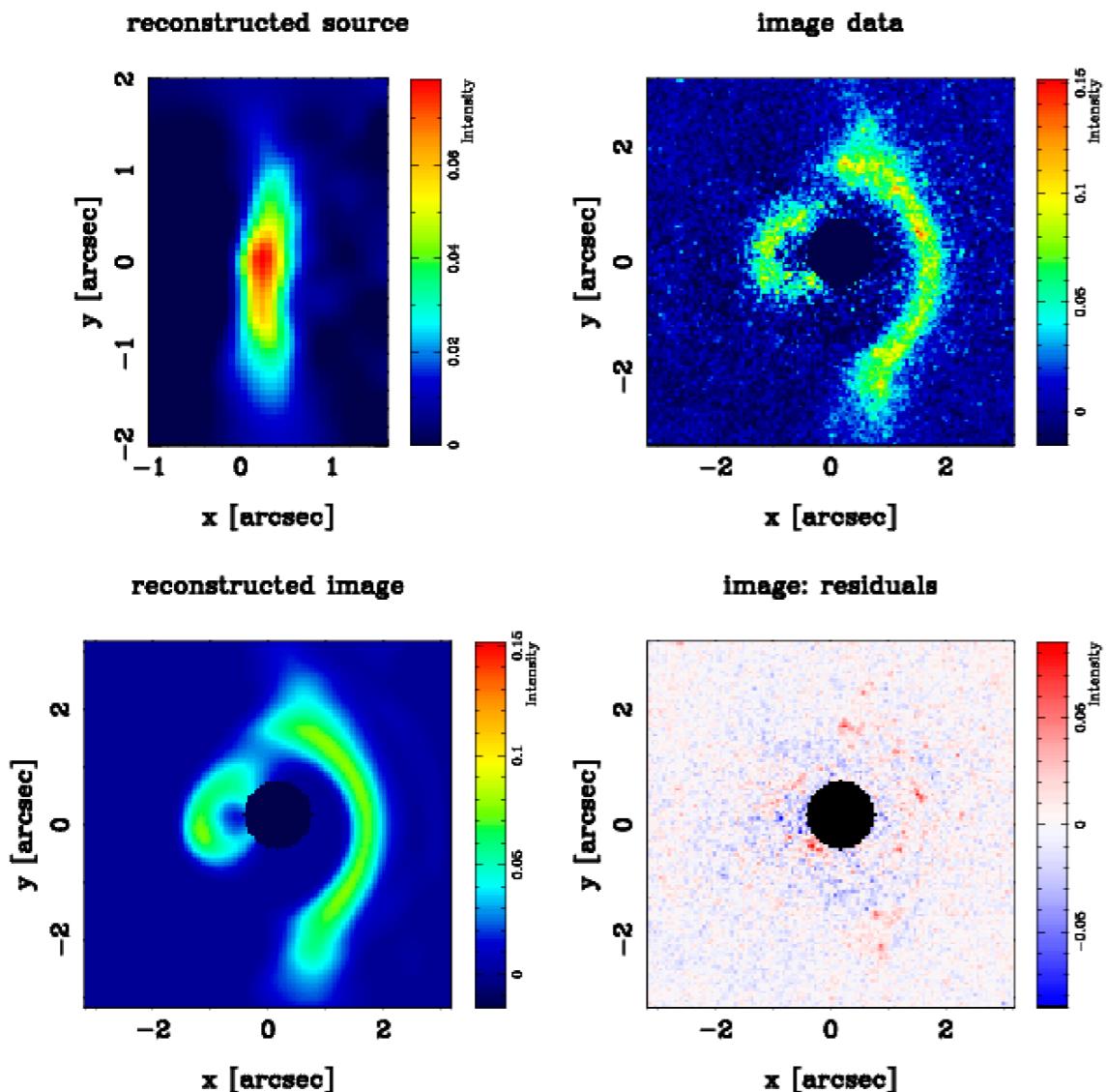


$\sigma \sim 250 \text{ km/s}$

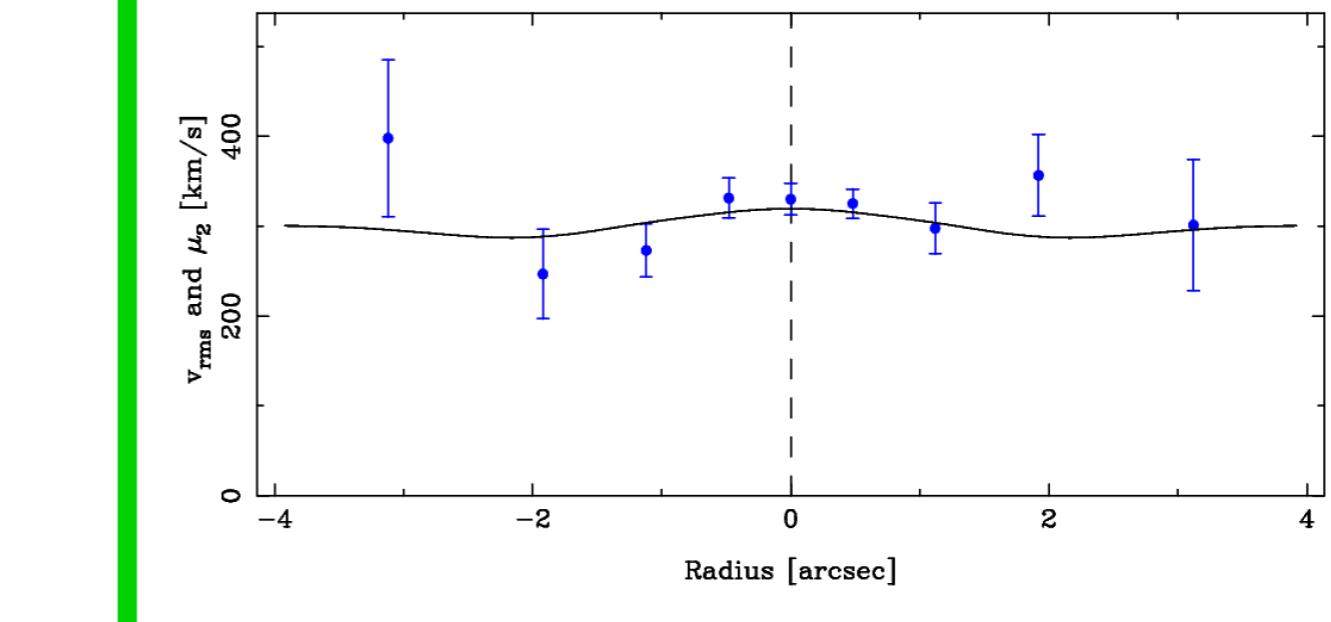


# SDSSJ0912

## GRAVITATIONAL LENSING



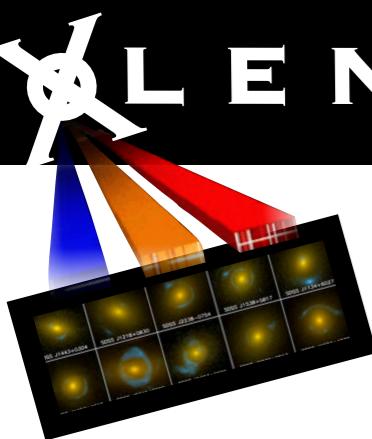
## STELLAR KINEMATICS



$z_{\text{lens}}$	$z_{\text{BG}}$	$R_{\text{eff}}(\text{kpc})$	$R_{\text{Ein}}(\text{kpc})$	$M_V(\text{mag})$
0.1642	0.3239	10.8	4.58	16.56

$$\sigma^* = 326 \pm 13 \text{ km/s}$$

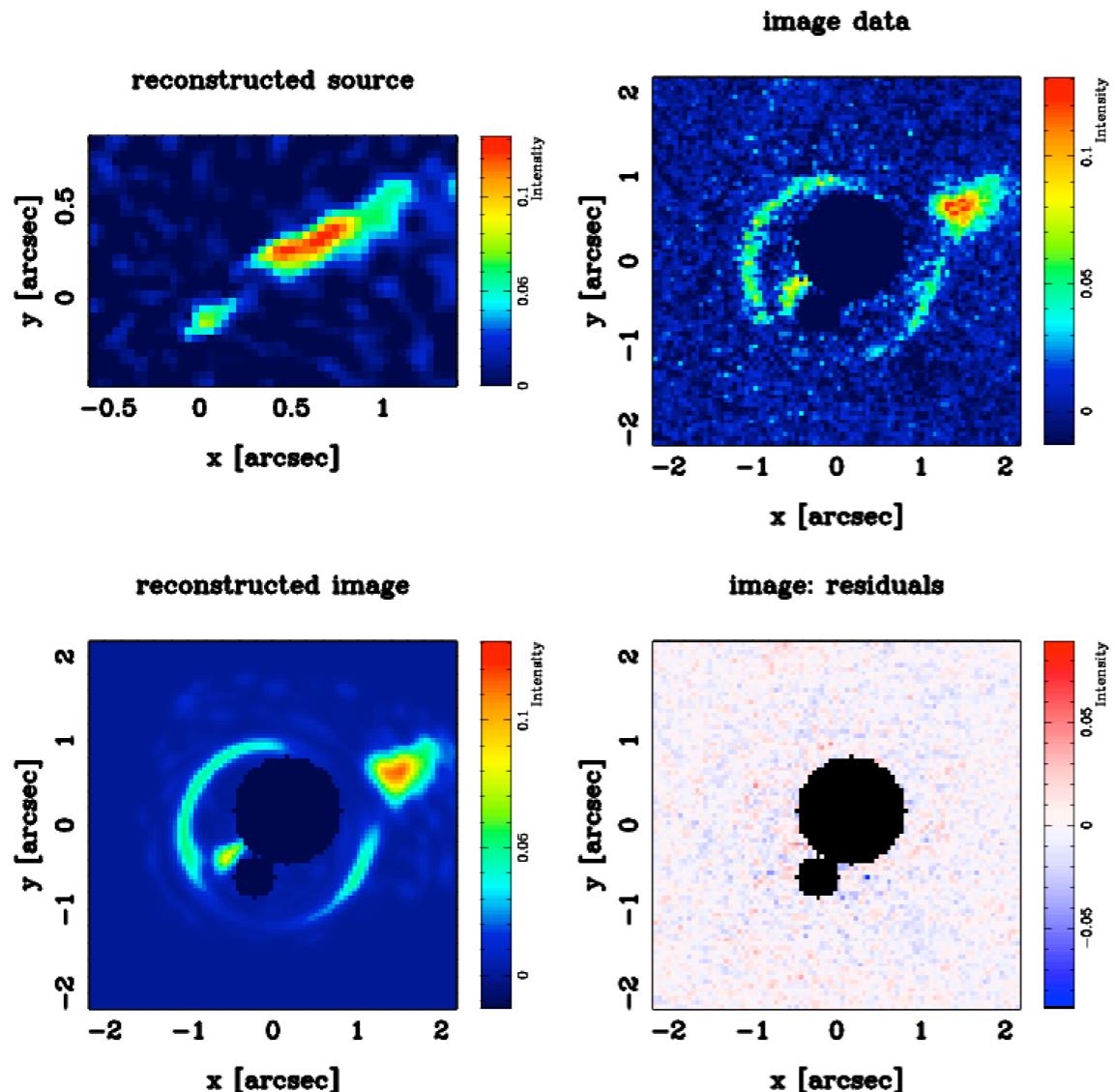
$$f_{\text{DM}}(1 R_{\text{eff}}) = 0.20 \pm 0.08$$



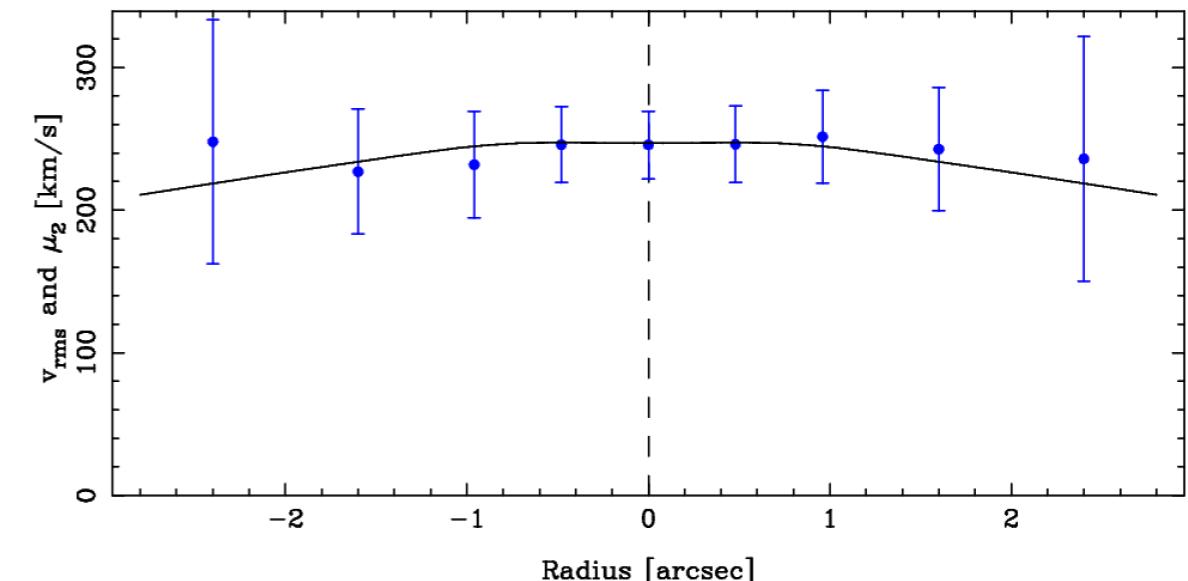
# SDSSJ0936



## GRAVITATIONAL LENSING



## STELLAR KINEMATICS



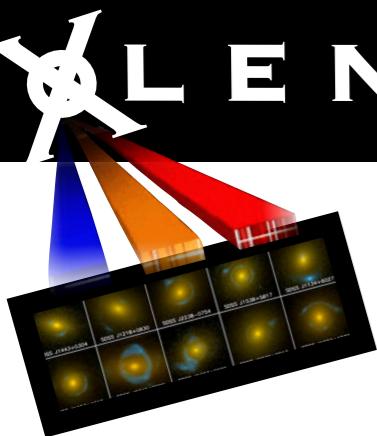
$z_{\text{lens}}$	$z_{\text{BG}}$	$R_{\text{eff}}(\text{kpc})$	$R_{\text{Ein}}(\text{kpc})$	$M_V(\text{mag})$
0.1897	0.5880	6.61	3.45	17.12

$$\sigma^* = 326 \pm 13 \text{ km/s}$$

$$f_{\text{DM}} (1 R_{\text{eff}}) = 0.04 \pm 0.03$$

L E N S

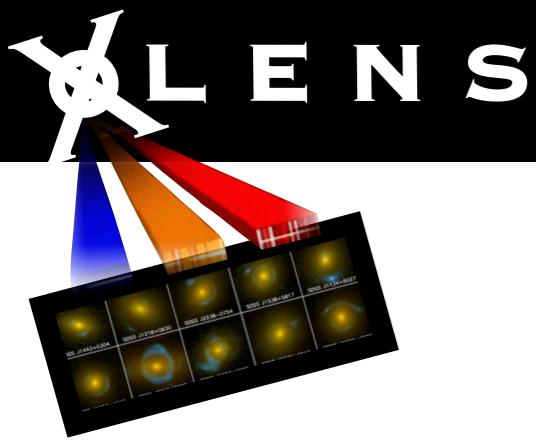
+ Combined Algorithm for Unified Lensing and Dynamics Reconstruction



# COMPLETELY BLIND ANALYSIS



Kapteyn Astronomical Institute  
University of Groningen (NL)

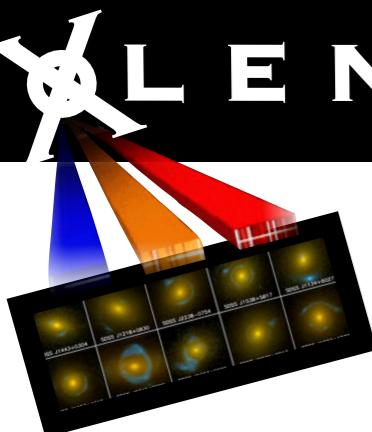


# COMPLETELY BLIND ANALYSIS



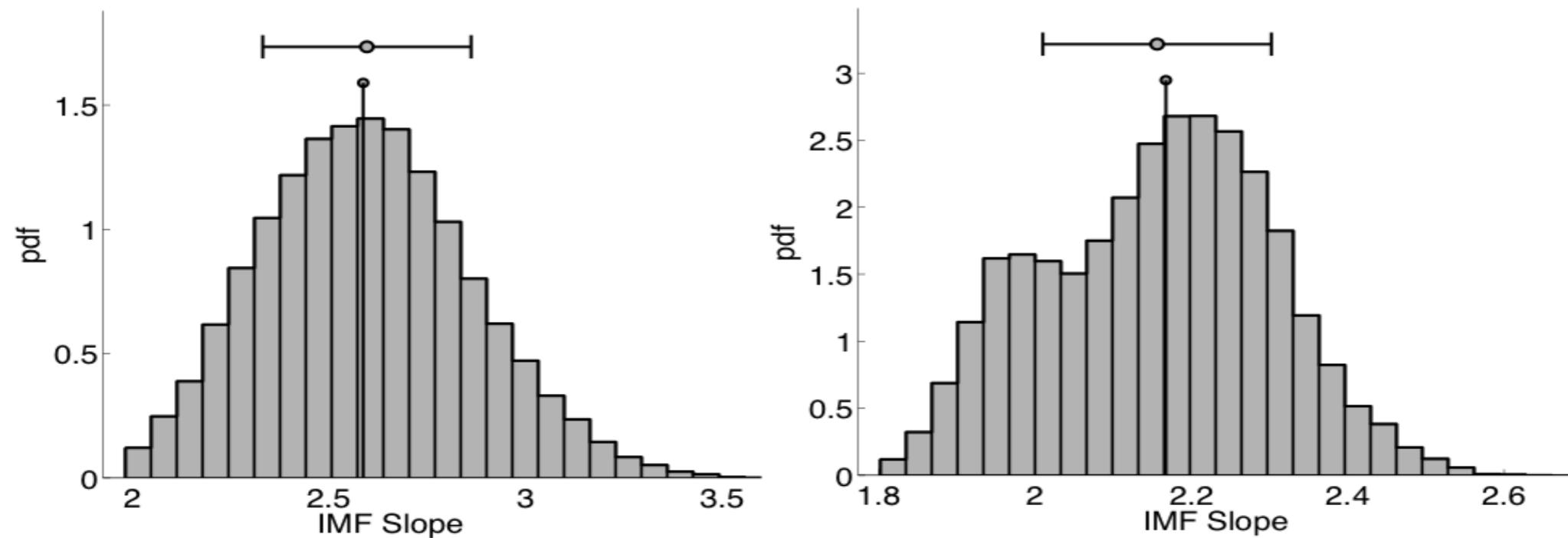
## 1. Lensing & Dynamics

parameter	prior J0936	posterior J0936	prior J0912	posterior J0912
$v_{\text{vir}}/\text{km s}^{-1}$	$\text{U}(0, 650)$	$49^{+64}_{-32}$	$\text{U}(0, 650)$	$385^{+115}_{-83}$
$\gamma$	$\text{U}(0, 2)$	$1.04^{+0.64}_{-0.67}$	$\text{U}(0, 2)$	$0.53^{+0.50}_{-0.37}$
$c_{-2}$	$\text{U}(0, 50)$	$18^{+17}_{-14}$	$\text{U}(0, 50)$	$9.1^{+4.5}_{-3.5}$
$q_h$	$\text{L}\mathcal{N}(1, 0.3)$	$0.94^{+0.29}_{-0.21}$	$\text{L}\mathcal{N}(1, 0.3)$	$0.54^{+0.09}_{-0.07}$
$M_\star/10^{11} M_\odot$	$\text{U}(0, 10)$	$3.41^{+0.09}_{-0.20}$	$\text{U}(0, 35)$	$10.12^{+0.67}_{-0.70}$
$b$	$\text{U}(0, 5)$	$0.88^{+0.34}_{-0.34}$	$\text{U}(0, 5)$	$1.94^{+0.21}_{-0.24}$

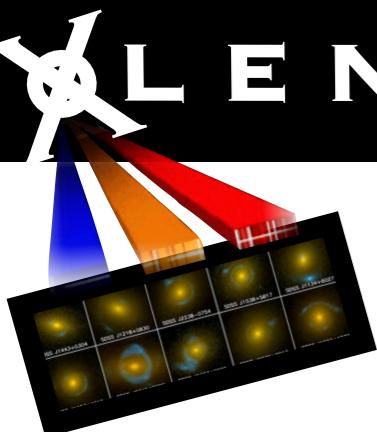


# COMPLETELY BLIND ANALYSIS

## 2. Spectroscopy & SSP modeling



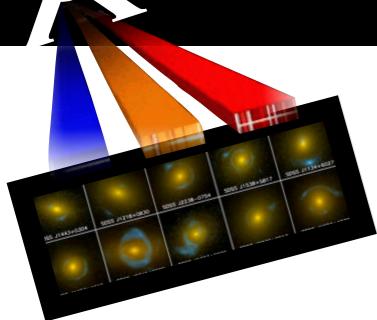
System	Log(Age) (Gyr)	[ $\alpha$ /Fe]	IMF slope	$M_{M_{\text{low}}=0.115}^*$ ( $\times 10^{11} M_{\odot}$ )
J0912+0029	$1.1 \pm 0.05$	$0.1 \pm 0.03$	$2.6 \pm 0.3$	$12.8 \pm 0.4$
J0936+0913	$0.9 \pm 0.05$	$0.05 \pm 0.02$	$2.1 \pm 0.15$	$3.01 \pm 0.03$



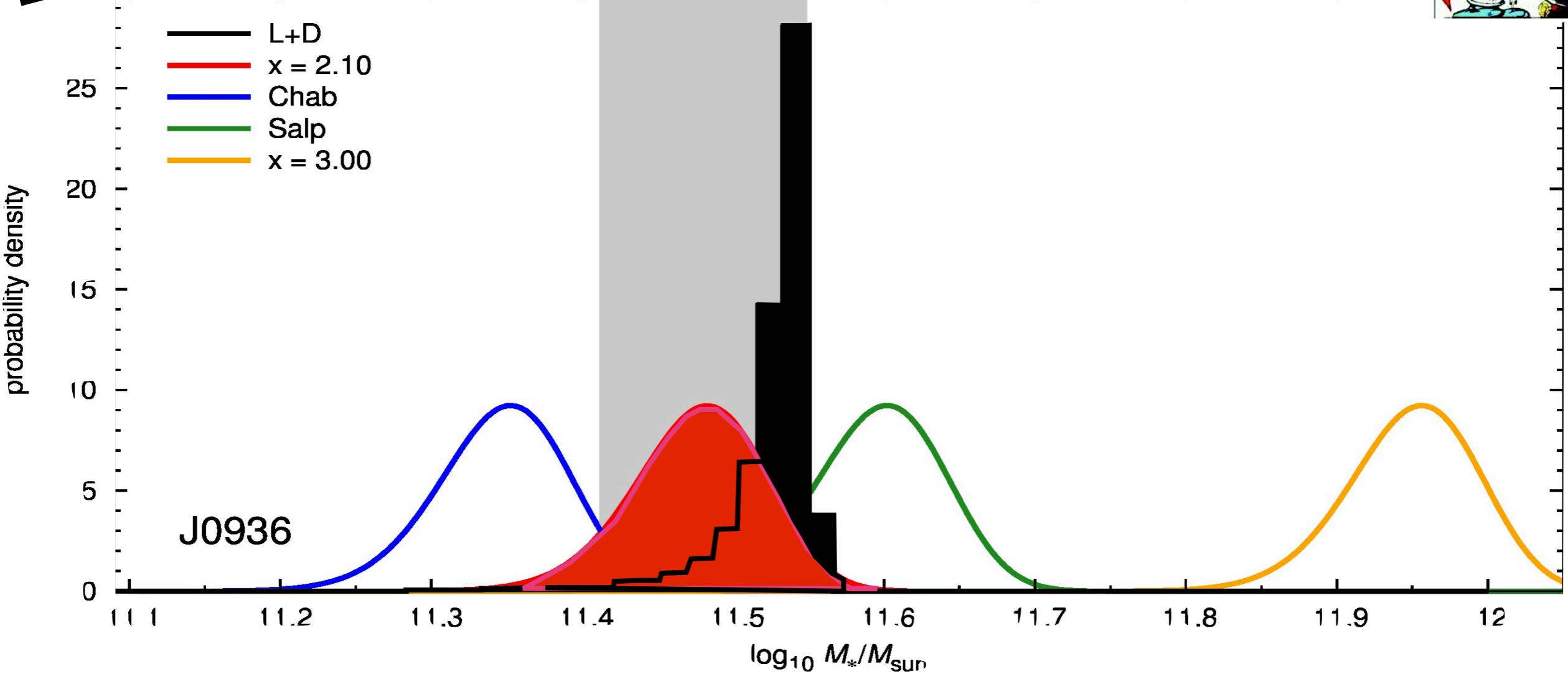
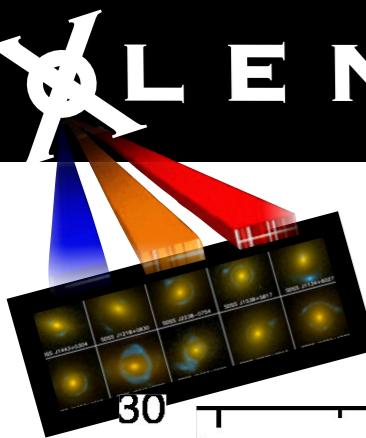
# COMPLETELY BLIND ANALYSIS



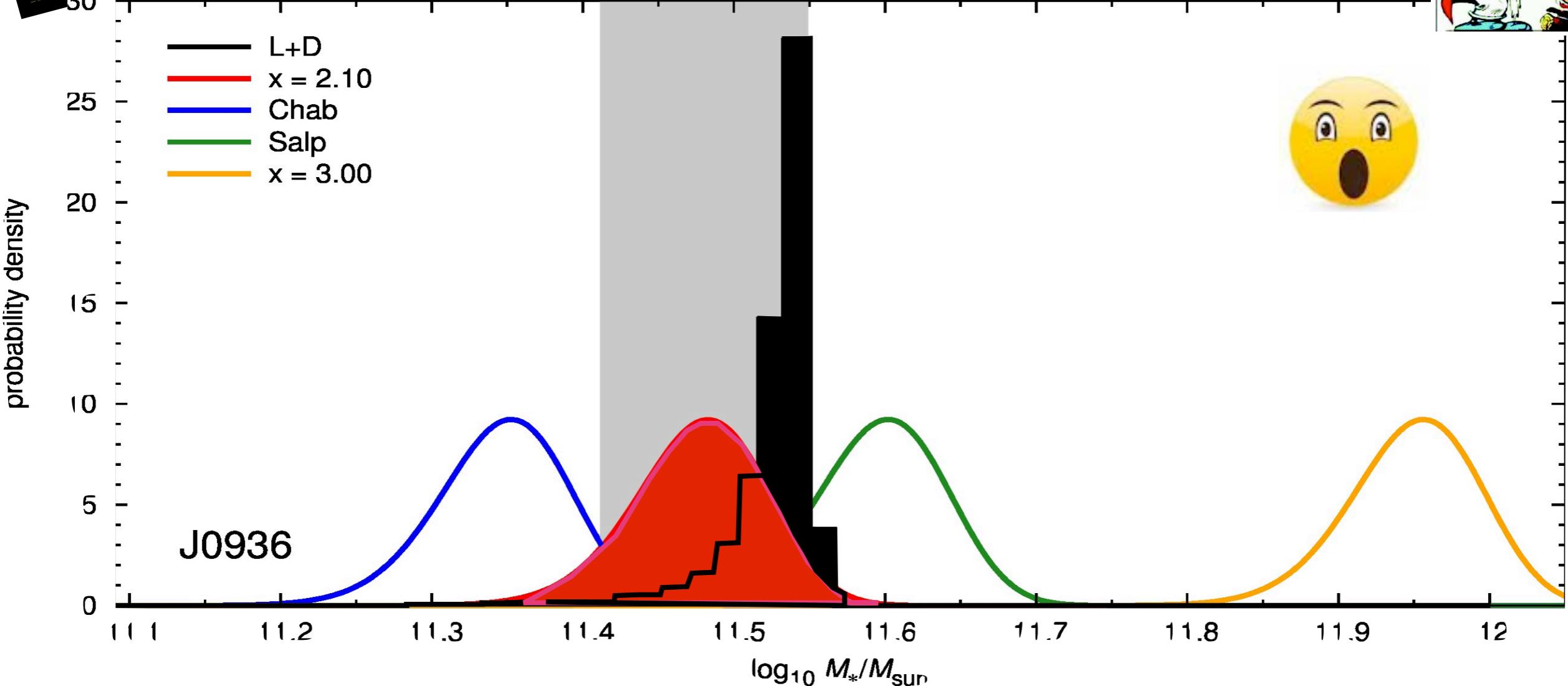
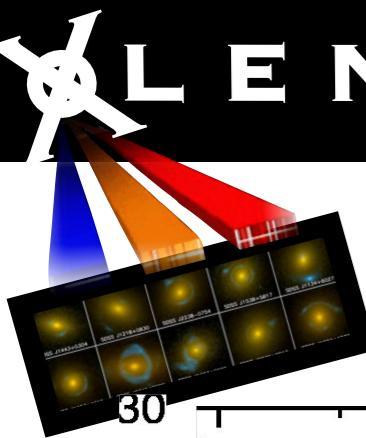
Kapteyn Astronomical Institute  
University of Groningen (NL)



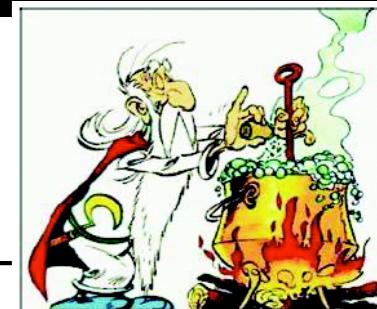
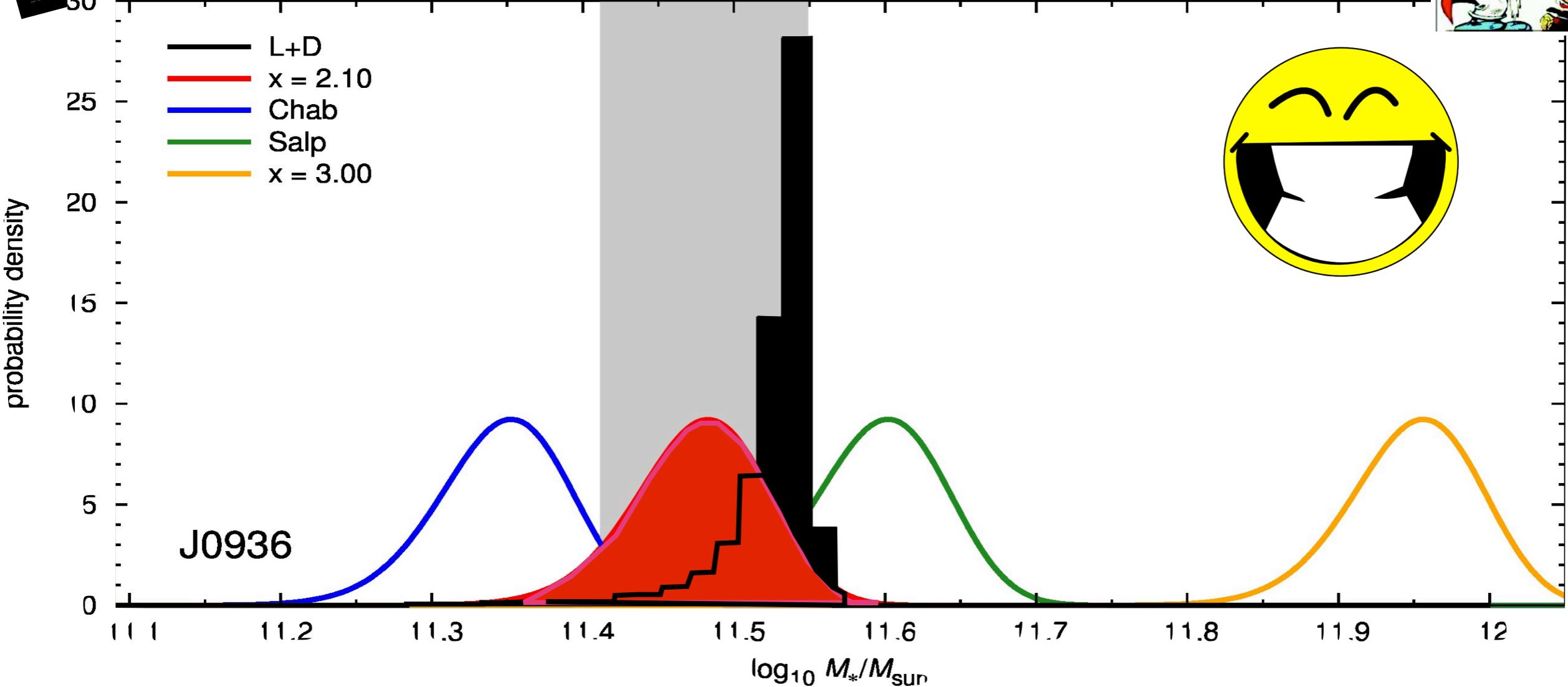
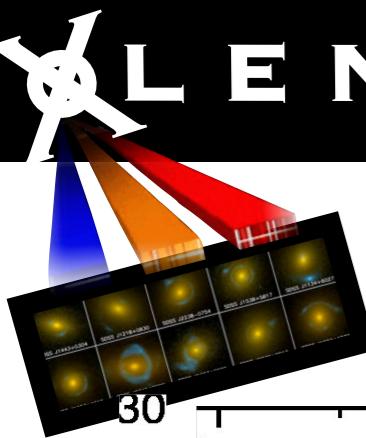
ical Institute  
ingen (NL)



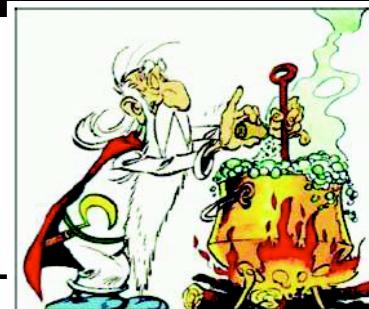
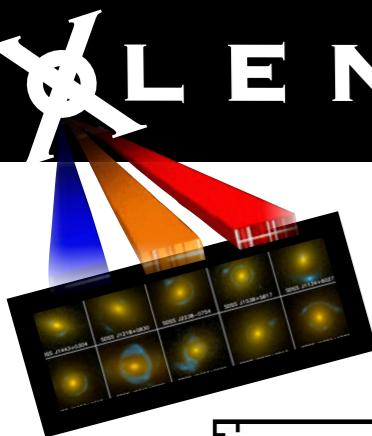
- The stellar masses inferred from the spectroscopic single stellar population (SSP) modelling based on line-strength indices is fully consistent with the *independent* inferences from the combined lensing and dynamics study (which makes no assumptions on the IMF)



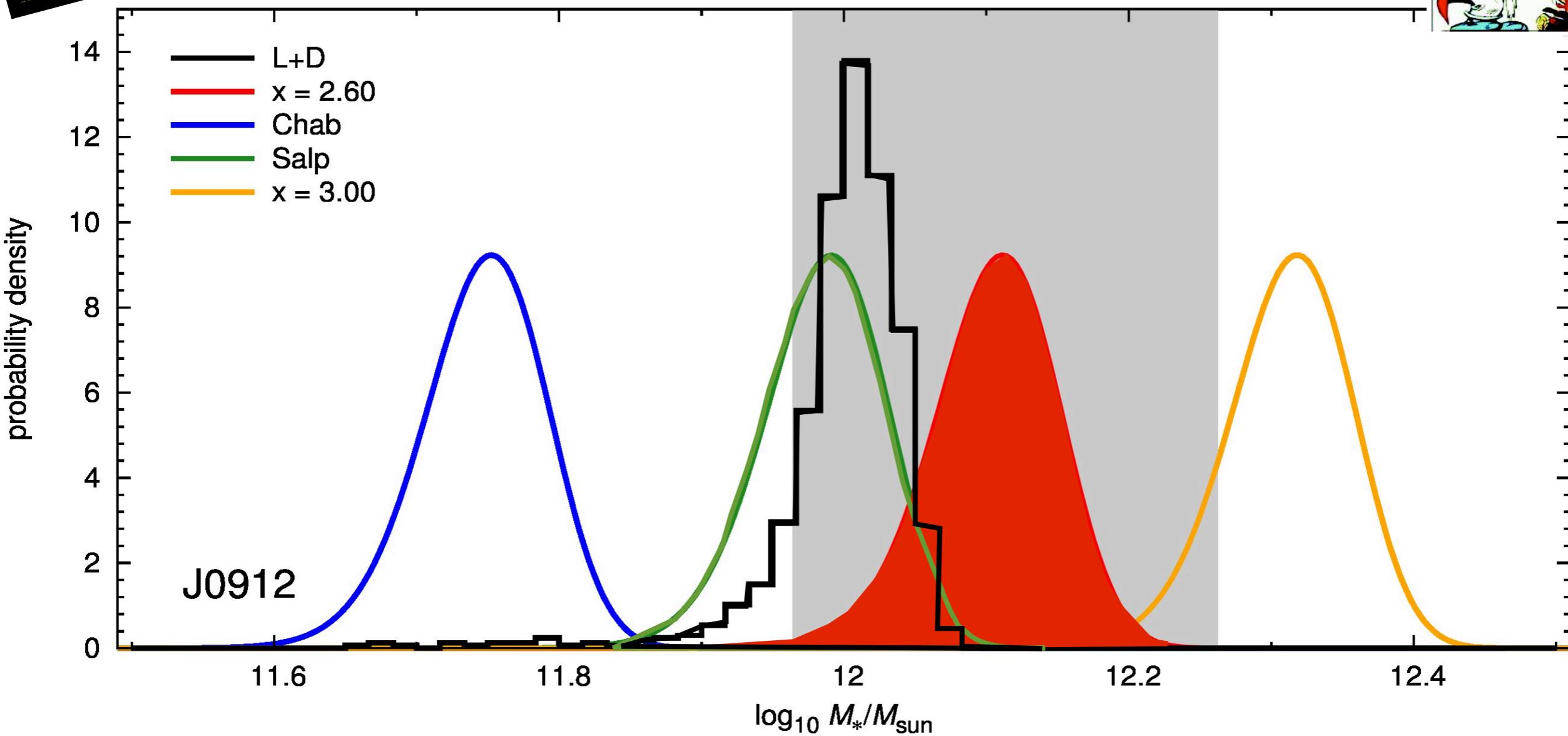
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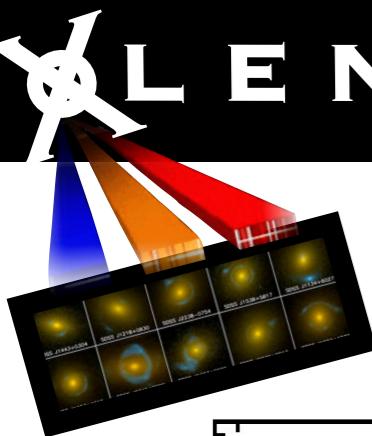
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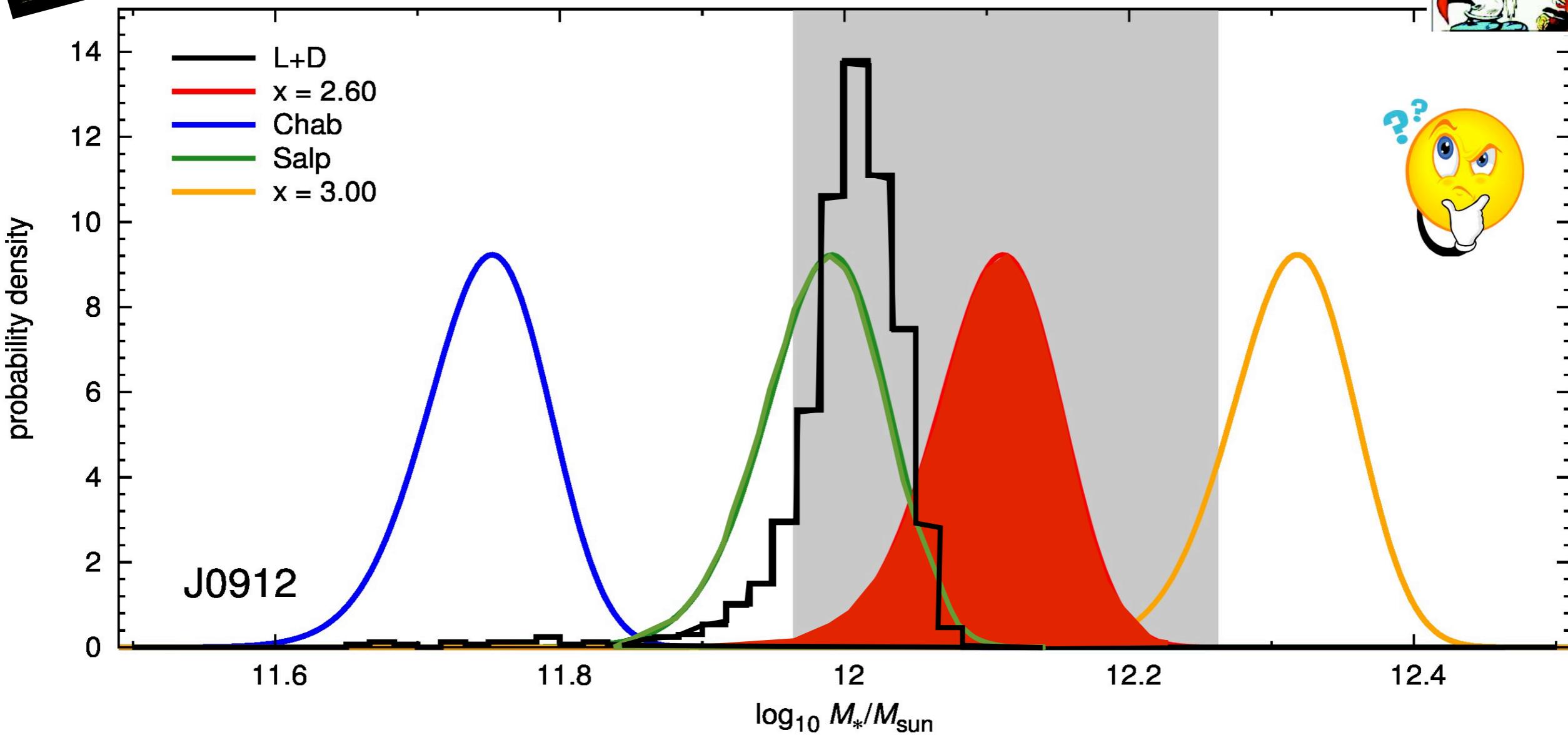
# SDSSJ0912



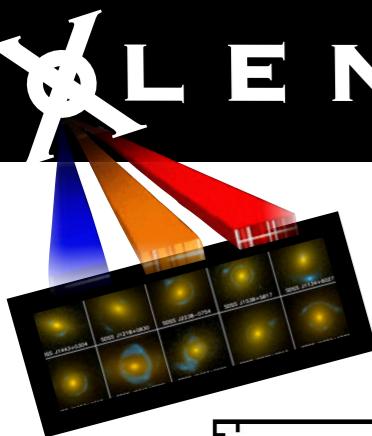
- Line-index-based stellar mass higher than the L&D one
- IMFs significantly steeper than Salpeter (“bottom-heavy”,  $x \geq 3.0$ ) are ruled out with decisive evidence: Bayes factor  $B > 1000$



# SDSSJ0912



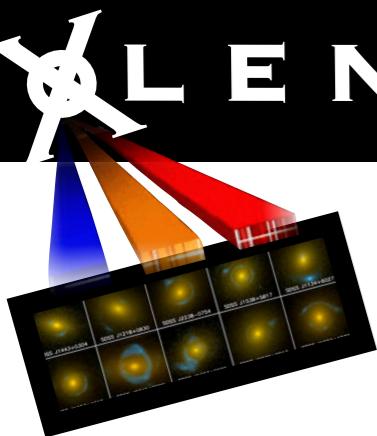
- Line-index-based stellar mass higher than the L&D one **WHY?**
- IMFs significantly steeper than Salpeter (“bottom-heavy”,  $x \geq 3.0$ ) are ruled out with decisive evidence: Bayes factor  $B > 1000$



## SDSSJ0912



- Line-in & D one **WHY?**
- IMFs significantly discrepant with simpler, more parsimonious models ( $x \geq 3.0$ ) are ruled out with decisive evidence: Bayes factor  $B > 1000$

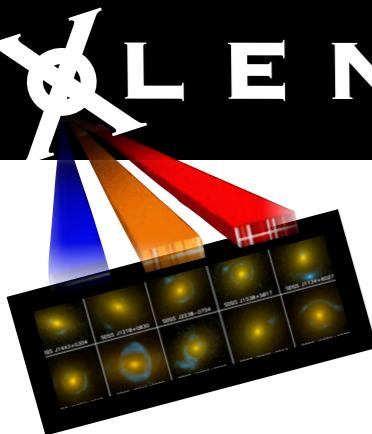


## THE LOW CUTOFF MASS

Using a (or more) set of isochrones and stellar libraries stellar population synthesis models construct the integrated light spectra:

$$f(\lambda) = \int_{m_l}^{m_h(t)} s(\lambda, m) \phi(m) dm$$

where  $\phi(m)$  is the IMF:  $\Phi(m) = \frac{dN}{dM} = M^{-\alpha}$



# THE LOW CUTOFF MASS

Using a (or more) set of isochrones and stellar libraries stellar population synthesis models construct the integrated light spectra:

$$f(\lambda) = \int_{m_l}^{m_h(t)} s(\lambda, m) \phi(m) dm$$

where  $\phi(m)$  is the IMF:

$$\Phi(m) = \frac{dN}{dM} = M^{-x}$$

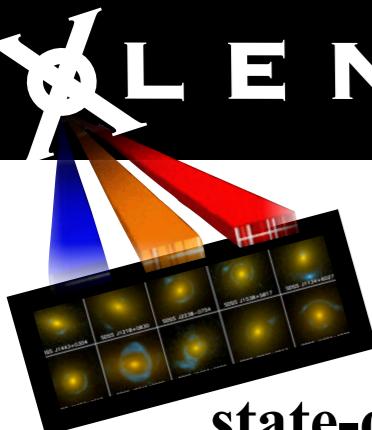
**LOWER-MASS LIMIT**

*Until now fully unconstrained parameter, despite critical to determine stellar M/L.*

Different codes -> different assumptions !!!

Impossible to determine  $M_{low}$  from spectroscopic studies alone

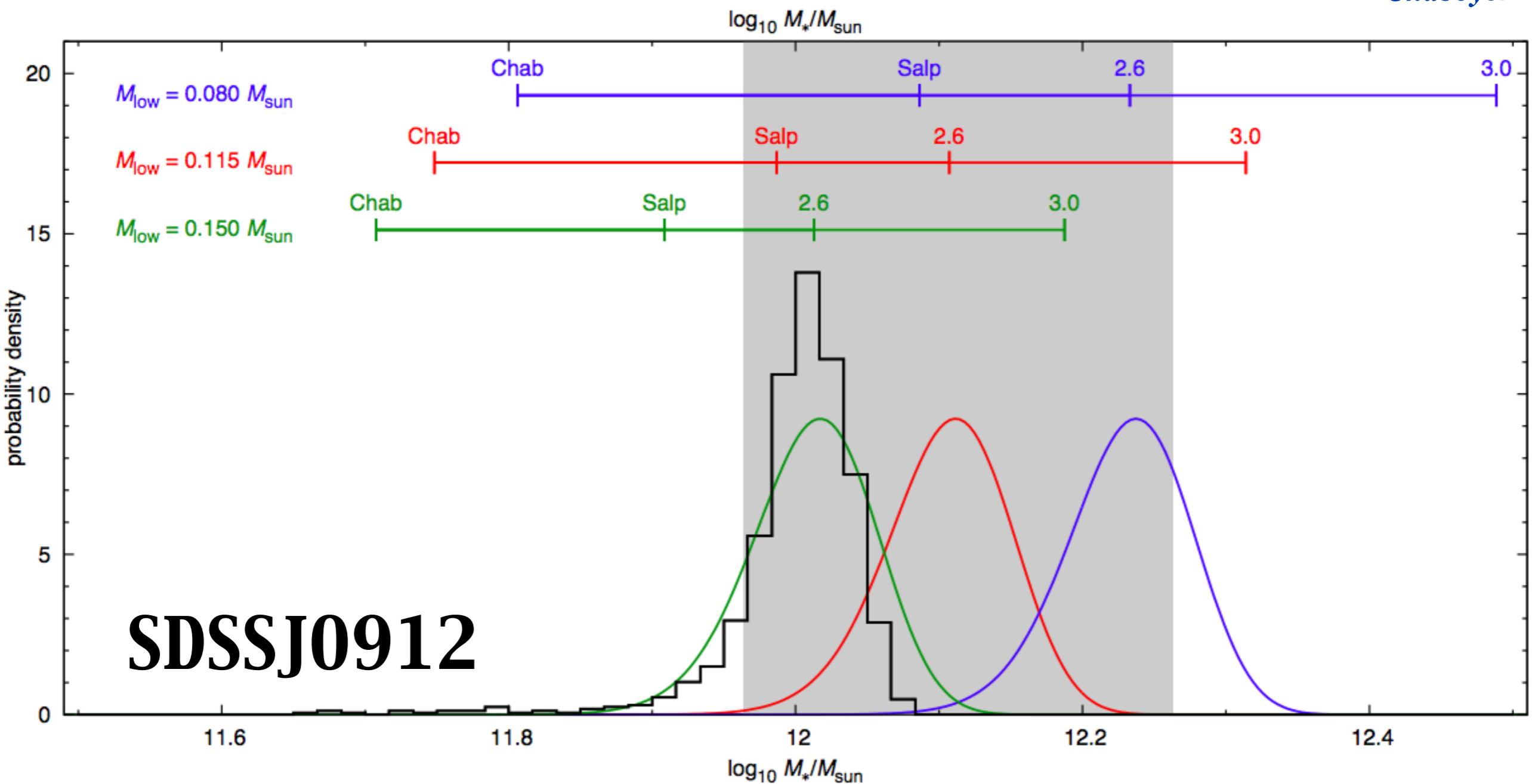
Stars with masses below  $\sim 0.15M_\odot$  have no effect on the spectral lines for any assumed IMF slope (*CvD12*)...but they give a non-negligible contribution to the total mass budget of the system (*Worthey 1994*).

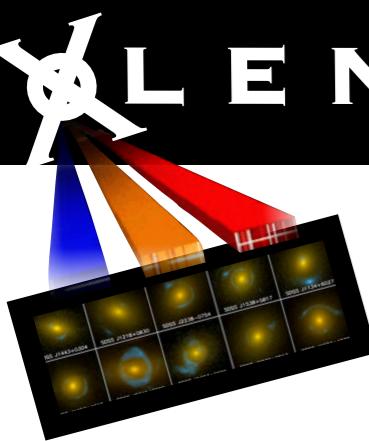


# THE LOW CUTOFF MASS

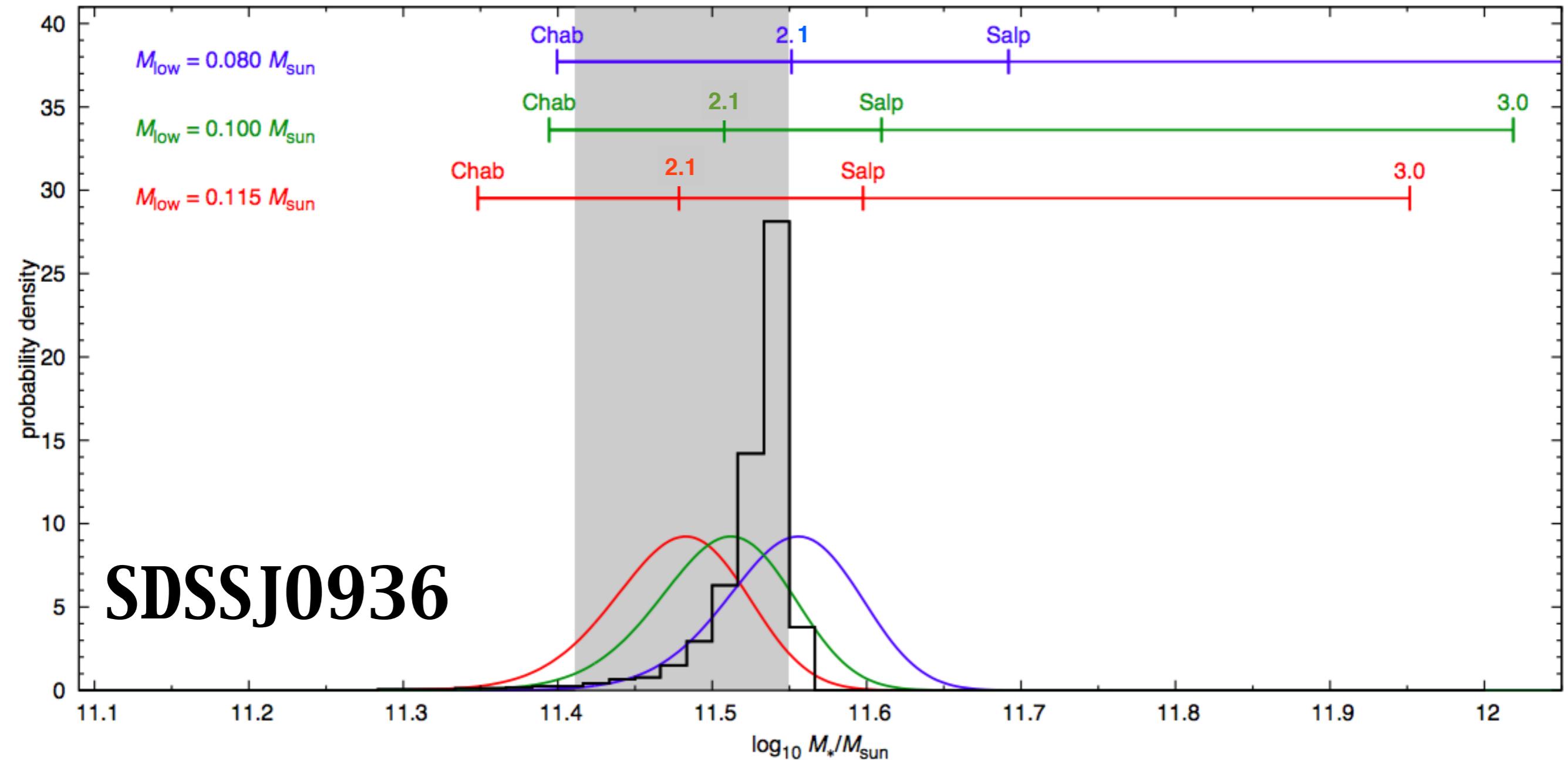
We calculate  $(M/L)^*$  using the isochrones at solar [Fe/H] from the state-of-the-art stellar evolution code Dartmouth Stellar Evolution Program selecting IMF slope, age, and  $[\alpha/\text{Fe}]$  inferred from the line-strength analysis

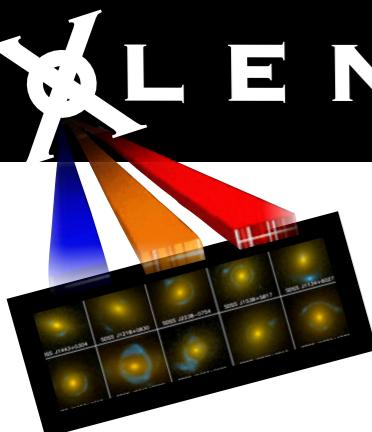
DSEP,  
Chaboyer+01





# THE LOW CUTOFF MASS

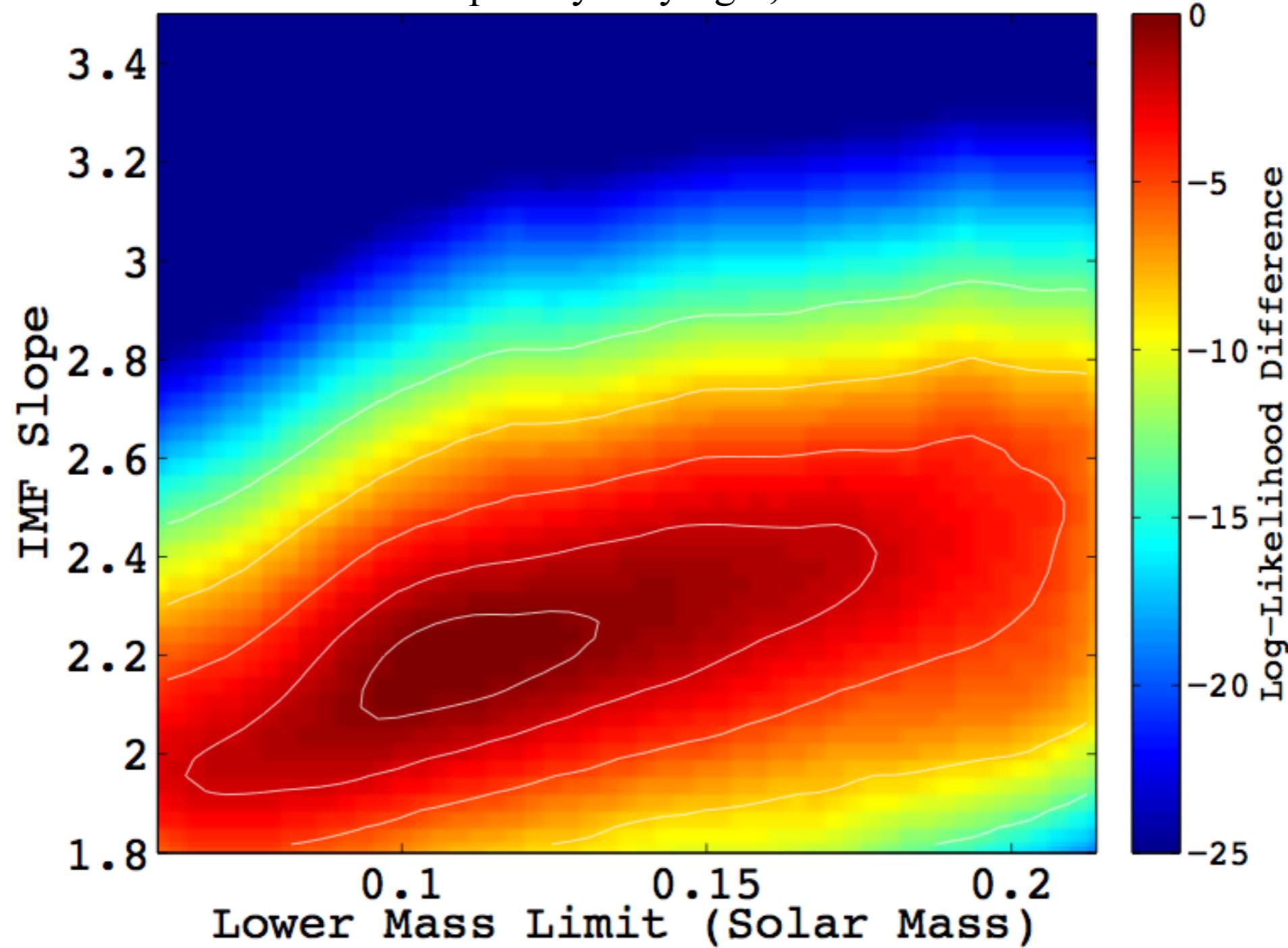


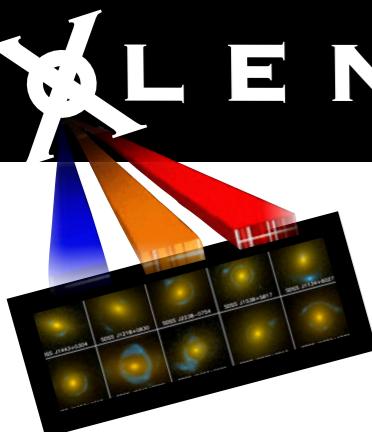


# FINAL JOINT PDF

MCMC to sample the joint lensing, dynamics and SSP posterior.

- 100000 samples by varying x, Mlow and LV -

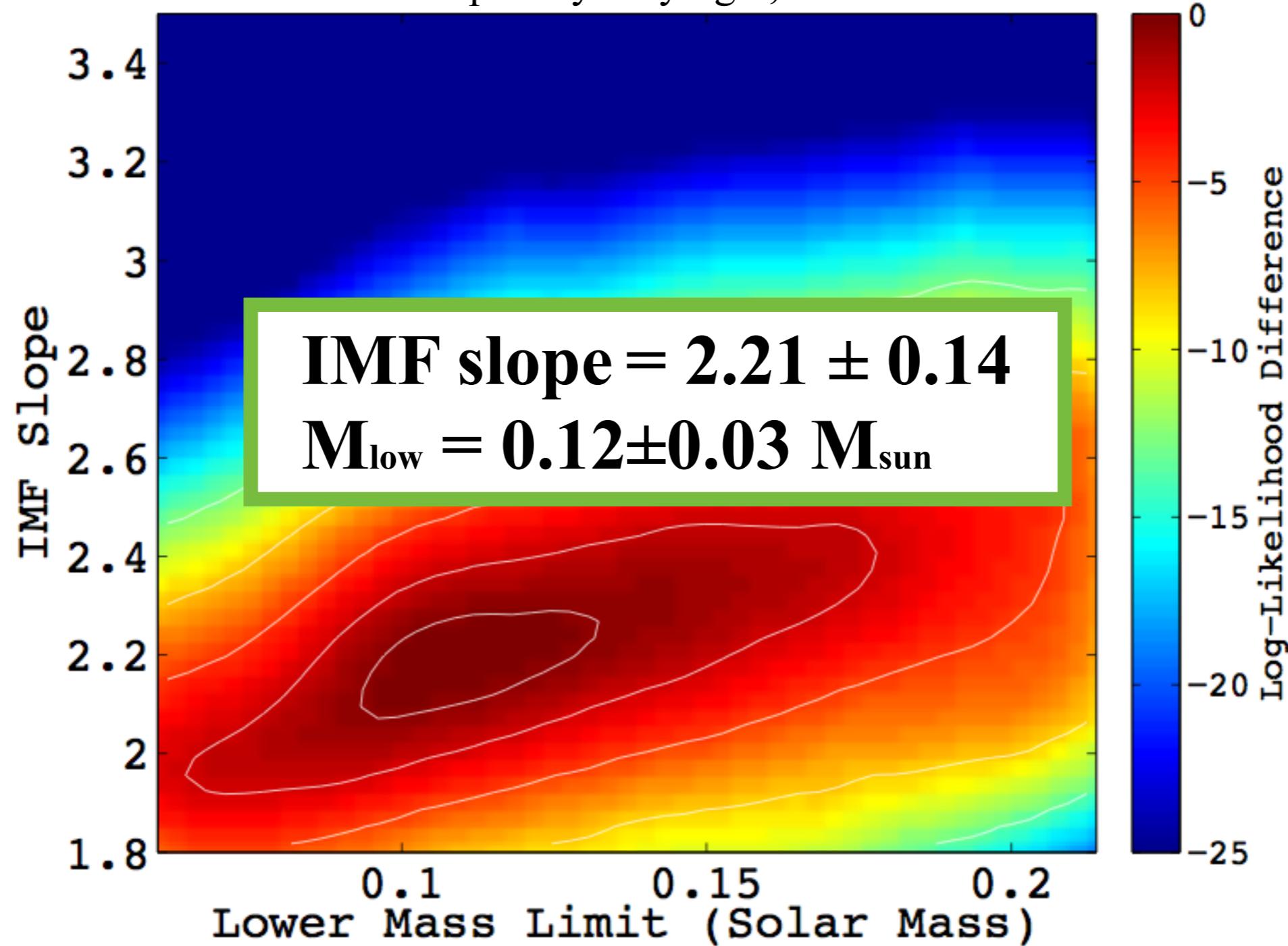


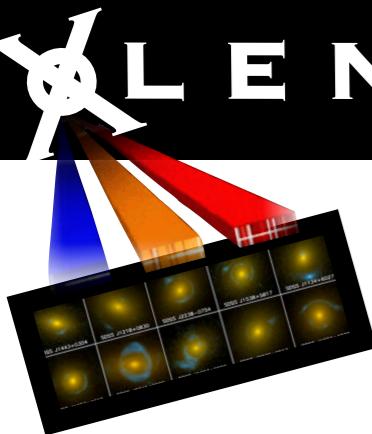


## FINAL JOINT PDF

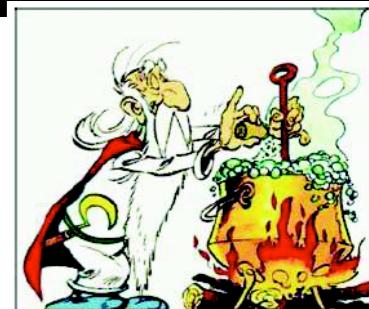
MCMC to sample the joint lensing, dynamics and SSP posterior.

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# CONCLUSION

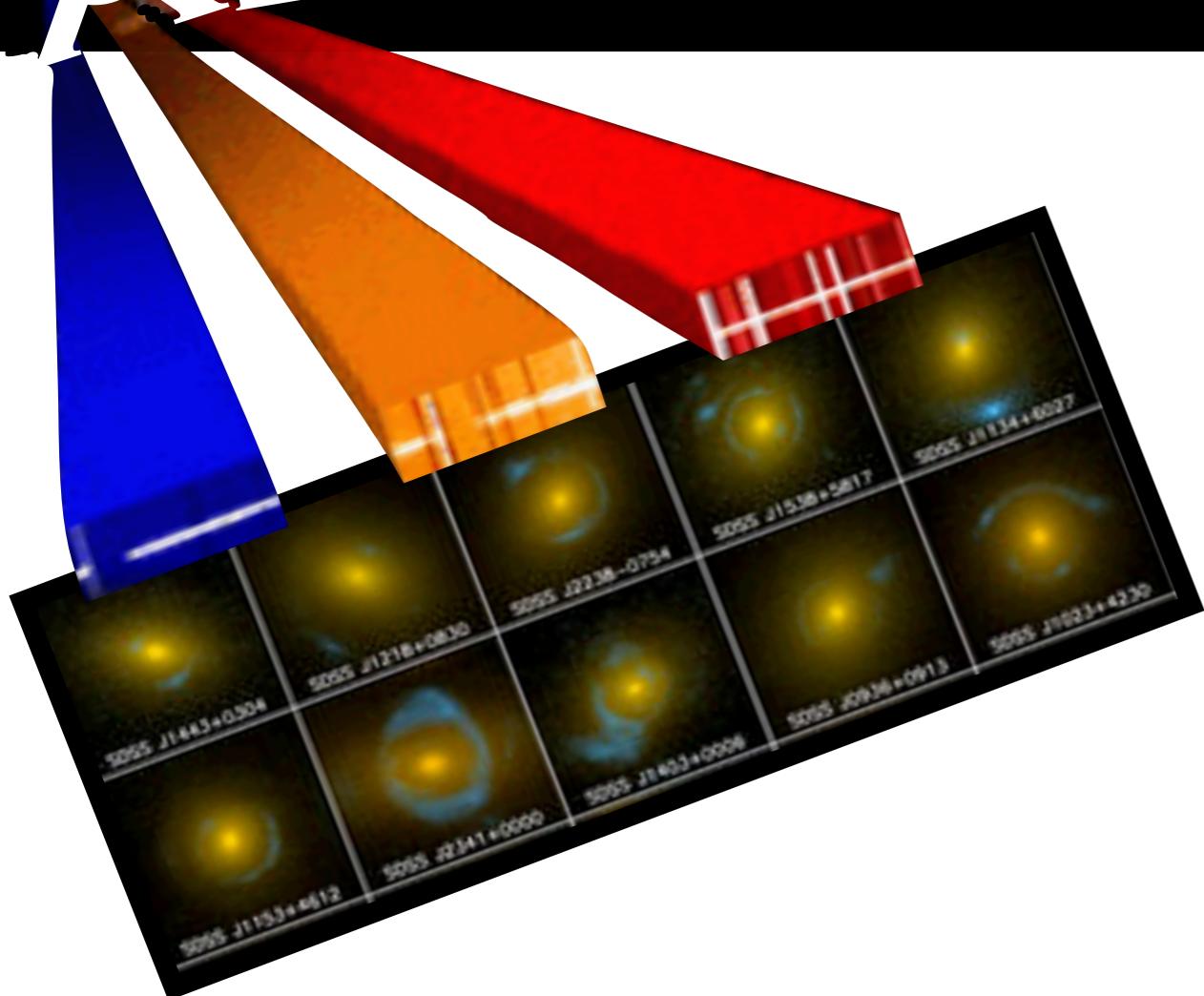


- The inferences on stellar masses from two independent methods are **consistent**
- SSP modeling suggests a steepening of the IMF slope with mass (more data are coming!)
- First constraint on low-mass cutoff of the IMF  
 $M_{\text{low}} = 0.12 \pm 0.03 M_{\text{sun}}$
- The joint inference on the IMF slope =  $2.21 \pm 0.14$  is consistent with Salpeter

*A special  
thank to  
Matteo Barnabè*



# L E N S + Combined Algorithm for Unified Lensing and Dynamics Reconstruction



# THE END