Weibel instability in astrophysical jets

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Nishikawa et al. 2006, ApJ 642, 1274 Ramirez-Ruiz, Nishikawa, & Hededal, 2007, in press (astro-ph/0707.4381)

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Outline of talk

- Motivations
- 3-D particle simulations of relativistic jets
 * electron-positron, (a pair jet created by photon annihilation)

 $\gamma = 5$ (electron-ion), 15, $4 < \gamma < 100$

- * pair jet into pair and electron-ion ambient plasmas $\gamma = 12.57, 1 < \gamma < 30$
- Evolution of the Weibel instability
- Particle Acceleration mechanism
- Summary of current 3-D simulations (Weibel Instability)
- Calculation of radiation based on particle trajectories
- Future plans of our simulations of relativistic jets

Motivations

- Study particle acceleration at external and internal shocks in relativistic jets selfconsistently with kinetic effects
- Study structures and dynamics of collisionless shocks caused by instabilities at the jet front and transition region in relativistic jets
- Particles acceleration and associated synchrotron/jitter radiation
- Examine possibilities for afterglows in gammaray bursts with appropriate ambient plasmas

Observations of M87

Shocks?

nonthermal electrons, enhanced magnetic field, jitter radiation (Medvedev 2000, 2006; Fleishman 2006)?



Schematic GRB from a massive stellar progenitor (Meszaros, Science 2001)



Necessity of 3-D full particle simulation for particle acceleration

- MHD simulations provide global dynamics of relativistic jets including hot spots
- MHD simulations include heating due to shocks, however do not create high energy particles (MHD simulation + test particle (Tom Jones))
- In order to take account of acceleration, the kinetic effects need to be included
- Test particle (Monte Carlo) simulations can include kinetic effects, but not self-consistently
- Particle simulations provide particle acceleration () with $(\varepsilon_e, \varepsilon_B)$ and emission self-consistently. However, due to the computational limitations, particle-in-cell (PIC) simulations covers only a small part of the full jet.
- Particle simulations can provide synchrotron and jitter radiation from ensemble of each particle (electron and positron) motion in electromagnetic fields.



Collisionless shock

Electric and magnetic fields created selfconsistently by particle dynamics randomize particles

jet

(Buneman 1993)

 $\partial B / \partial t = -\nabla \times E$ $\partial E / \partial t = \nabla \times B - J$ $dm_0 \gamma v / dt = q(E + v \times B)$ $\partial \rho / \partial t + \nabla \cdot J = 0$





(Medvedev & Loeb, 1999, ApJ)

3-D Simulations of Weibel instability

(Silva et al. 2003,

ApJL)

Counter-steaming electron-positron shells



(Jaroschek, Lesch, & Treumann, ApJ, 2005)

Electron-ion plasma for a long time for nonlinear stage (Frederiksen at al. 2004, ApJL; Hededal et al. 2004, ApJL)





(Spitkovsky 2006)

Initial parallel velocity distributions of pair-created jets

- A: $\gamma = (1 (v_j/c)^2)^{-1/2} = 5$
- B: $\gamma = (1 (v_j/c)^2)^{-1/2} = 15$
- C: $4 < \gamma < 100$ (distributed cold jet)

(pair jet created by photon annihilation, $_+_\rightarrow e^{\pm}$)

• A': $\gamma = 5$ (electron-ion)

Growth times of Weibel instability:

 $__{A} \ll \tau_{A'} \ll __{B} \ll __{C}$

Schematic initial parallel velocity distribution of jets





Evolution of B_x due to the Weibel instability el-positron $\gamma = 15$ (B) (convective instability)

X-MAGNE FIELD T= 5.0



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B_x component generated by current channels at $t = 59.8 \omega_{pe}$



el-positron $4 < \gamma < 100$









Magnetic field energy and parallel and perpendicular velocity space along Z $\omega_{pe}t = 59.8$

Isosurfaces of jet particles and z-component of current density injected into electron-ion ambient plasma

 $v_{\parallel} = 12.57$

(electron: blue, positron: gray)

(+*J_z*: *blue*, -*J_z*:*red*)





(local magnetic filed lines: white)





Magnetic field generation and particle acceleration with narrow jet $(u_{\parallel} = \gamma v_{\parallel} = 12.57)$



blue dots: ambient (positrons and ions)

(Ramirez-Ruiz, Nishikawa, Hededal 2007)

Present theory of Synchrotron radiation

- Fermi acceleration (not self-consistent simulation) (particles are crossing at the shock surface many times and accelerated, the strength of turbulent magnetic fields are assumed)
- The strength of magnetic fields is assumed based on the equipartition (magnetic field is similar to the thermal energy) (ϵ_B)
- The density of accelerated electrons are assumed by the power low $(F(\gamma) = \gamma^p; p = 2.2?)(\epsilon_e)$
- Synchrotron emission is calculated based on p and $\varepsilon_{\rm B}$
- There are many assumptions in this calculation

Self-consistent calculation of radiation

- Electrons are accelerated by the electromagnetic field generated by the Weibel instability (without the assumption used in test-particle simulations for Fermi acceleration)
- Radiation is calculated by the particle trajectory in the self-consistent magnetic field
- This calculation include Jitter radiation (Medvedev 2000, 2006) which is different from standard synchrotron emission

Radiation from collisionless shock

To obtain a spectrum, "just" integrate:

$$\frac{d^2 W}{d\Omega d\omega} = \frac{\mu_0 c q^2}{16\pi^3} \left| \int_{-\infty}^{\infty} \frac{\mathbf{n} \times \left[(\mathbf{n} - \boldsymbol{\beta}) \times \dot{\boldsymbol{\beta}} \right]}{(1 - \boldsymbol{\beta} \cdot \mathbf{n})^2} e^{i\omega(t' - \mathbf{n} \cdot \mathbf{r}_0(t')/c)} dt' \right|^2$$

where \mathbf{r}_0 is the position, $\boldsymbol{\beta}$ the velocity and $\boldsymbol{\beta}$ the acceleration



New approach: Calculate radiation from integrating position, velocity, and acceleration of ensemble of particles (electrons and positrons)

Hededal, Thesis 2005 (astro-ph/0506559)

3D jitter radiation (diffusive synchrotron radiation) with a ensemble of mono-energetic electrons ($\gamma = 3$) in turbulent magnetic fields (Medvedev 2000; 2006, Fleishman 2006)



Hededal & Nordlund (astro-ph/0511662)

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Radiation from collisionless shock



Hededal & Nordlund 2005, submitted to ApJL (astro-ph/0511662)

Summary

- Simulation results show Weibel instability which creates filamented currents and density along the propagation of jets.
- Weibel instability may play a major role in particle acceleration in relativistic jets.
- The magnetic fields created by Weibel instability generate highly inhomogeneous magnetic fields, which is responsible for Jitter radiation (Medvedev, 2000, 2006; Fleishman 2006).
- For details see Nishikawa et al. ApJ, 2003, 2005, 2006, Hededal & Nishikawa ApJ, 2005, and proceeding papers (astro-ph/0503515, 0502331, 0410266, 0410193)

Future plans for particle acceleration in relativistic jets^{26/39}

- Further simulations with a systematic parameter survey will be performed in order to understand shock dynamics
- In order to investigate shock dynamics further diagnostics will be developed
- Simulations with large systems will be performed with the codes parallelized with OpenMP and MPI
- Investigate synchrotron (jitter) emission, and/or polarity from the accelerated electrons and compare with observations (Blazars and gamma-ray burst emissions)
- Develop a new code implementing synchrotron loss and/or inverse Compton scattering

Gamma-Ray Large Area Space Telescope (GLAST)

(will be launched in early 2008)

Compton Gamma-Ray Observatory (CGRO) http://www-glast.stanford.edu/



Burst And Transient Source Experiment (BATSE) (1991-2000)

PI Jerry Fishman



- Large Area Telescope (LAT) PI Peter Michaelson: 20 MeV to about 300 GeV
- GLAST Burst Monitor (GBM) PI Chip Meegan (MSFC): X-rays and gamma rays with energies between 5 keV and 25 MeV (http://gammaray.nsstc.nasa.gov/gbm/)
 The combination of the GBM and the LAT provides a powerful tool for studying gamma-ray bursts, particularly for time-resolved spectral studies over a very large energy band.



Fushin

(god of wind)



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M87

Mass of black hole: 3 billion solar masses Resolve ~ 100 m



M87 -- From 200,000 Light-Years to 0.2 Light-Year

VLA - 2 cm

Three-dimensional GRPIC Simulation of Jets from Accretion Disks

Background:

Accrete3D was developed to study the self-consistent evolution of the jet from the accretion disk.

GRPIC Considerations

- GRMHD is a fluid approximation
- Particle motion is self-consistent (not ideal fluid)
- Dynamics of charged particle separation (not frozen)

Questions in Disk-Jet Dynamics/Simulation

- What is the acceleration mechanism?
- Why is the jet collimated?
- Can the disk-jet system become steady self-consistently?



Total magnetic field energy (Bx2 +By2 +Bz2) averaged in the x-y plane $B^{2} - B_{\perp}^{2} - B_{\perp}^{2} - B_{\perp}^{2}$





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Parallel and perpendicular velocity distributions





Pair-creation by collisions with lower energy photons: γγ_e⁺e⁻



Schematic plot of e^{\pm} pair cascades triggered by the back-scattering of seed γ -ray photons on the external medium.

Initial parallel velocity distributions of paircreated jets (e=) (into ambient pair plasma)

• A:
$$\gamma = (1 - (v_j/c)^2)^{-1/2} = 12.57$$

- B: 1 < γ < 30 (distributed cold jet)
 (pair jet created by photon annihilation, _+_→ e[±])
- A'and B': injected into ambient electron-ion plasma

Growth times of Weibel instability:

 $__{B'} \ll \tau_{A'} \ll_{B} \approx __{A}$

Schematic initial parallel velocity distribution of jets




$\epsilon_{\rm B}$ along the jet for four different cases



Growth of the two-stream instability at time t = 59.8_pe





Evolution of accretion disk with kinetic processes



Disk Instabilities

• We have conducted a preliminary analysis on the plasma mode and density structure within the disk.

- There is no electric field at T = 0.
- The first row is the density profile within the disk. The density

structure develops waves as the jet develops.

• The second row shows the growth of |m| = 4 for the zcomponent of the electric field. As the jet fully develops the instabilities grow within the disk.

• The third row shows the mode amplitude of the instability.

Summary and Further Development

• There appears to be mode coupling between the disk and the jet within the simulation. We see some of the same instabilities within the disk electric field within the jet region.

- The low grid resolution prevents an in-depth analysis of the density modes.
- We will increase the number of particles to study the density fluctuations and to test the correspondence with the field modes.
- We will include studies of the particle heating and work done by the field on the particles.
- Using MPI, we will make the code parallel.



Longer simulation of electron-ion jet injected into unmagnetized plasma

 $t = 59.8_{pe}$ \mathbf{V} X-MAGNE FIELD T=4600.0 1Ø 1.6 106 1.2 . 8 1ø⁵ . 4 $\mathbf{B}_{\mathbf{X}}$ \mathbf{z}^{10^4} -.4 103 -.8 10^{2} -1.2 1Ø¹ -1.6





VPAJET FR-RA T=4600.0



Scientific objectives

- How do shocks in relativistic jets evolve in accelerating particles and emission?
- How do 3-D relativistic particle simulations reveal the dynamics of shock front and transition region?
- What is the main acceleration mechanism in relativistic jets, shock surfing, wakefield, Fermi models or stochastic processes?
- Obtain spectra and time evolutions from simulations and compare with observations
- Understand observations from GLAST (GBM) based on simulation and theoretical studies

Electron acceleration by ion Weibel instability



Phase space distributions of elctrons





Parallel and perpendicular velocity space of ambient electrons along Z



Electron jet velocity distributions







Generated magnetic field Bx along Z direction

at $Y = 43 \Delta$ Blue $X = 33 \Delta$ Red $X = 43 \Delta$

Green X = 53 Δ

 $4 < \gamma < 100$ (distributed cold jet)







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Re

X/∆`X



$E \times B$ acceleration and deceleration in x-y plane







J_z and $(E_B)_z$ in the nonlinear stage in the x-y plane



 $\omega_{\rm pe} t = 59.8$

 \otimes ion current channel

_ electron current channel

E_B force accelerate and B_x, B_y decelerate particles





Z/ - _V_phase space of jet electrons at $t = 59.8 \omega_{pe}$



$Z/\Delta - \gamma V_{phase space of ambient electrons at t = 59.8 \omega_{pe}$



$Z/\Delta - \gamma V_{\perp}$ phase space of ambient electrons at $t = 59.8 \omega_{pe}$







color: electron density



Electron acceleration at t = $59.8 \omega_{pe}$



Frequency spectrum of radiation emitted by a relativistic electron

$$\frac{d^2 W}{d\omega d\Omega} = \frac{d^2 W_{\perp}}{d\omega d\Omega} + \frac{d^2 W_{\parallel}}{d\omega d\Omega}$$
$$= \frac{e^2 \omega^2}{3\pi^2 c} (\frac{a\theta_{\gamma}^2}{\gamma^2 c})^2 K_{2/3}^2(\eta) + \frac{e^2 \omega^2 \theta^2}{3\pi^2 c} (\frac{a\theta_{\gamma}}{\gamma c})^2 K_{1/3}^2(\eta)$$

$$\theta_{\gamma}^2 \equiv 1 + \gamma^2 \theta^2$$
, $\gamma = (1 - v^2/c^2)^{-1/2}$ and $\eta = \frac{\omega a \theta_{\gamma}^3}{3c\gamma^3}$, and $a = \frac{v^2}{\dot{v}_{\perp}} \approx \frac{c^2}{\dot{v}_{\perp}}$



(Jackson 1999; Rybicki & Lightman 1979)

Generated magnetic field B_x along Z direction

Blue $X = 33 \Delta$ Red $X = 43 \Delta$ Green $X = 53 \Delta$

at Y = 43

$$t = 28.6 / \omega_{pe}$$





Relationship between the total magnetic field energy and particle acceleration







Perturbed current density J_z (X – Y plane)

 $t = 28.6/\omega_{pe}$

Arrows $(\boldsymbol{B}_{\mathbf{x}}, \boldsymbol{B}_{\mathbf{y}})$

Z = 230_



J_z component generated by current channels (x-y plane) at $t = 59.8 \omega_{pe}$



Comparison between electron-ion and electron-positron

no-ambient magnetic field $\omega_{pe}t = 23.4$



(Nishikawa et al. 2005)


(Hededal & Nishikawa 2005)



Magnetosonic shock structure in 1-D system



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$E_B \ acceleration \ and \ deceleration \qquad (Z/\Delta = 430)$ $J_z \qquad arrows: E_x, E_y \qquad (E_B)_z \qquad arrows: B_x, B_y$ $U_z \qquad (ELE) \ T=3900.0 \qquad (EB)_z \qquad ($





⁽Hededal & Nishikawa 2004)



(Hededal & Nishikawa 2004)

Electron acceleration in perpendicular injection



(Hededal & Nishikawa 2004)

1-D simulations of positron acceleration (Hoshino et al. 1992) Maser instability



Illustration of the electron surfing mechanism



Density and J_z **in x-y plane**

 $\omega_{\rm pe}t = 23.4$



Flat jet injected parallel to B
Electron-ion jet,
$$m_i/m_e = 20$$

 $\beta = v_j/c = 0.9798, v_{et}/c = 0.1$
 $_= n_j/n_a \approx 0.741$
 $\gamma = (1-(v_j/c)^2)^{-1/2} = 5$
 $v_{je} = 3v_{et}, v_{ji} = 3v_{it}, v_{it}/c = 0.022$
 $\omega_{pe}/__e = 2.89, V_A/c = 0.0775, M_A = 12.65$
 $\beta_e (=8\pi n_e T_e/B^2) = 1.66$
 $\omega_{pe_t} = 0.026, r_j = 40 _x \approx 10__{ce} (infinite)$
 $__e = 1.389_, \rho_i = 6.211 \Delta$

Electron density (arrows: B_z, B_x)



Perpendicular acceleration of jet electron



86/39 A Flat jet injected into an unmagnetized plasma Electron-positron jet, $m_p/m_e = 1$ $\beta = v_i/c = 0.9798, v_{et}/c = 0.1$ $_{-} = n_i / n_a \approx 0.741$ $\gamma = (1 - (v_i/c)^2)^{-1/2} = 5$ $v_{je} = 0.1 v_{et}, v_{jp} = 0.1 v_{pt}$ $\omega_{\rm pe}_{\rm t} = 0.013$ $\lambda_{ce} = c/\omega_{pe} = 9.6\Delta, \ \lambda_e = v_{et}/\omega_{pe} = 0.96\Delta$

A Flat jet injected into an unmagnetized plasma

Electron-positron jet, $m_p/m_e = 1$ $= n_i / n_a \approx 0.741, v_{et} = v_{pt} = 0.1 c$ $v_{je} = 0.1 v_{et}, v_{jp} = 0.1 v_{pt}$ (cold jet) $\omega_{\rm pe}_{\rm t} = 0.013$ $\lambda_{ce} = c/\omega_{pe} = 9.6\Delta$ (electron skin depth) $\lambda_e = v_{et} / \omega_{pe} = 0.96 \Delta$ (electron Debye length) Δ : grid size (= 1)

Electron-positron jet injected



electron-positron ambient plasma

electron-ion ambient plasma





$Z/_-V_{\perp}$ phase space for jet electrons at $t = 59.8 \omega_{pe}$







All pair plasmas



Magnetic field generation and particle acceleration with narrow injection



(Ramirez-Ruiz, Nishikawa, Hededal 2007)